

# Argument and Story Strength - Bayesian vs. Qualitative Approaches

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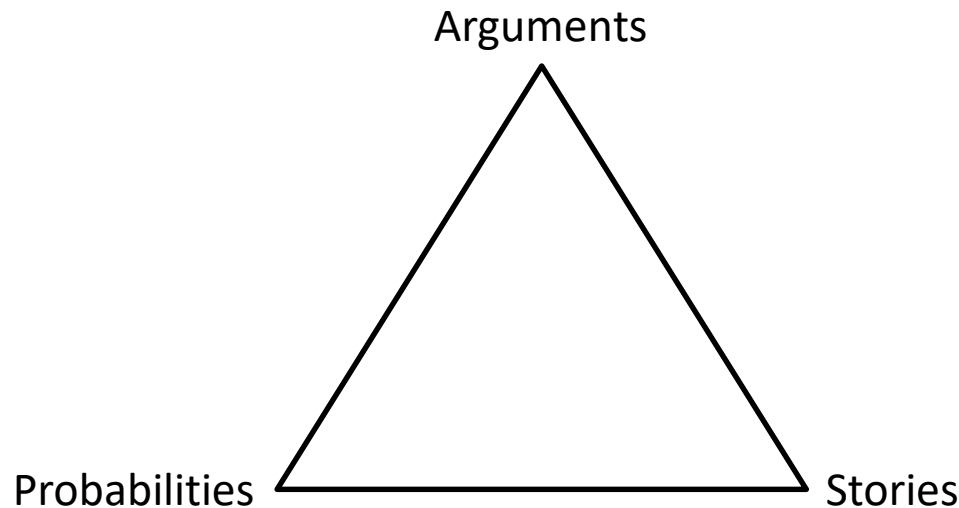
*Tilburg University*

# Stories – Arguments – Probabilities

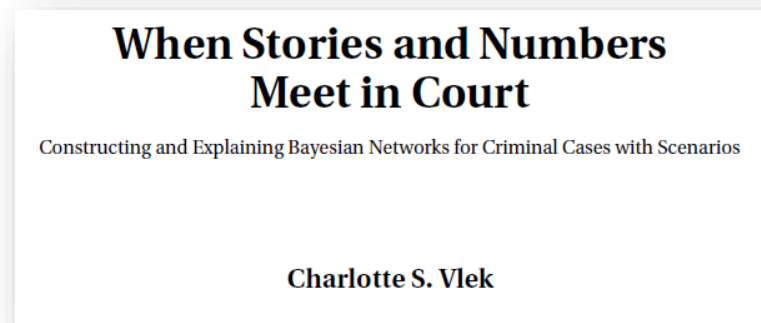
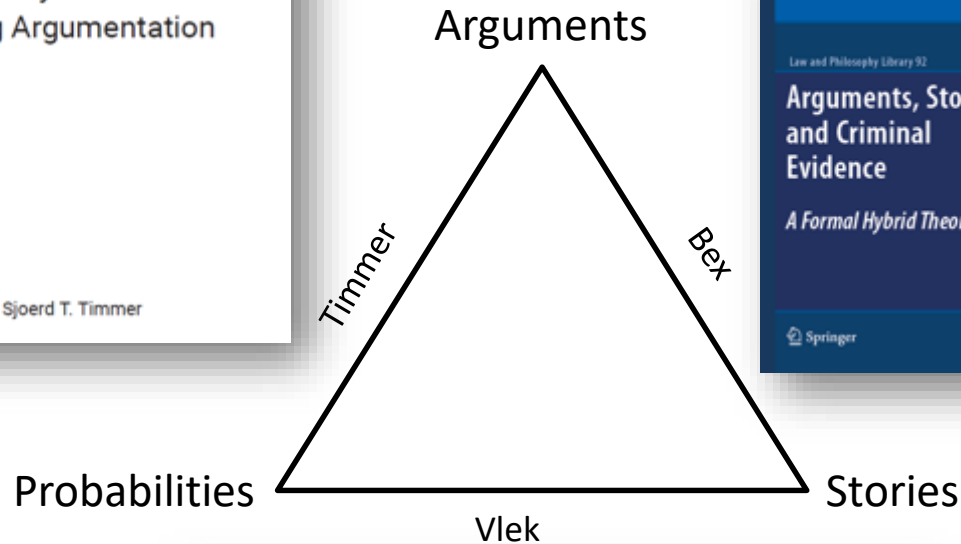
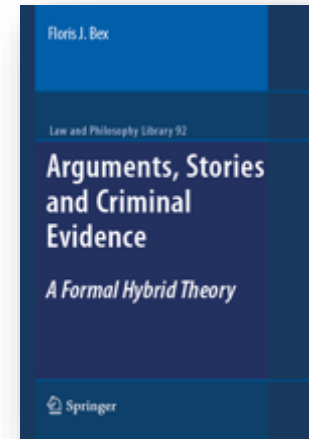
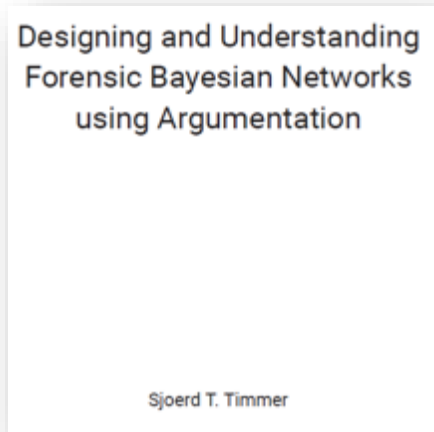
- Explanations are causally coherent sequences of events (*stories*) that explain the evidence in a case.
- Multiple explanations for different conclusions have to be proposed, analysed and compared (*argumentation*), and the “best” (most likely) one should be chosen (*probabilities*)

# Stories – Arguments – Probabilities

- Stories: coherent sequences of events
- Arguments: reasons for or against a conclusion
- Probabilities: measure of likelihood that some event has occurred



# Stories – Arguments – Probabilities



# Stories vs. Arguments

- Stories are “holistic”
- Stories provide an overview
- Stories encapsulate causal reasoning
- Stories represent how humans order a mass of evidence
  
- Arguments are “atomistic”
- Arguments provide a means of detailed analysis
- Arguments encapsulate evidential reasoning
- Arguments represent how humans talk about individual evidence

# Qualitative vs. Quantitative

- Probabilities allow for fine-grained **degrees of uncertainty**
- Probabilities allow for the correct modelling of **probabilistic influences** between evidence & events
- Qualitative approaches require **no precise estimates** of probabilities
- Qualitative approaches are closer to how many **domain experts reason**

# Comparing arguments & stories

- There are various pitfalls when reasoning with stories and arguments, but can we measure how good or strong a story or an argument is?

# Argument Strength

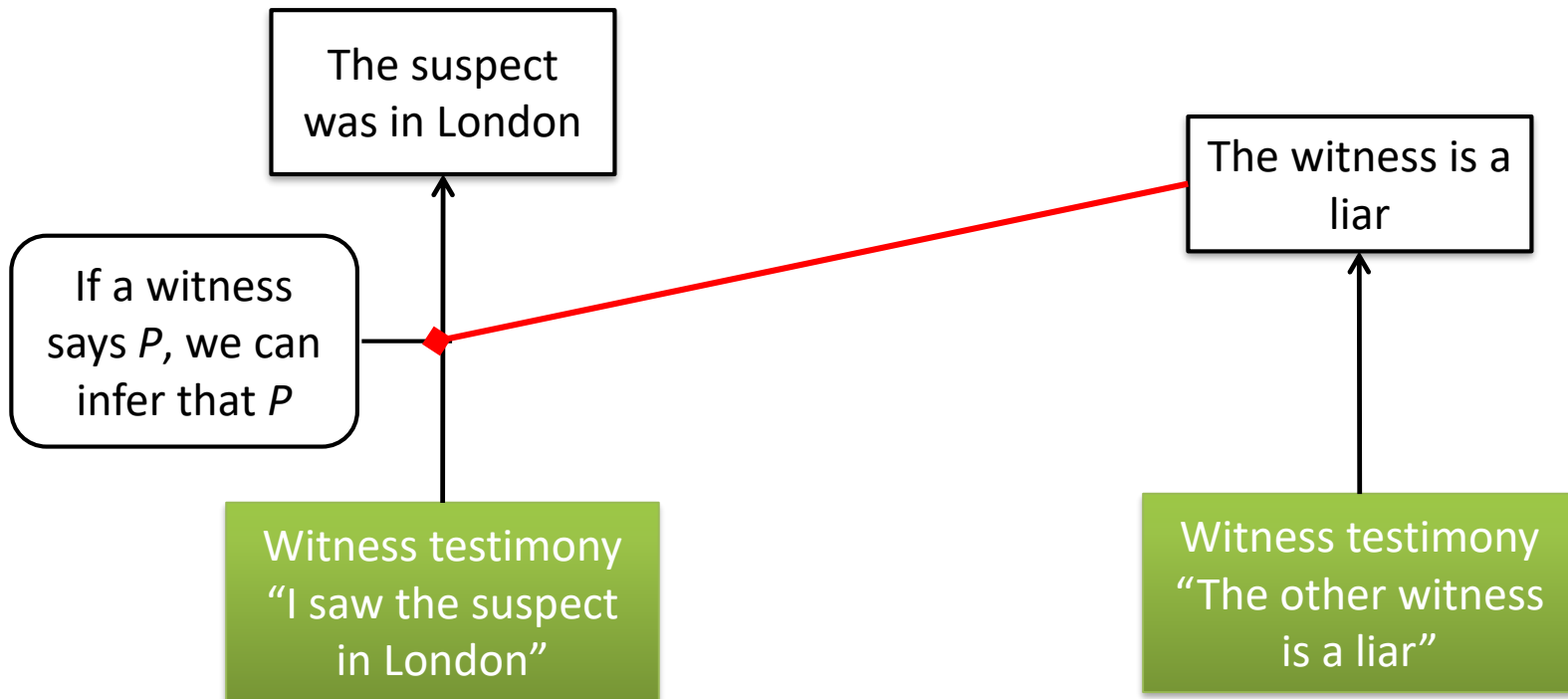
- Which argument wins?





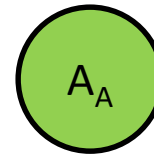
# Argument Strength

- Is the attacker strong enough?



# Dialectical semantics

- Dynamically assign status to arguments
  - Status may change if new arguments are put forward



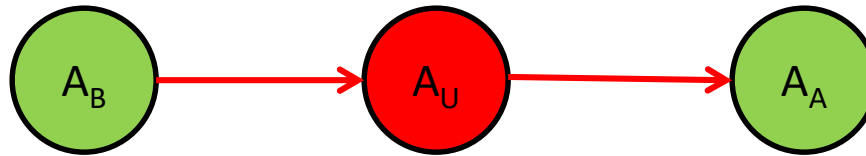
# Dialectical semantics

- Dynamically assign status to arguments
  - Status may change if new arguments are put forward



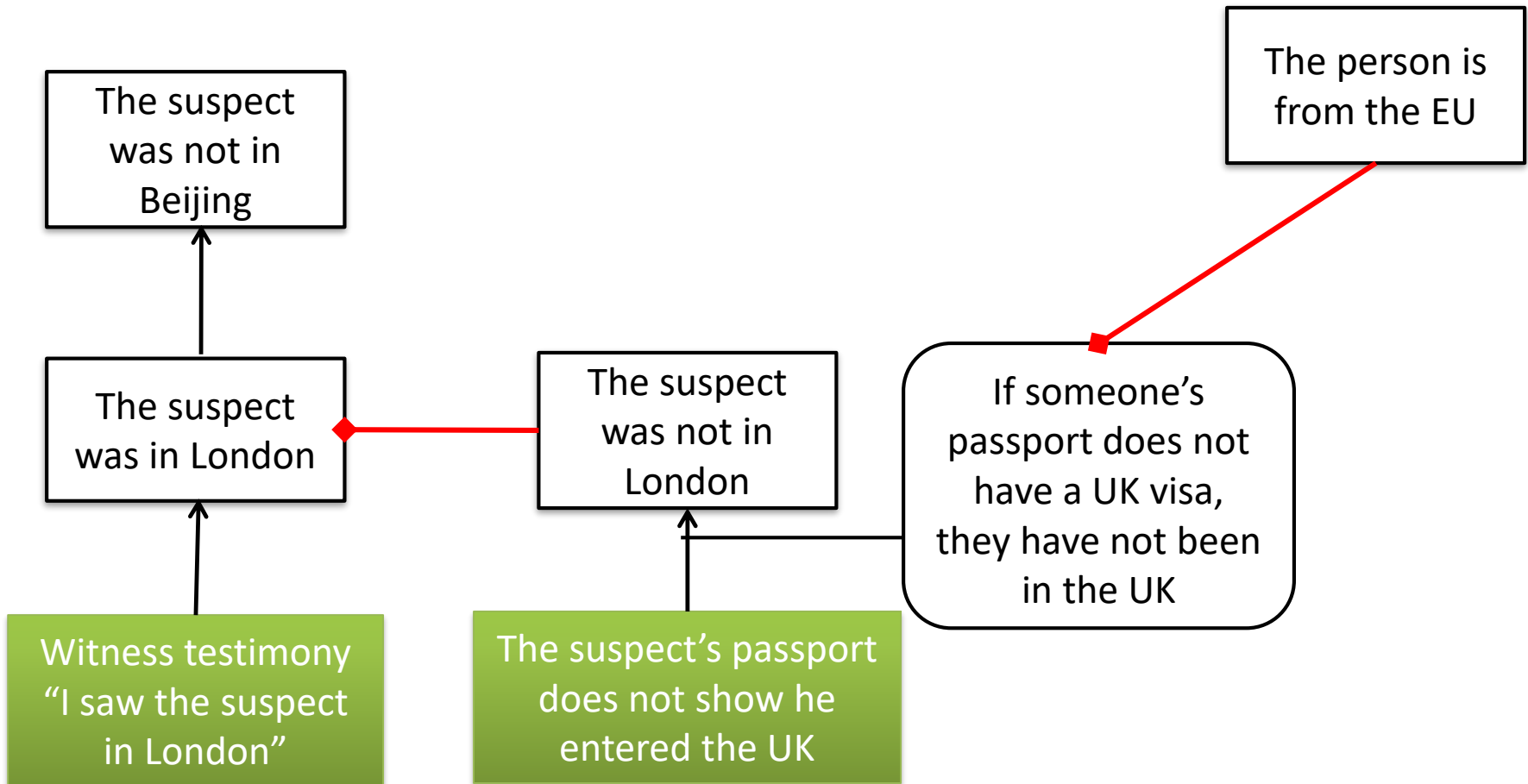
# Dialectical semantics

- Keep attacking until you win!



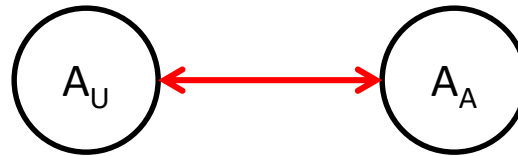
*"The one who has the last word laughs best"*

# Reinstatement



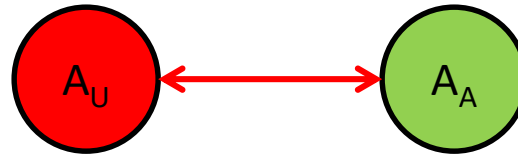
# Dialectical semantics

- But how to choose between 2 arguments that attack each other?



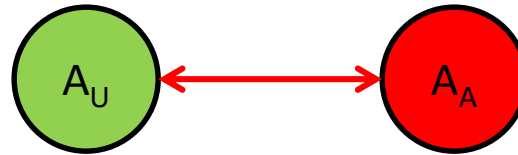
# Dialectical semantics

- Strength of arguments
  - $A_U < A_A$  ( $A_a$  is preferred over  $A_U$ )



# Dialectical semantics

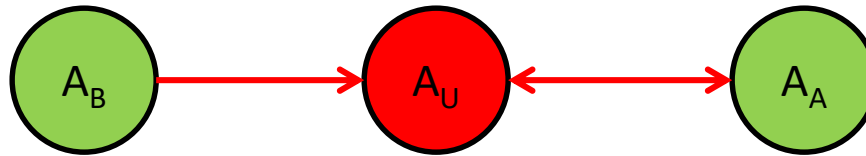
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# Dialectical semantics

- Keep attacking until you win!



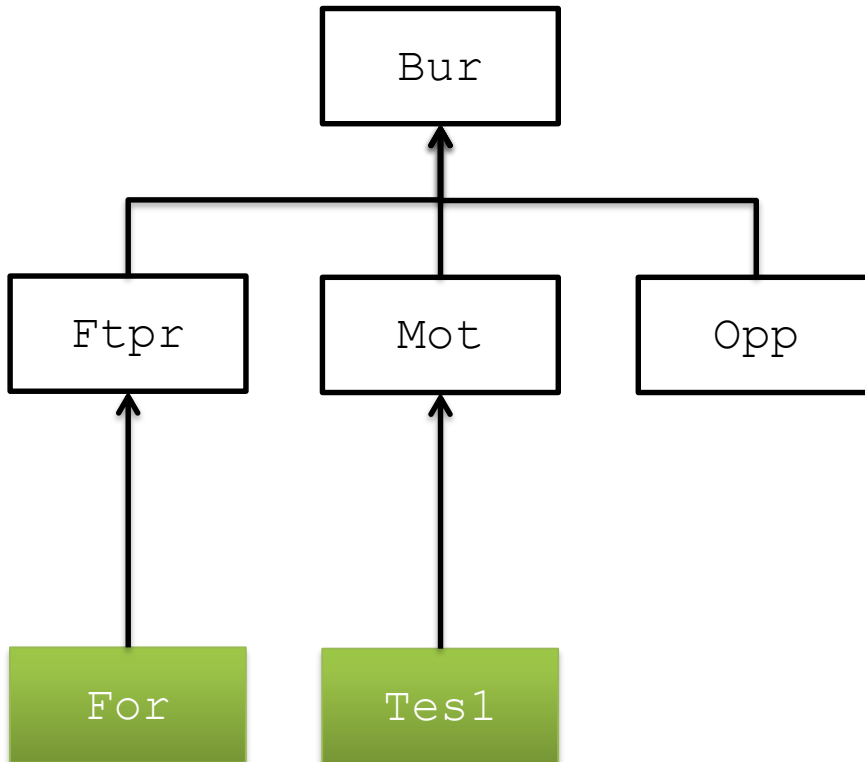
*"The one who has the last word laughs best"*

# Reinstatement



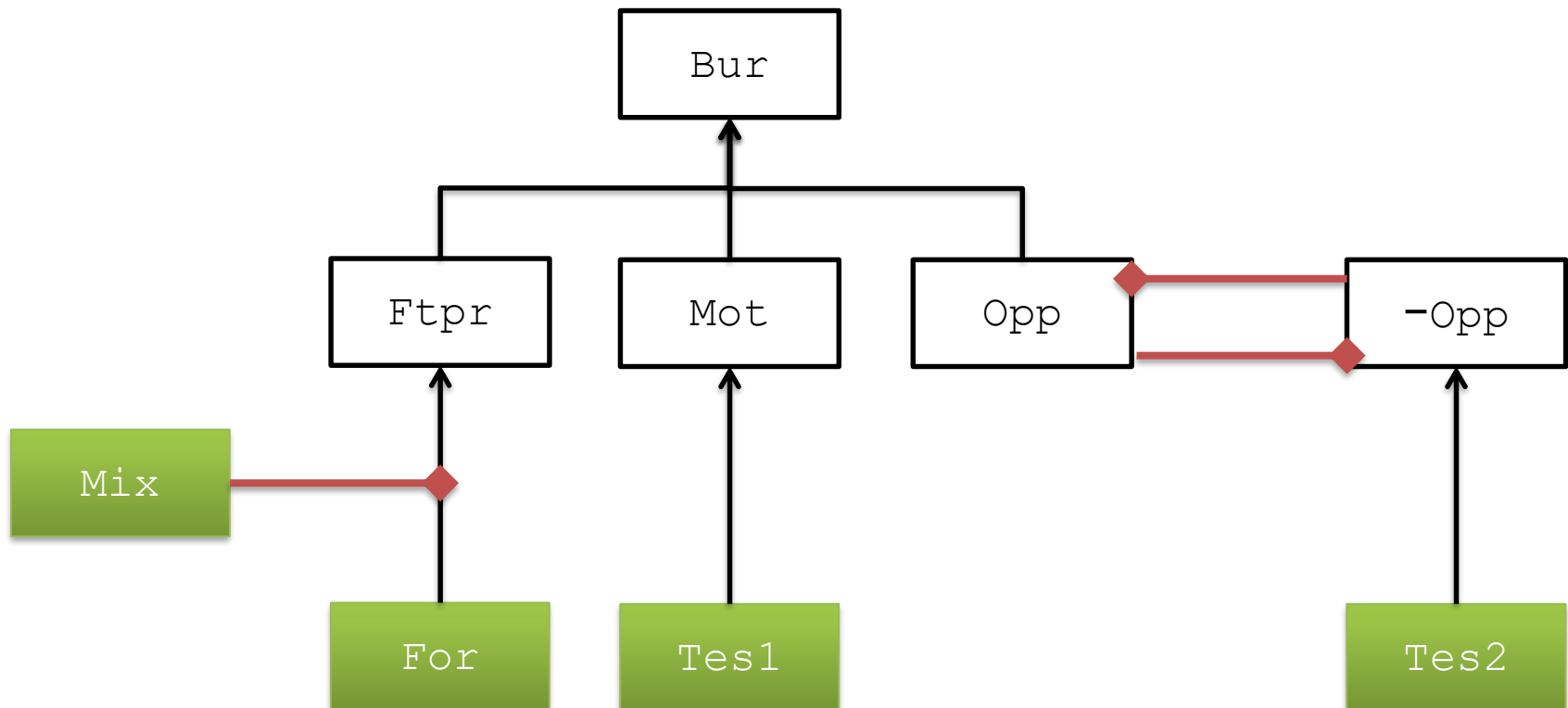
# Structured arguments vs. Bayesian Networks

- The burglary ( $B_{ur}$ ) was committed by the suspect, because there is a footprint match ( $F_{tpr}$ ) and a motive ( $M_{ot}$ ) backed by a report ( $F_{or}$ ) and a testimony ( $T_{es1}$ ), and the suspect has no alibi, so  $O_{pp}$ .



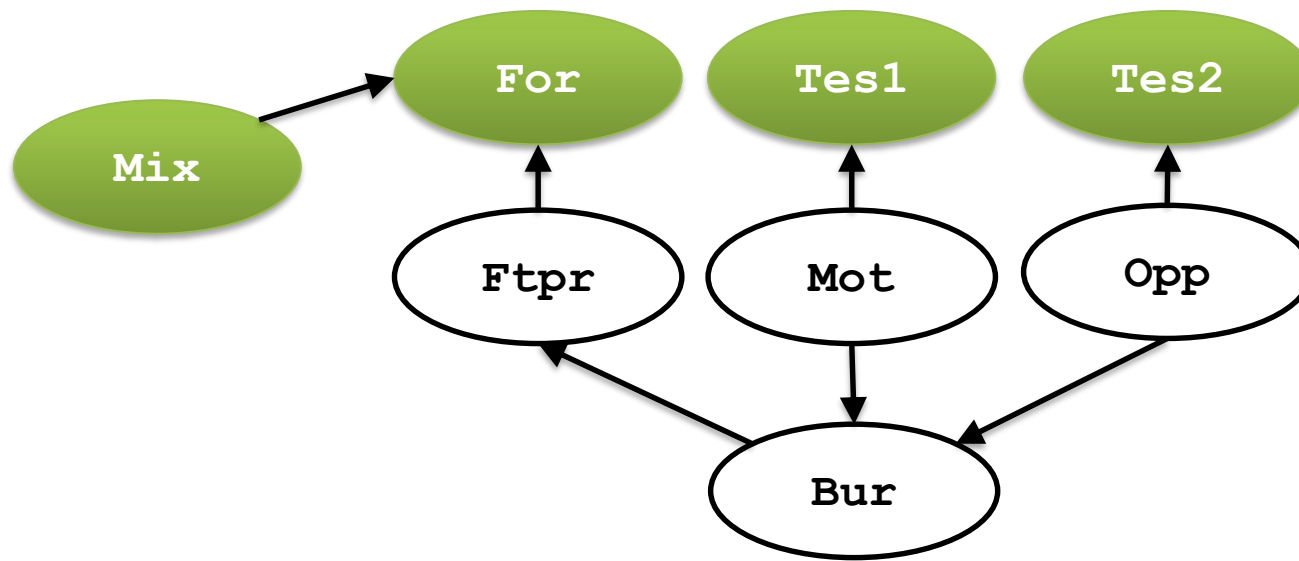
# Structured arguments vs. Bayesian Networks

- However, there is evidence of a mixup in the lab ( $Mix$ ), which means the footprint match is not really backed by evidence. Furthermore, the suspect later gave a testimony ( $Tes2$ ) with an alibi, so  $\neg Opp$ .



# Structured arguments vs. Bayesian Networks

- Represent joint probability distribution as DAG + CPT
- Directed Acyclic Graph
  - Nodes are variables **Bur** = [Bur, -Bur]
  - Arcs represent probabilistic dependencies between nodes (**Mot**, **Bur**)

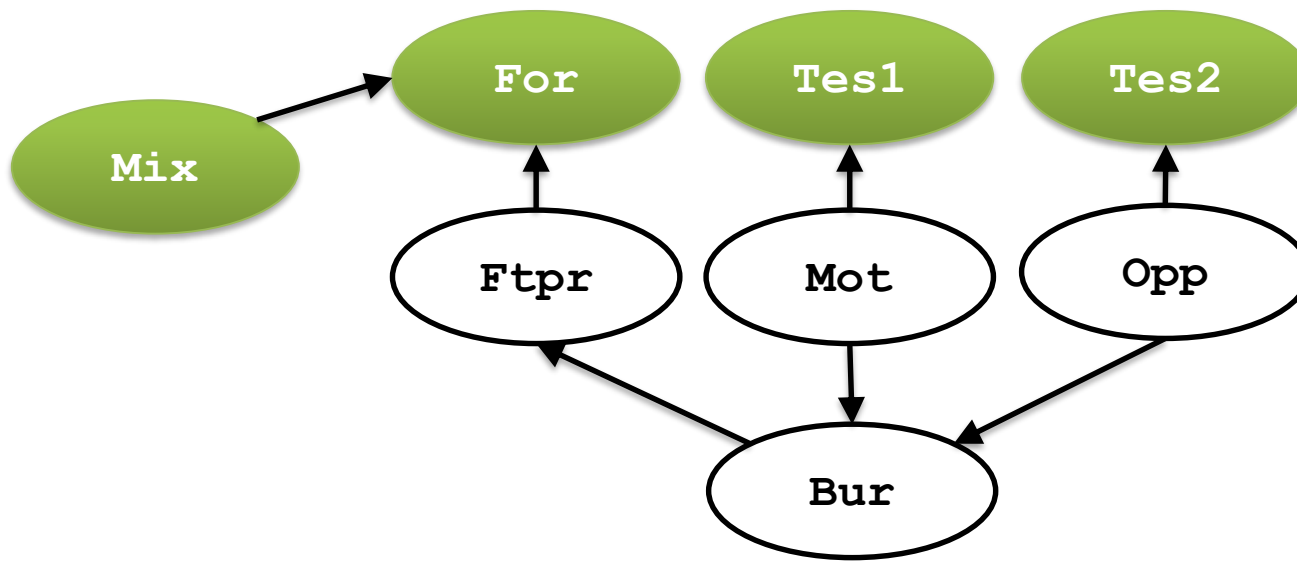


# Probabilistic reasoning

- Probability of events and the links between evidence/events
- Probability of a proposition (event) being true or false
  - $P(e)$ ,  $P(\neg e)$
  - $P(e) + P(\neg e) = 1$
- Conditional probability of  $e$  given evidence  $ev$ 
  - $P(e | ev)$
- Probability of observed variable (evidence) = 1

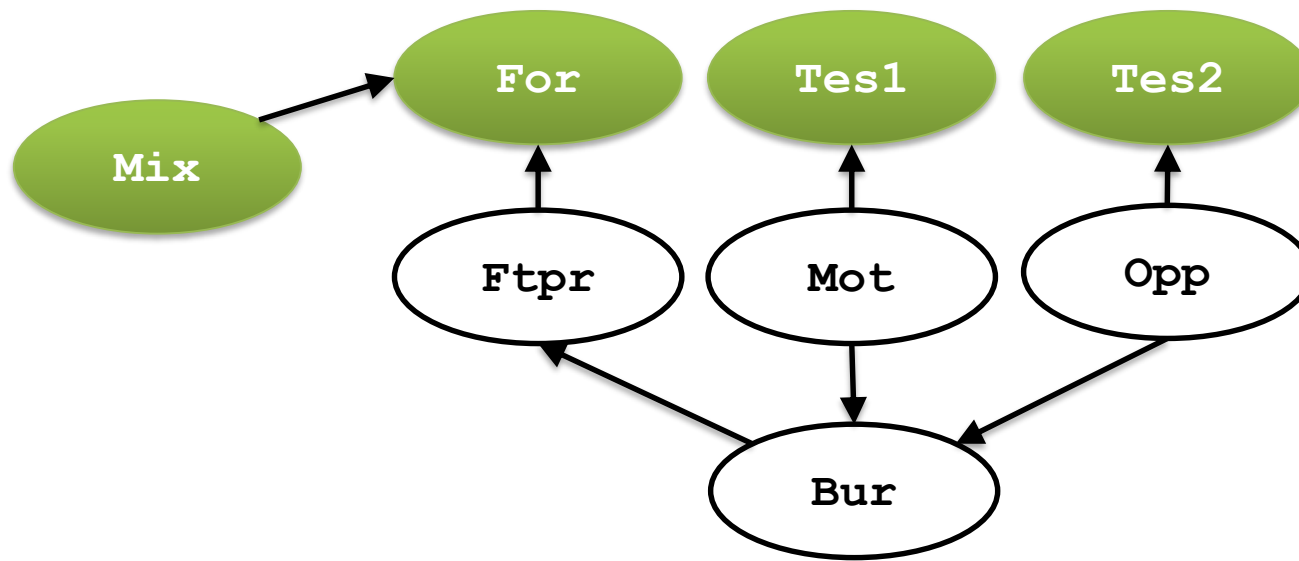
# Bayesian Networks

- (Conditional) probabilities
  - $\Pr(\text{Mot})=0.4$ ;  $\Pr(-\text{Mot})=0.6$ ;
  - $\Pr(\text{Ftpr} \mid \text{Bur})=0.8$ ;  $\Pr(-\text{Ftpr} \mid \text{Bur})=0.2$   
 $\Pr(\text{Ftpr} \mid -\text{Bur})=0.01$ ;  $\Pr(-\text{Ftpr} \mid -\text{Bur})=0.99$
  - $\Pr(\text{Tes1}) = 1$



# Bayesian Networks

- Given the evidence and all the probabilities, we can precisely calculate the posterior probability of the conclusion (Bur)





# Inference to the Best Explanation

- Given observations, hypothesise possible explanations
  - I have a cough – cold or flu?
  - Computer fails to start – why?
  - Body found – what happened?
- Choose the “best” explanation
  - Strongest explanation
- How to determine strength of explanations?
  - Using argumentation? Using Bayesian networks?

# Formal IBE

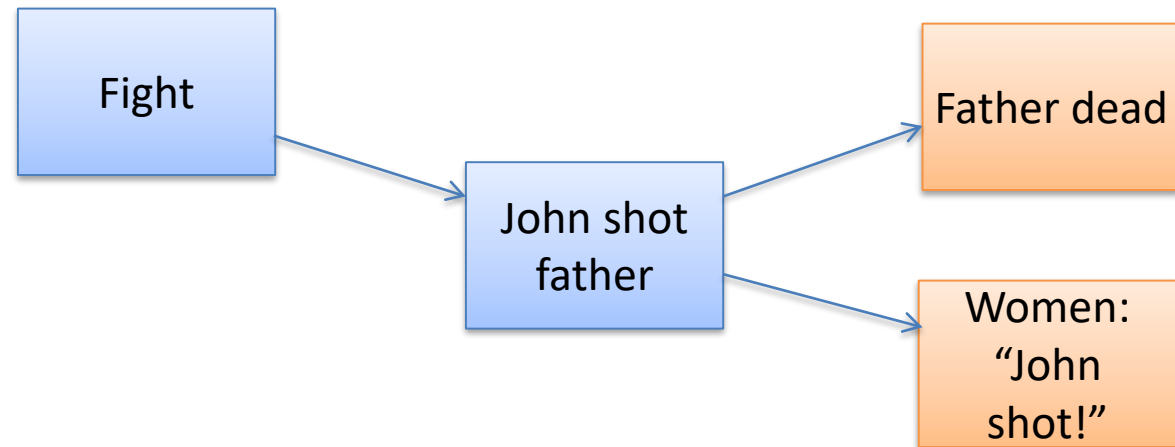
- Given a set of observations  $O$

Father dead

Women:  
"John  
shot!"

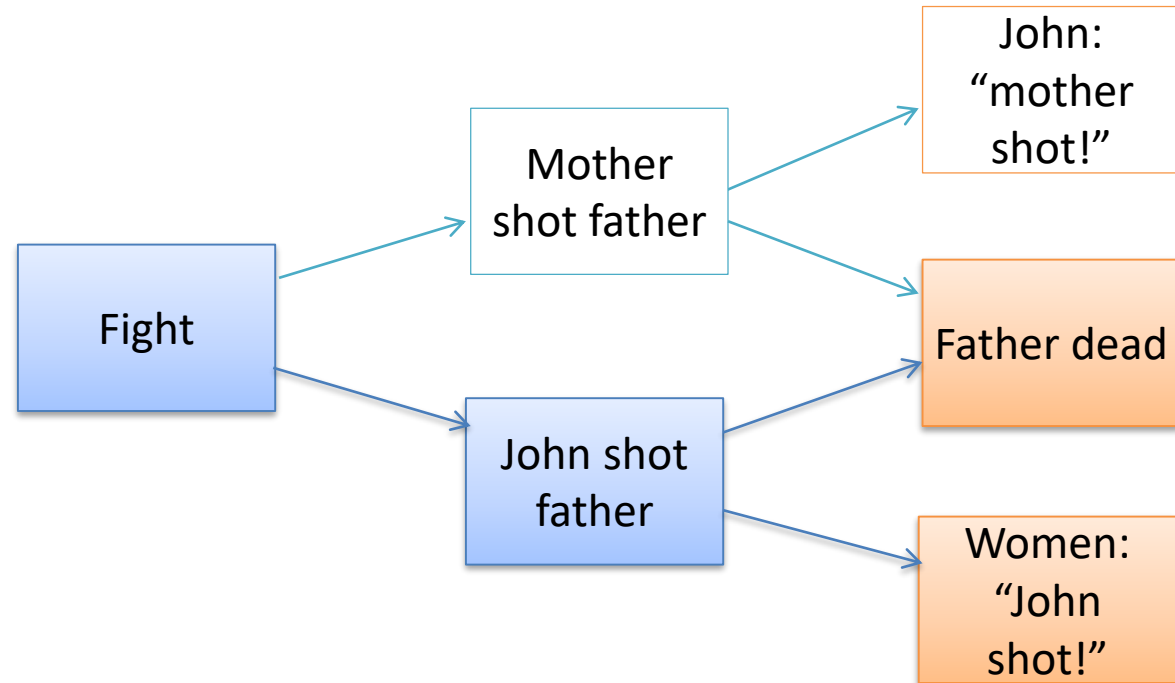
# Formal IBE

- Assume hypothesis  $H$  and rules  $R$  s.t.  
 $H, R \vdash O$



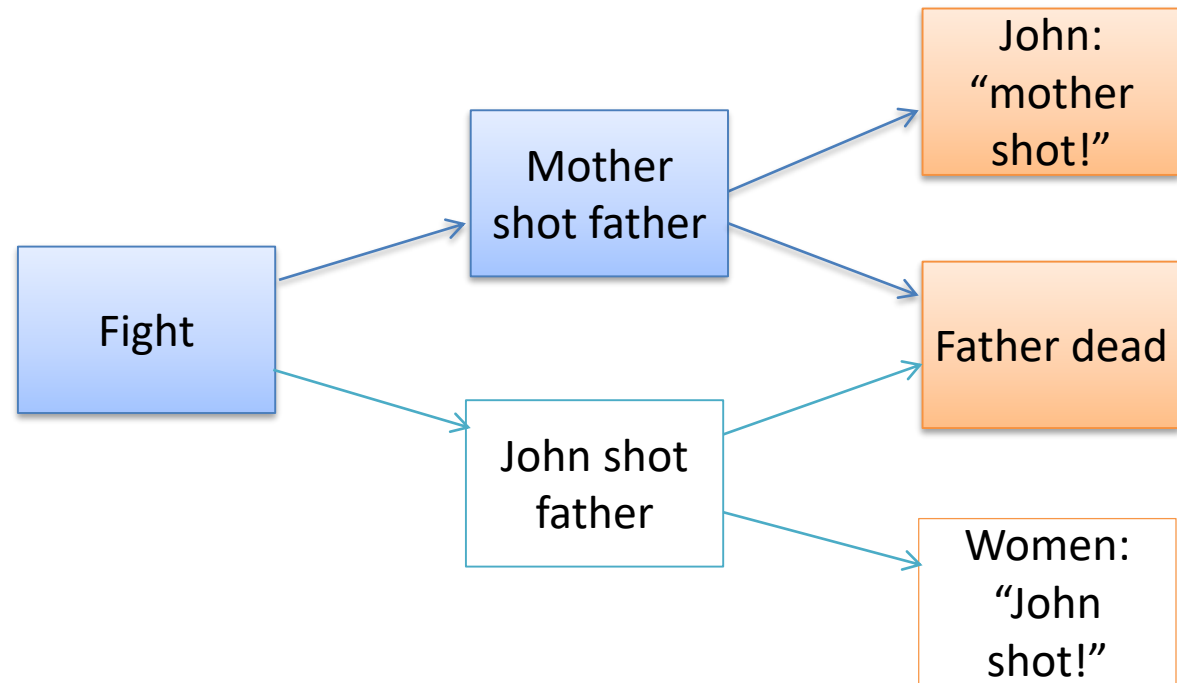
# Formal IBE

- Alternative explanations



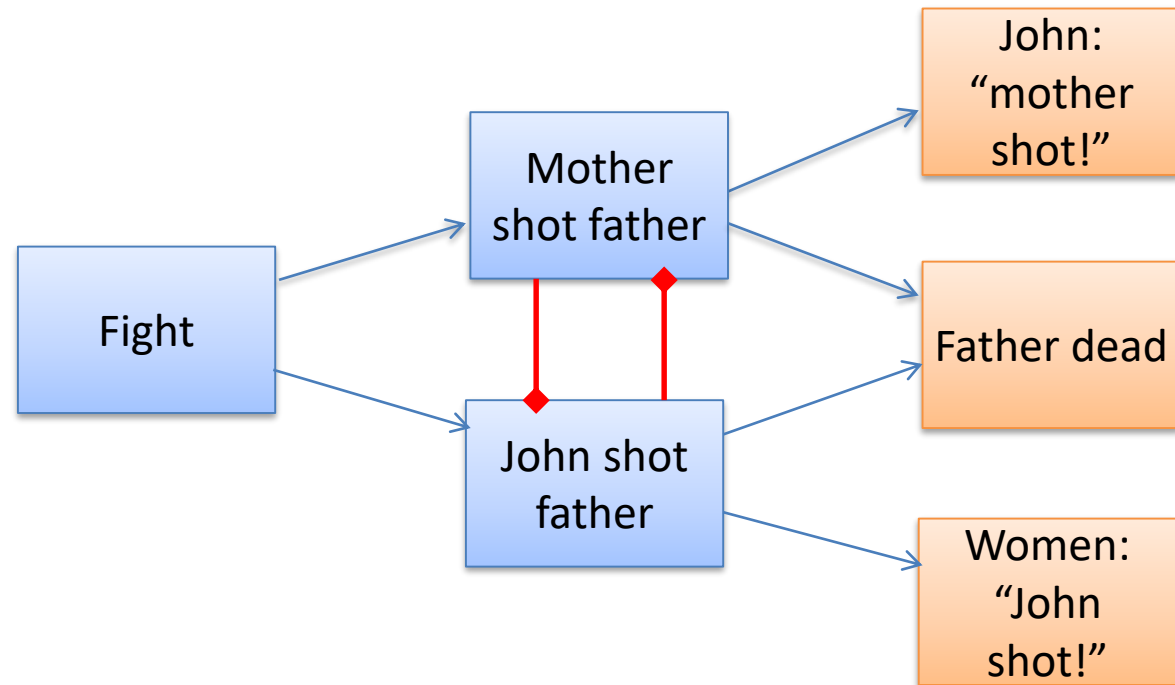
# Formal IBE

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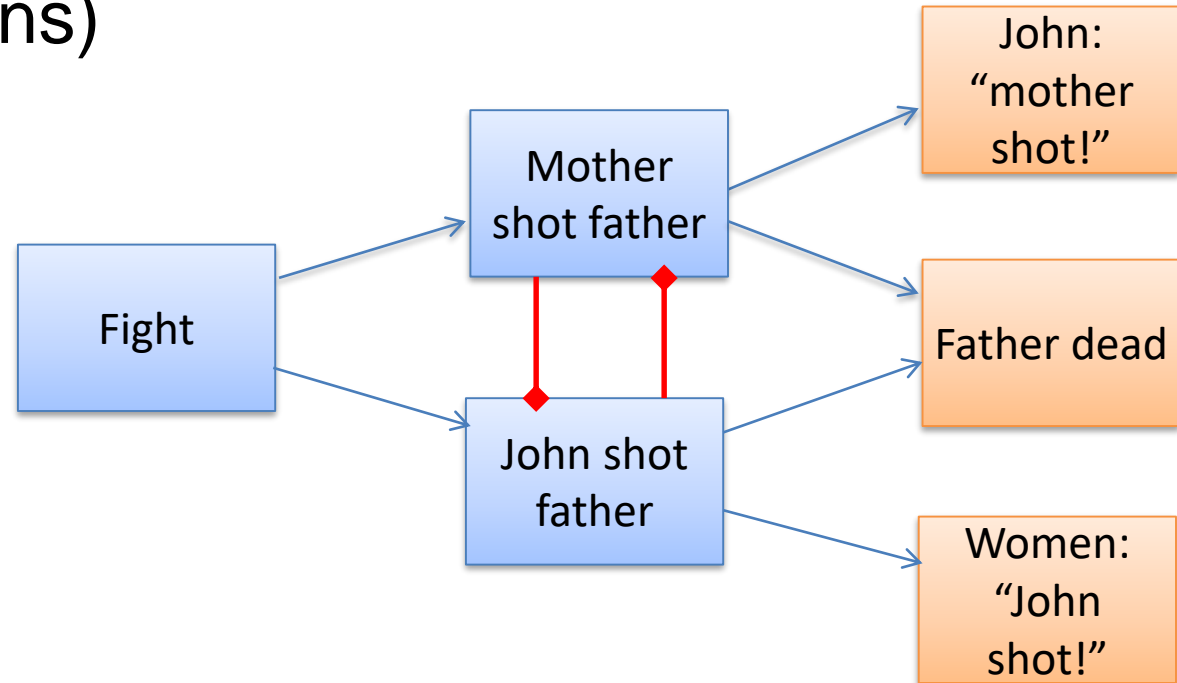
# Argumentative IBE

- Defeasible explanations (i.e.  $H, R \mid \sim O$ )
- Explanations as contradictory arguments



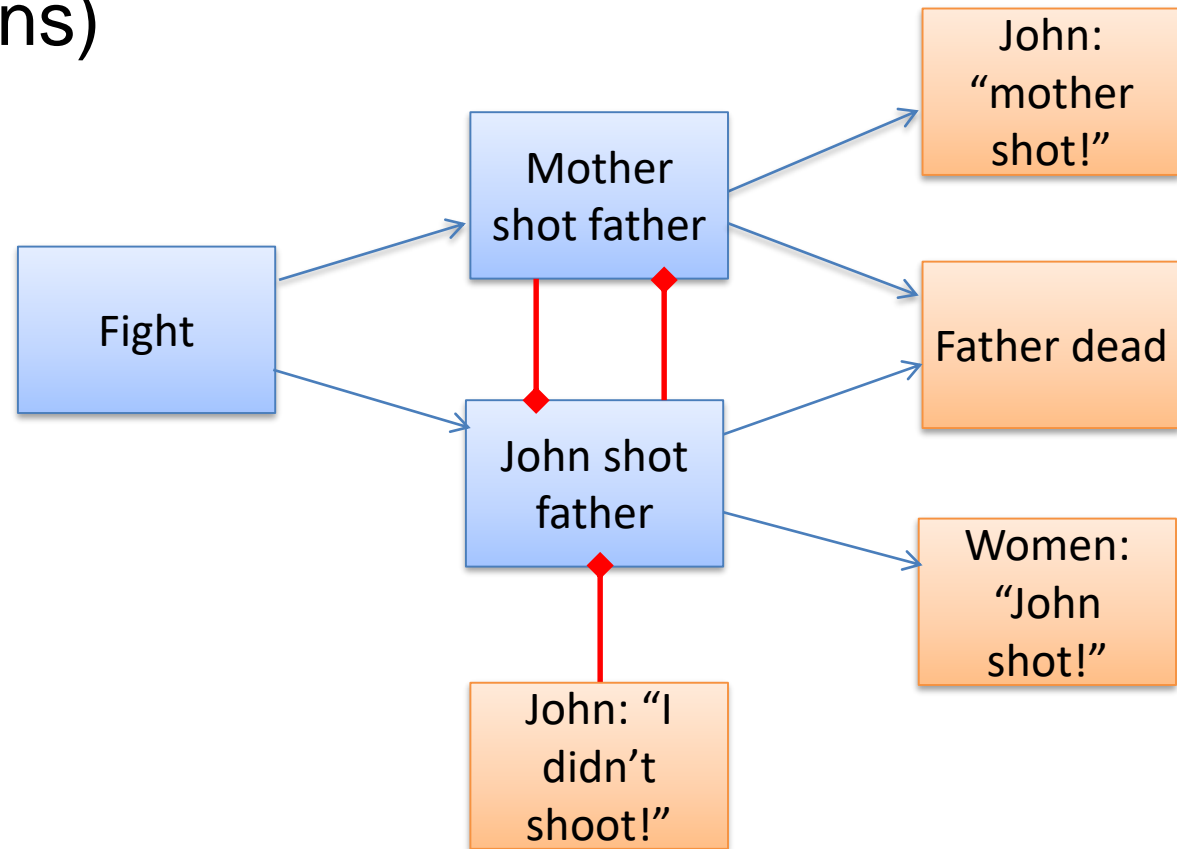
# Argumentative IBE

- Explanations themselves can be attacked/supported by arguments (based on observations)



# Argumentative IBE

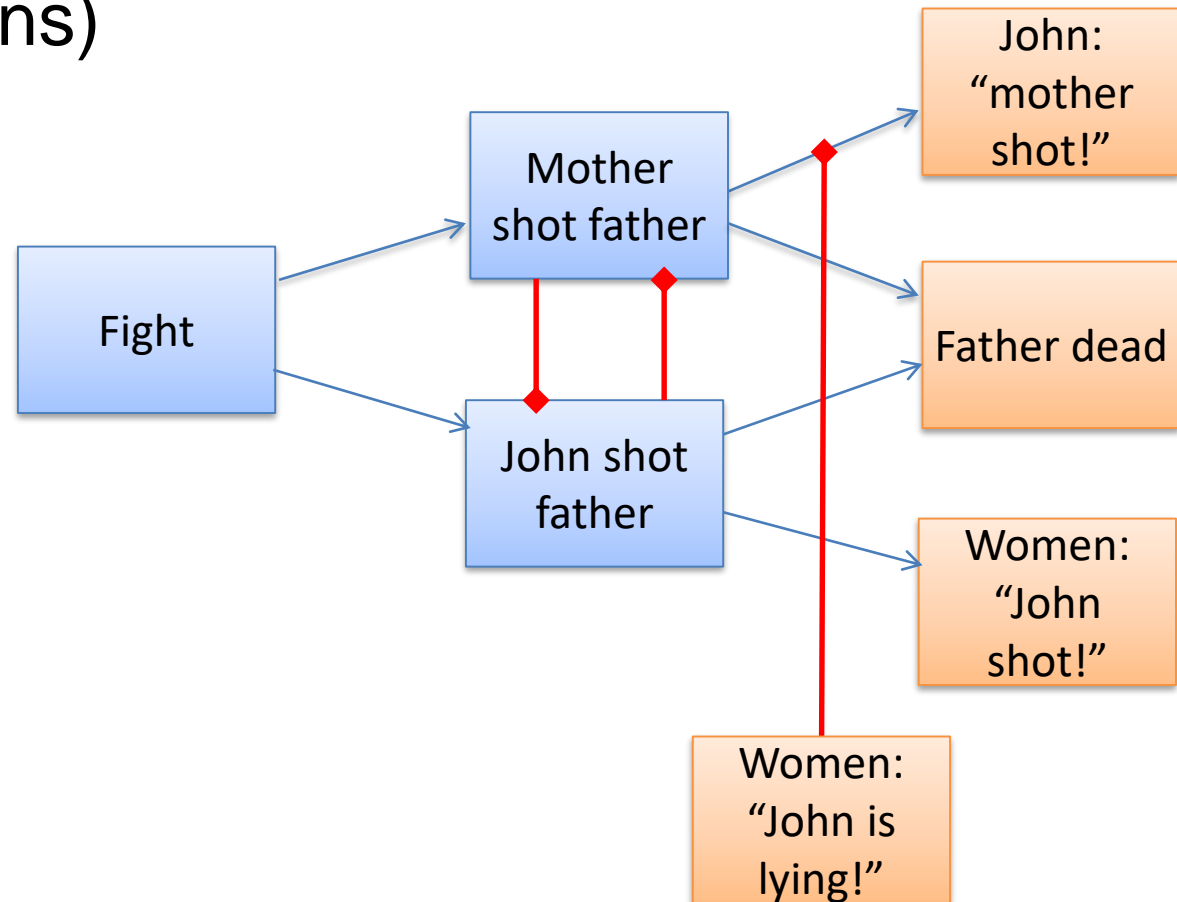
- Explanations themselves can be attacked/supported by arguments (based on observations)





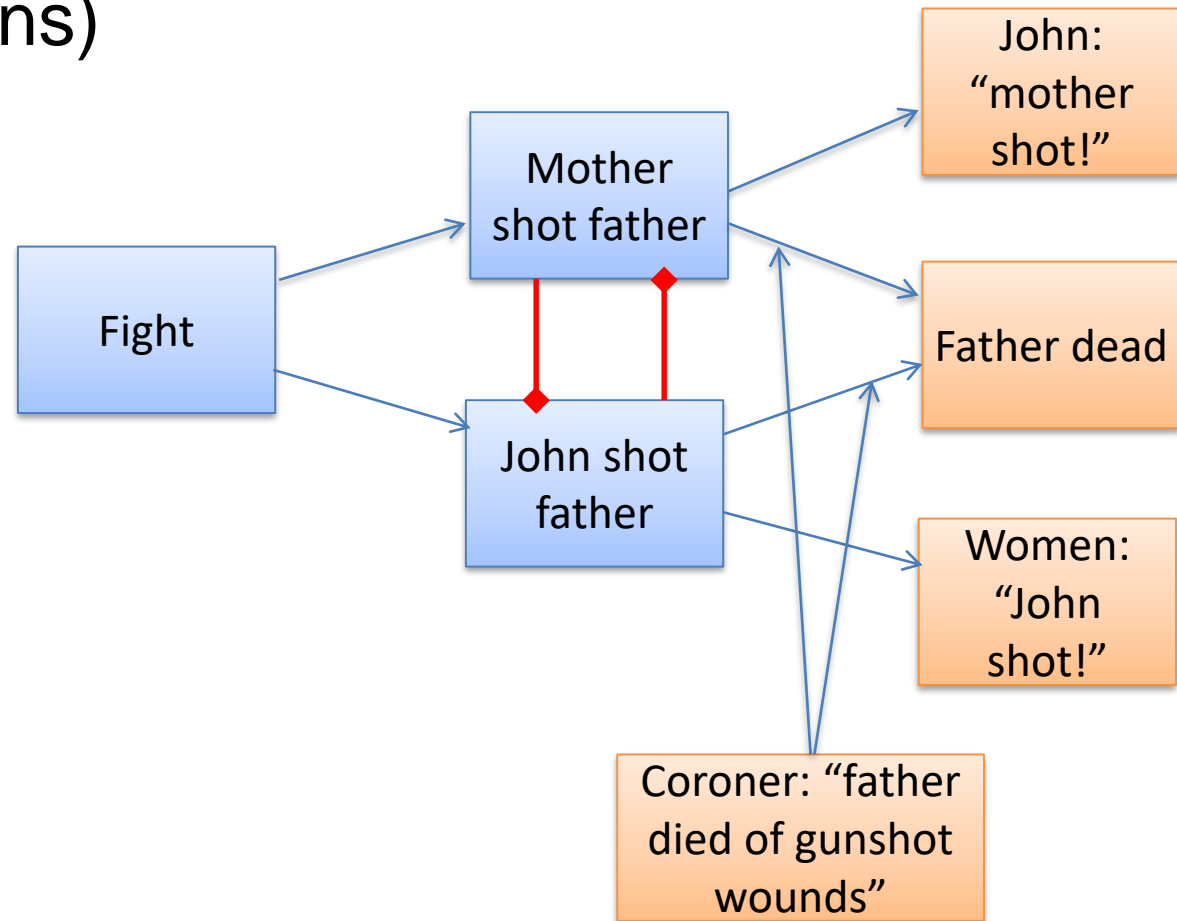
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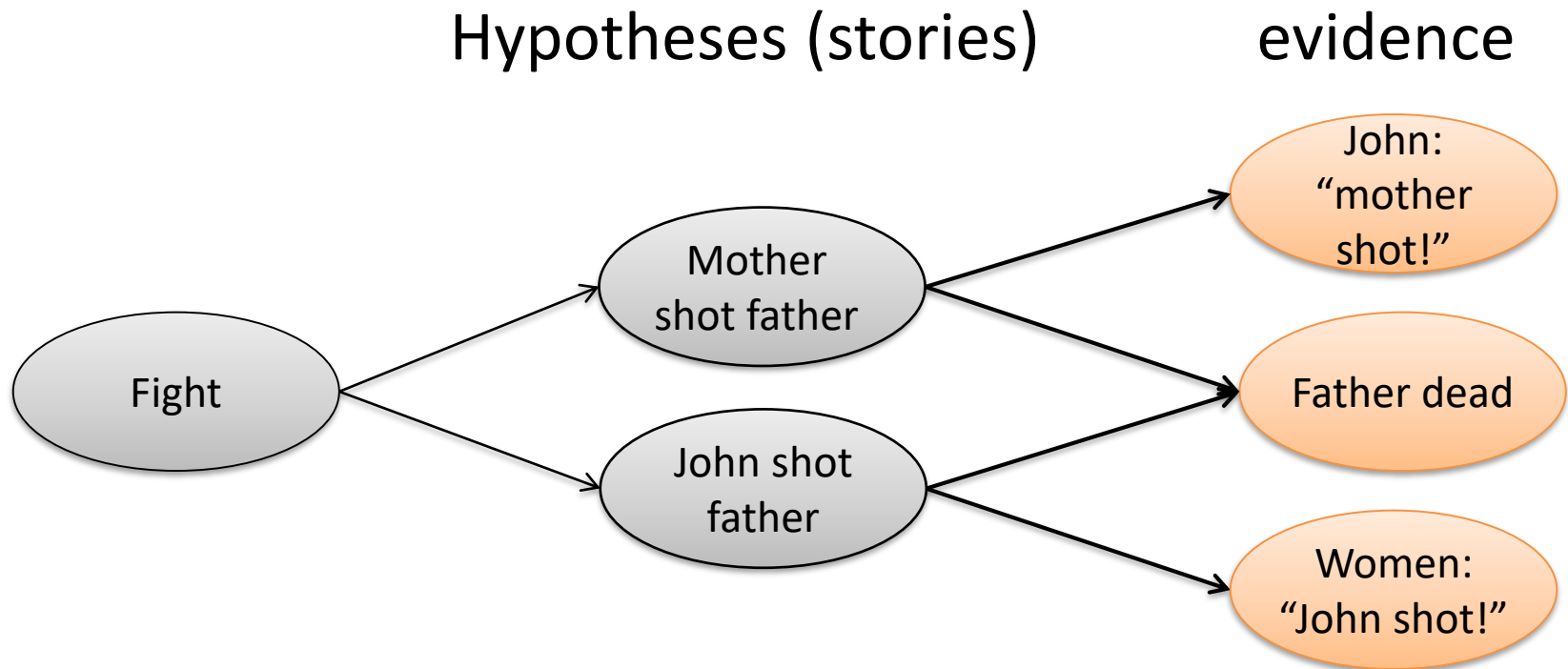
# Argumentative IBE

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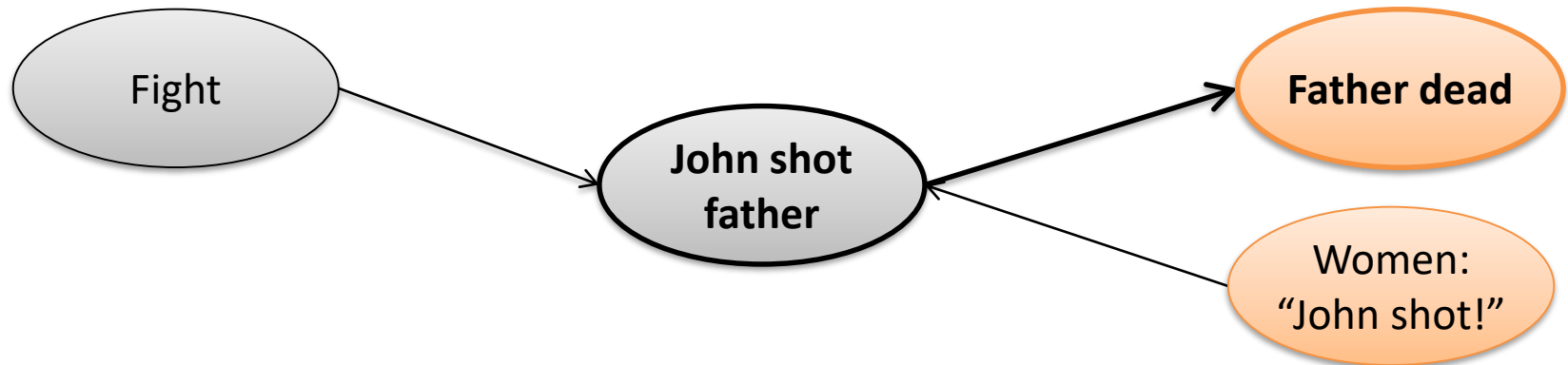
# Capturing IBE Structure

- Alternative stories



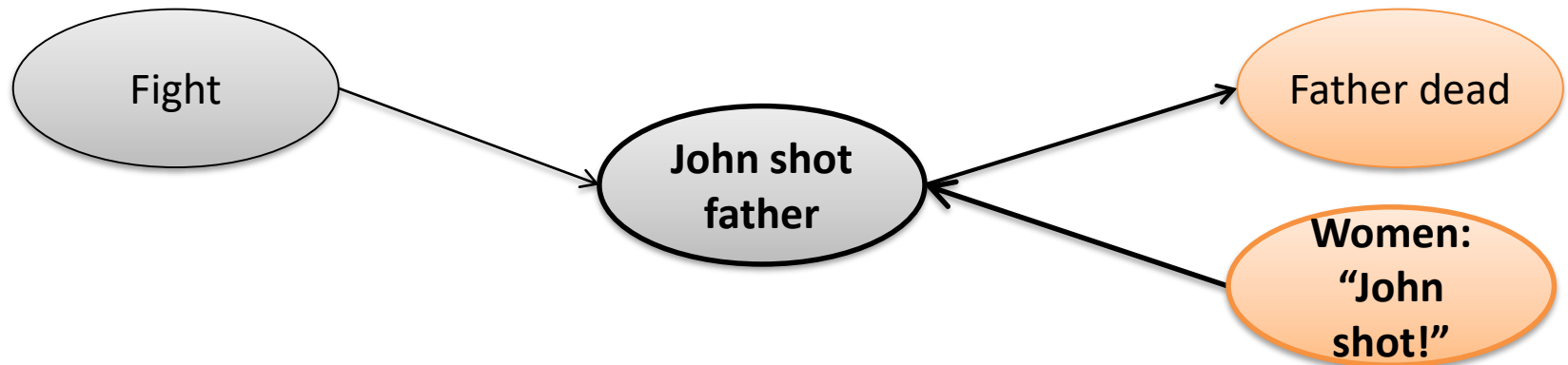
# Capturing IBE Structure

- Causal reasoning:
  - John shooting father causes father to die  
*The story explains the evidence*



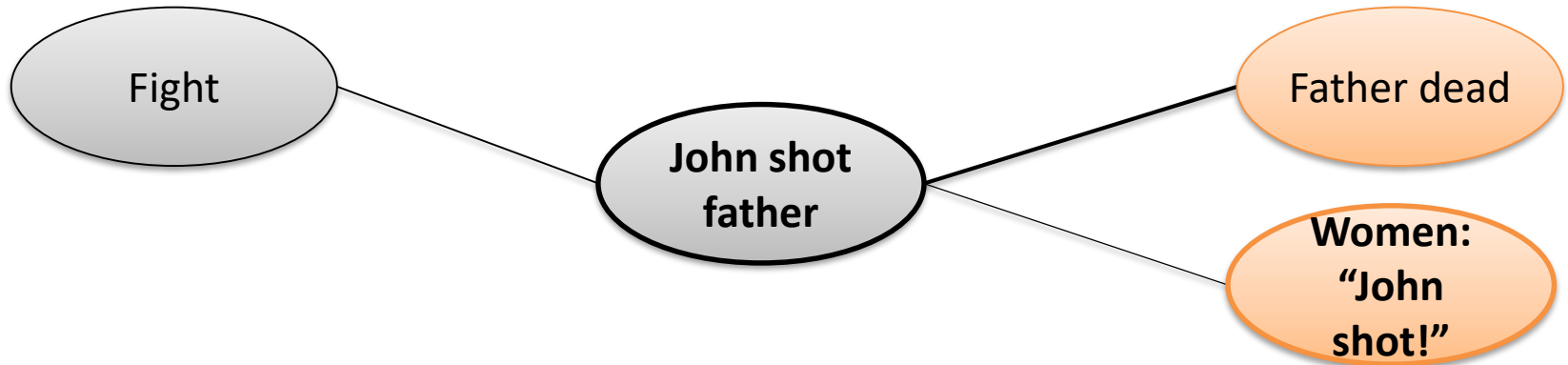
# Capturing IBE Structure

- Evidential reasoning:
  - Women saying “John shot father” is evidence for John shot father  
*Testimony supports the story*



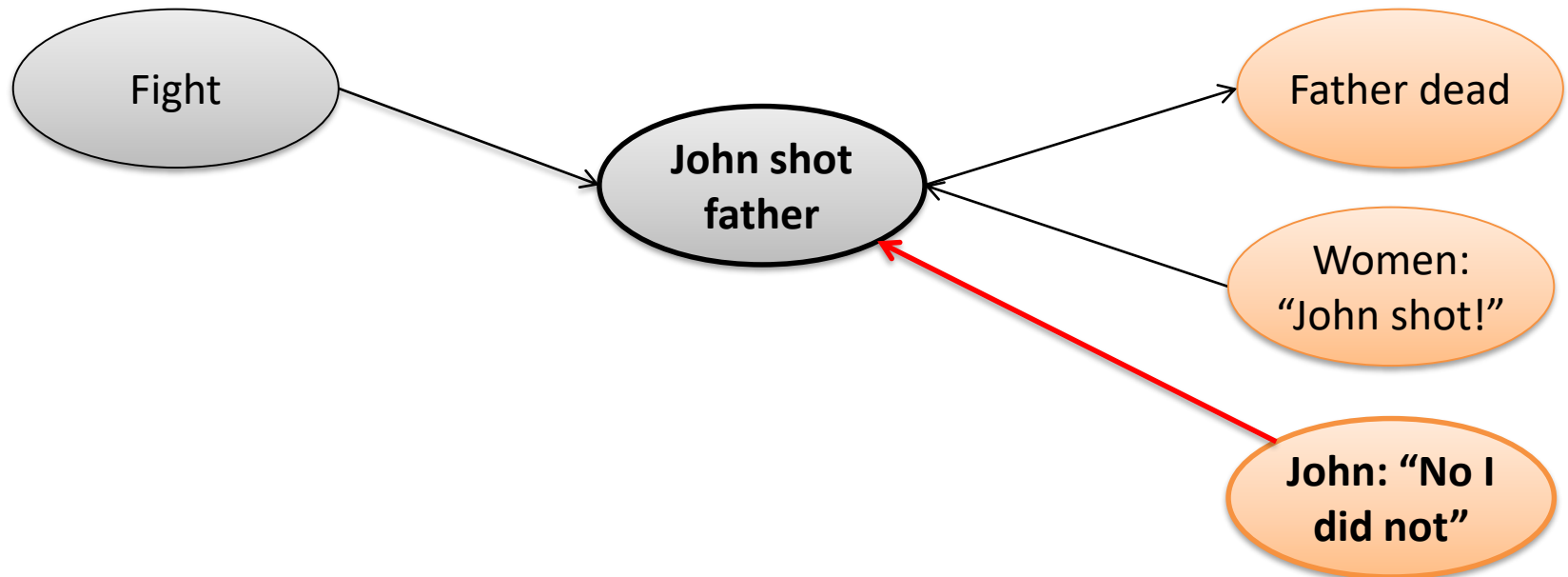
# Capturing IBE Structure

- Directions of arrows (inference) does not matter!



# Capturing IBE Structure

- Contradictory evidence
  - John’s denial attacks the fact that John shot father  
*The evidence contradicts the story*

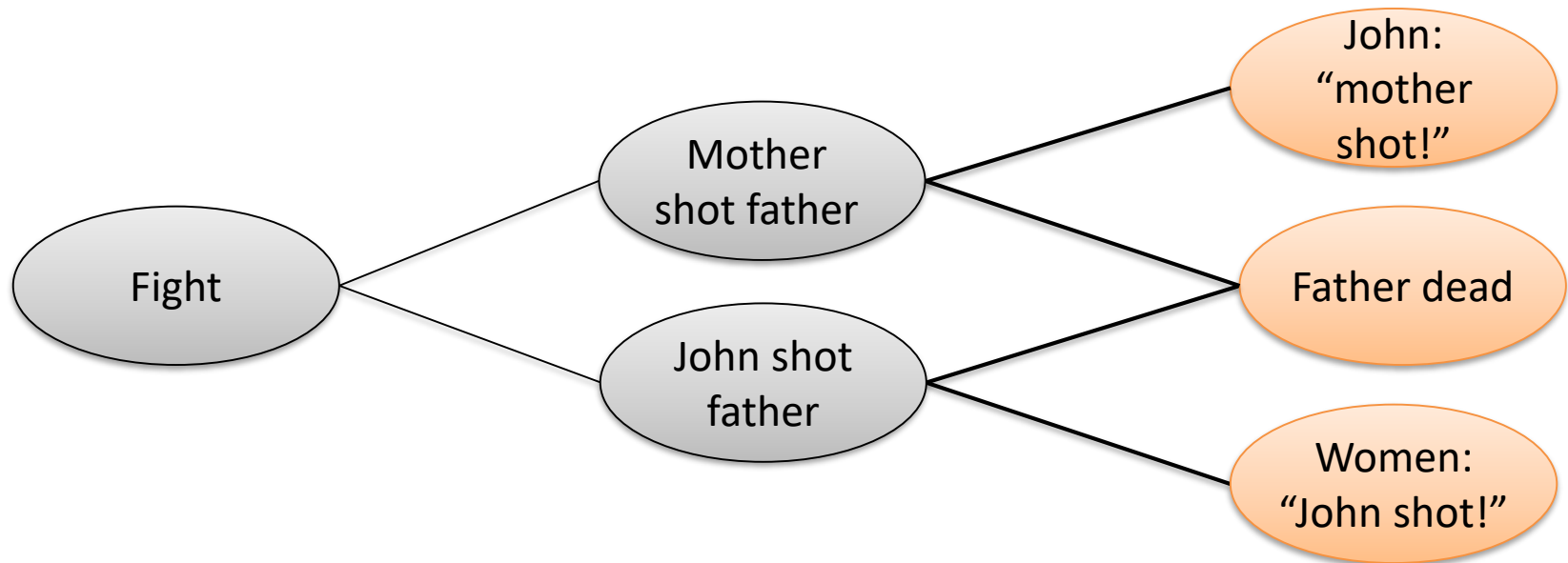


# Capturing IBE Structure

- Can be sets of (logical) propositions with support (argumentation) and causal (story) links

Hypotheses (stories)

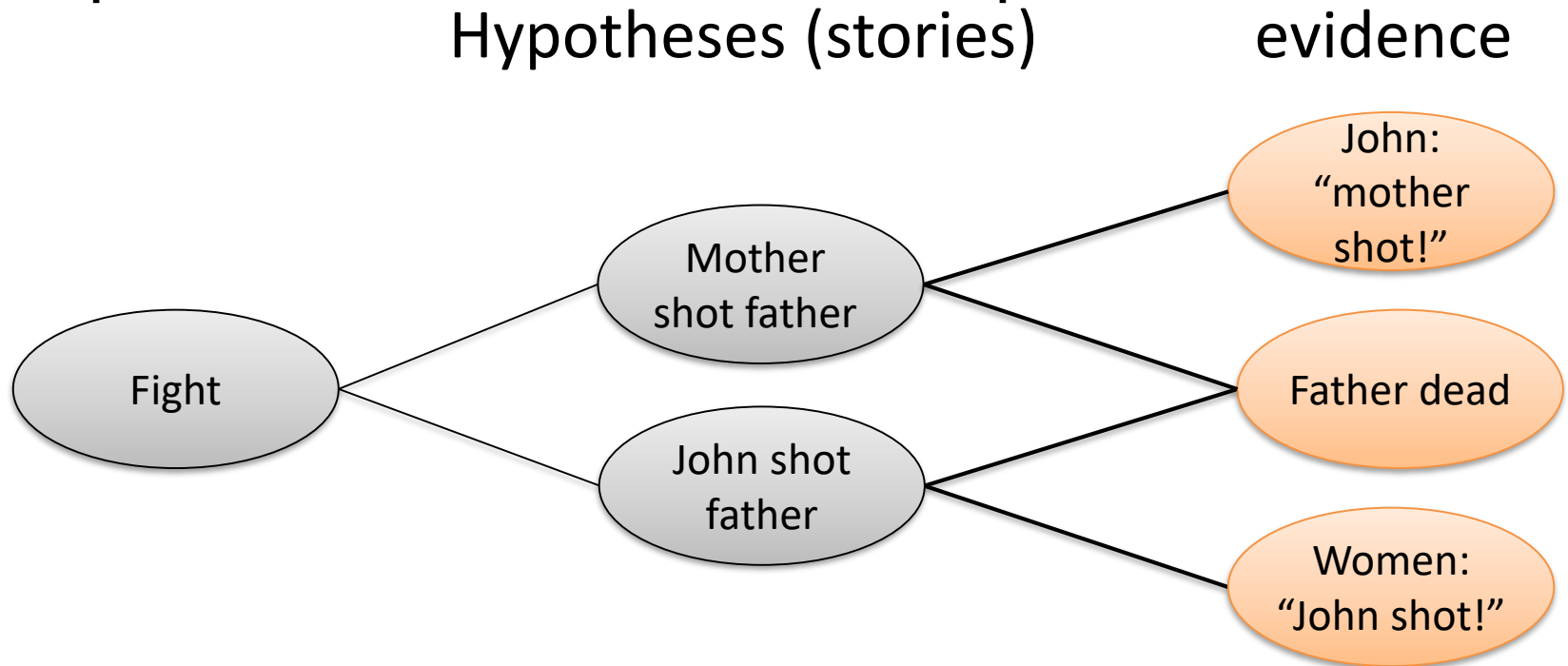
evidence





# Capturing IBE Structure

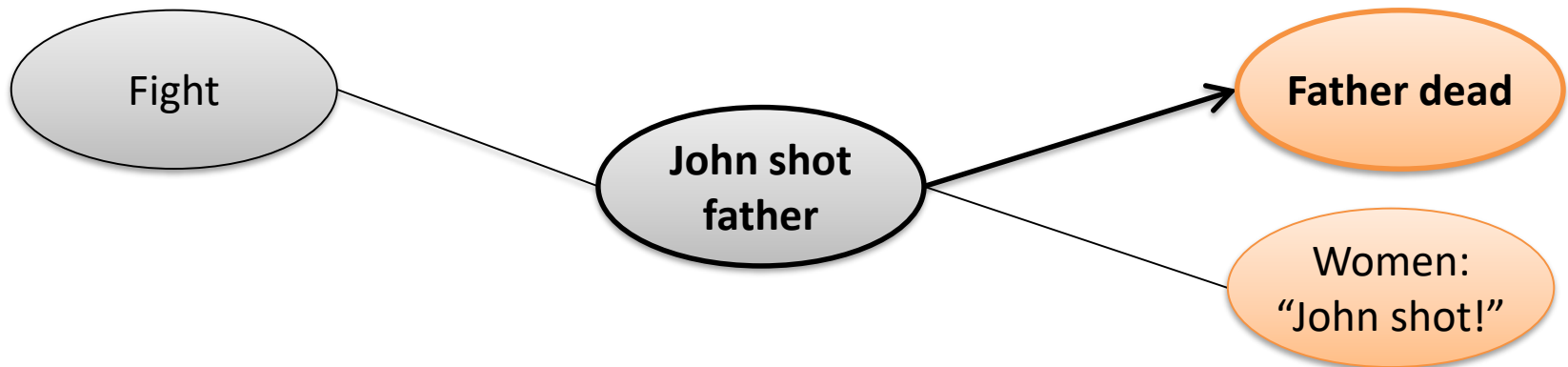
- But also a Bayesian Network where nodes represent variables and link dependencies



# Capturing IBE

## Adding probabilities

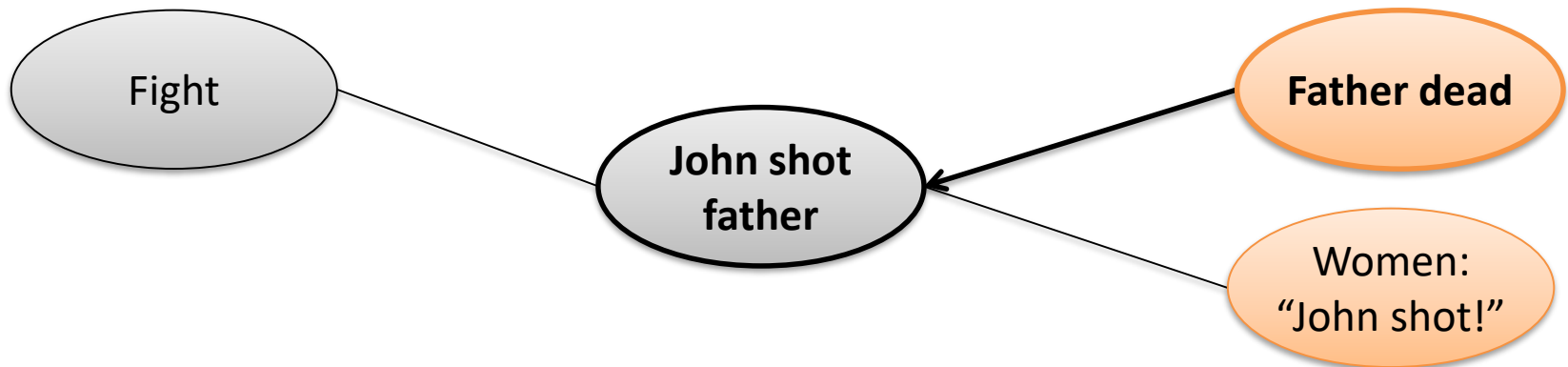
- Conditional probabilities
  - $\Pr(f\_dead \mid J\_shot) + \Pr(\neg f\_dead \mid J\_shot) = 1$
  - $\Pr(f\_dead \mid \neg J\_shot) + \Pr(\neg f\_dead \mid \neg J\_shot) = 1$
- Depends on direction of arrow



# Capturing IBE

## Adding probabilities

- Conditional probabilities
  - $\Pr(J\_shot \mid f\_dead) + \Pr(\neg J\_shot \mid f\_dead) = 1$
  - $\Pr(J\_shot \mid \neg f\_dead) + \Pr(\neg J\_shot \mid \neg f\_dead) = 1$
- Depends on direction of arrow

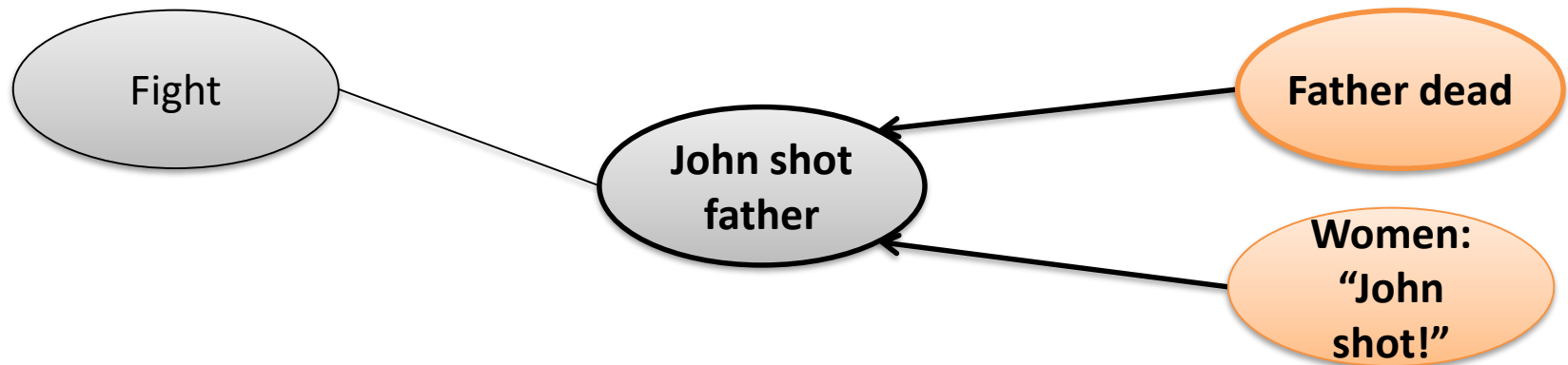


# Capturing IBE

## Adding probabilities

- **Conditional probabilities**

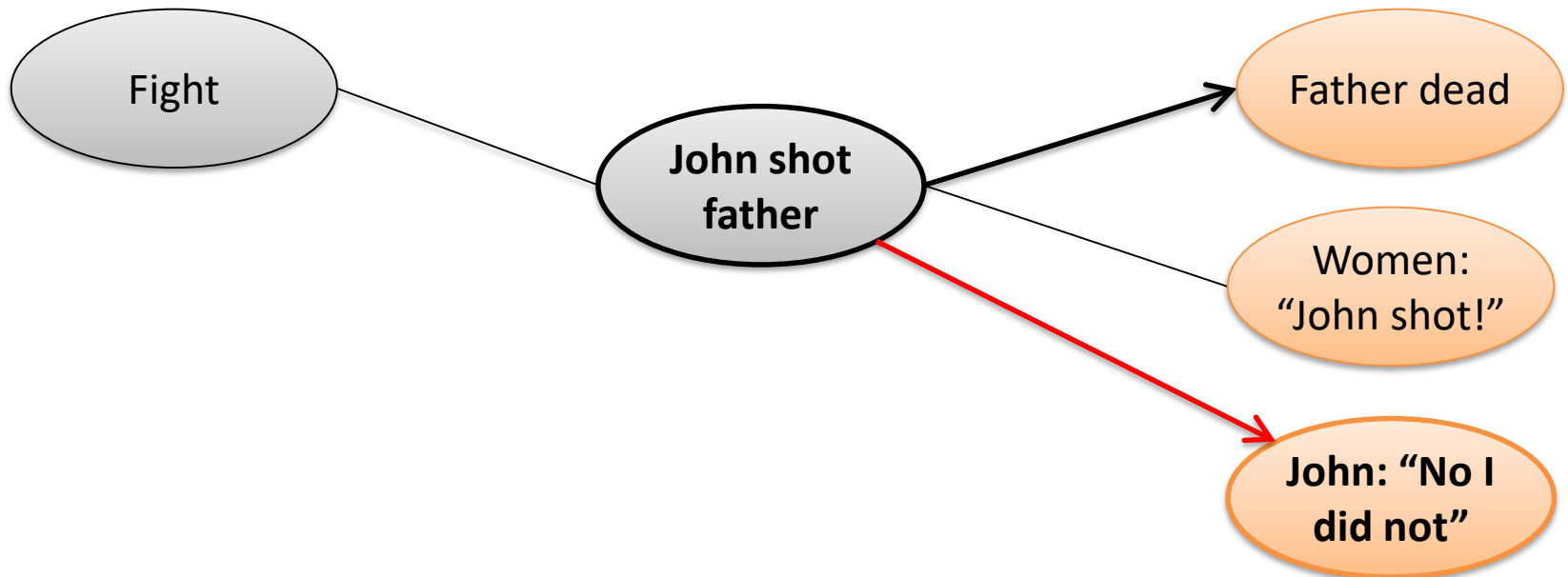
- $\Pr(J\_shot \mid f\_dead, women) + \Pr(\neg J\_shot \mid f\_dead, women) = 1$
- $\Pr(J\_shot \mid f\_dead, \neg women) + \Pr(\neg J\_shot \mid f\_dead, \neg women) = 1$
- $\Pr(J\_shot \mid \neg f\_dead, women) + \Pr(\neg J\_shot \mid \neg f\_dead, women) = 1$
- $\Pr(J\_shot \mid \neg f\_dead, \neg women) + \Pr(\neg J\_shot \mid \neg f\_dead, \neg women) = 1$



# Capturing IBE

## Support vs attack

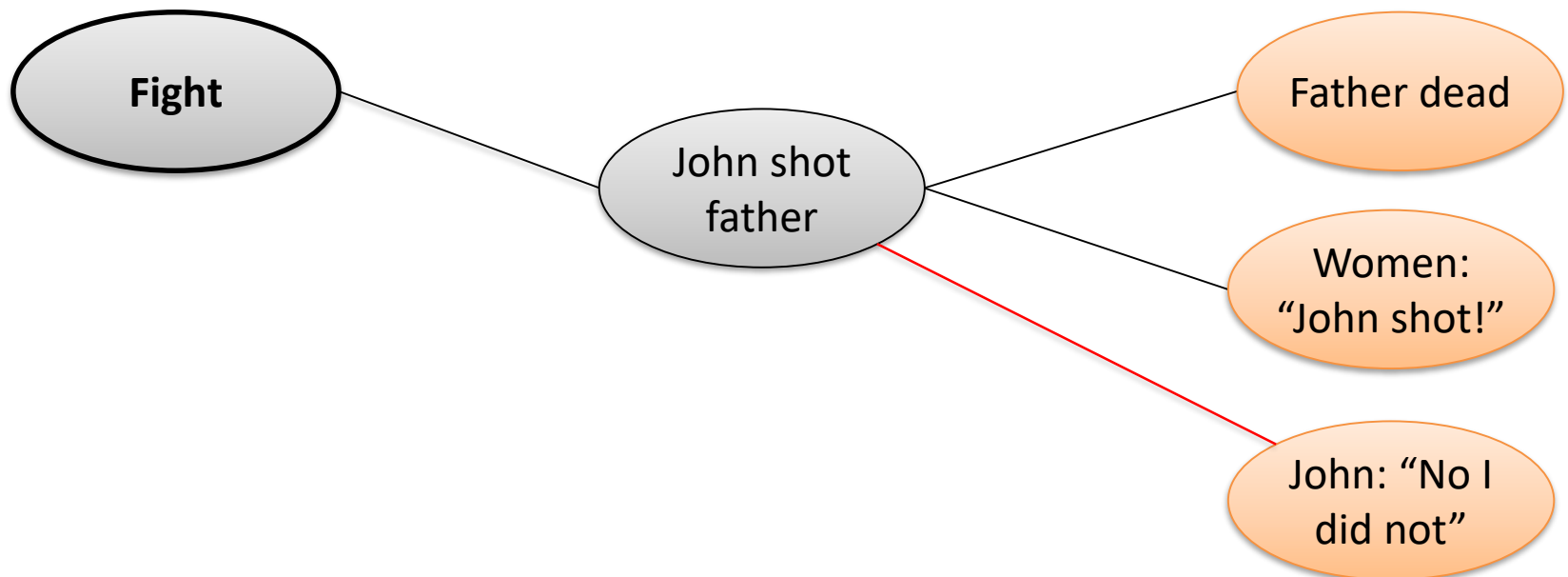
- Supporting evidence
  - $\Pr(f\_dead \mid J\_shot) > \Pr(f\_dead \mid \neg J\_shot)$
- Attacking evidence
  - $\Pr(J\_denial \mid \neg J\_shot) > \Pr(J\_denial \mid J\_shot)$



# Capturing IBE

## Adding probabilities

- Prior probabilities
  - $\Pr(\text{Fight}) + \Pr(\neg\text{Fight}) = 1$   
*The prior probability that a fight breaks out*



# Strength of explanations

- Stories need to be compared
  - How well do they conform to the evidence?
  - How coherent are they of themselves?
- A good/strong story is complete, plausible and conforms to much of the important evidence

# Strength of explanations

- **Evidential Coverage**
  - Evidential Support: how much of the evidence supports the story (is explained by it)?
  - Evidential Attack: how much of the evidence attacks the story (is contradicted by it)?
- **Completeness**
  - Does the story mention all the relevant events we expect to see?
- **Plausibility**
  - Are the story and its elements plausible (irrespective of the evidence)?
- **Consistency**
  - Is the story consistent?



# Strength of explanations

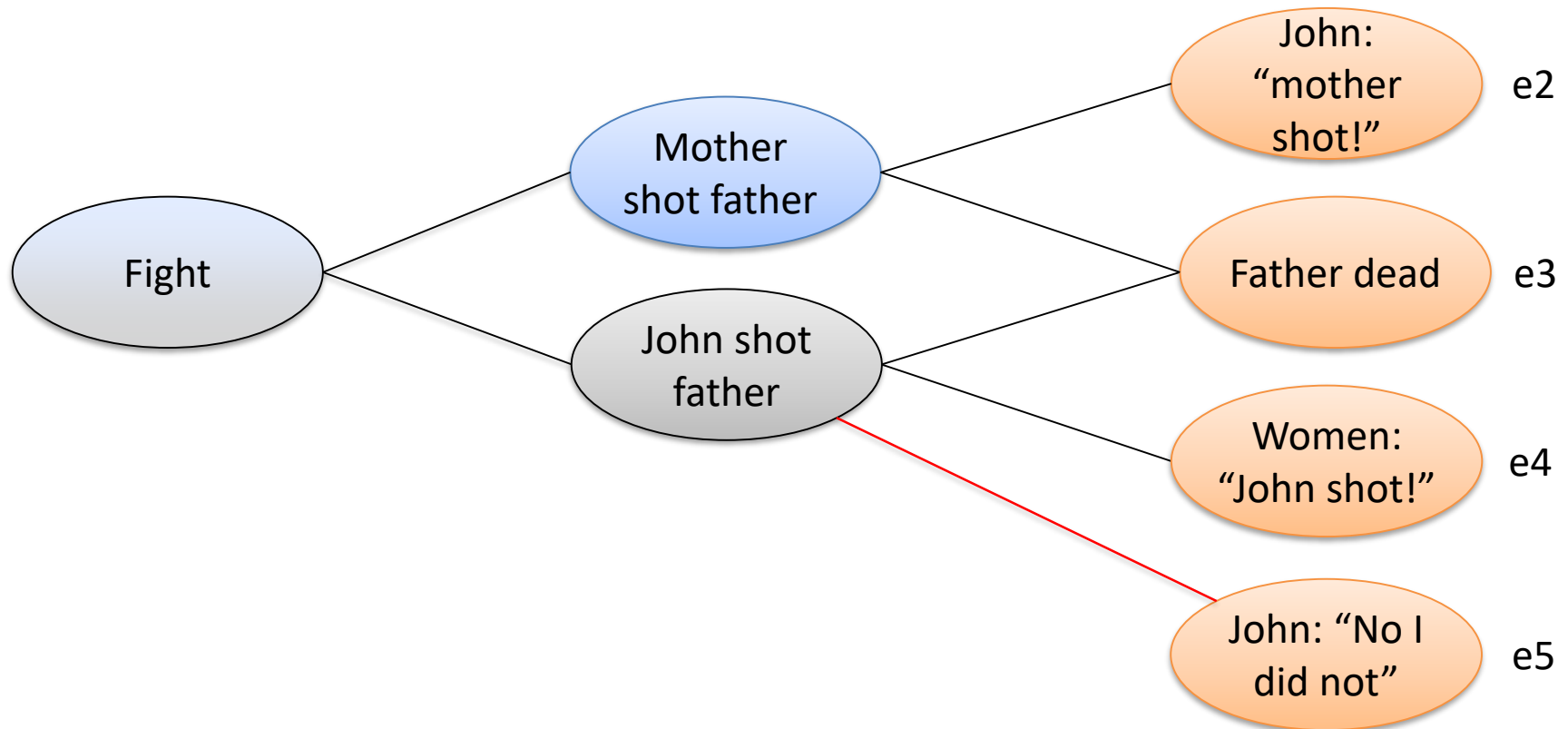
- Evidential Coverage
  - Evidential support
  - Evidential attack
- Completeness
- Plausibility
- Consistency
  
- Given these elements of story strength, we can
  - Reason about them (*Argumentation*)
  - Measure them (*Probabilities*)

# Strength of explanations

## Evidence

- Reasoning with evidential support and attack
- Check which evidence directly supports or attacks a story
  - Support: the evidence supporting a story
  - Attack: the evidence attacking a story
- What are the differences with other (competing) stories?
  - Which evidence does my story not (yet) explain?
  - Which attacks do I need to respond to?

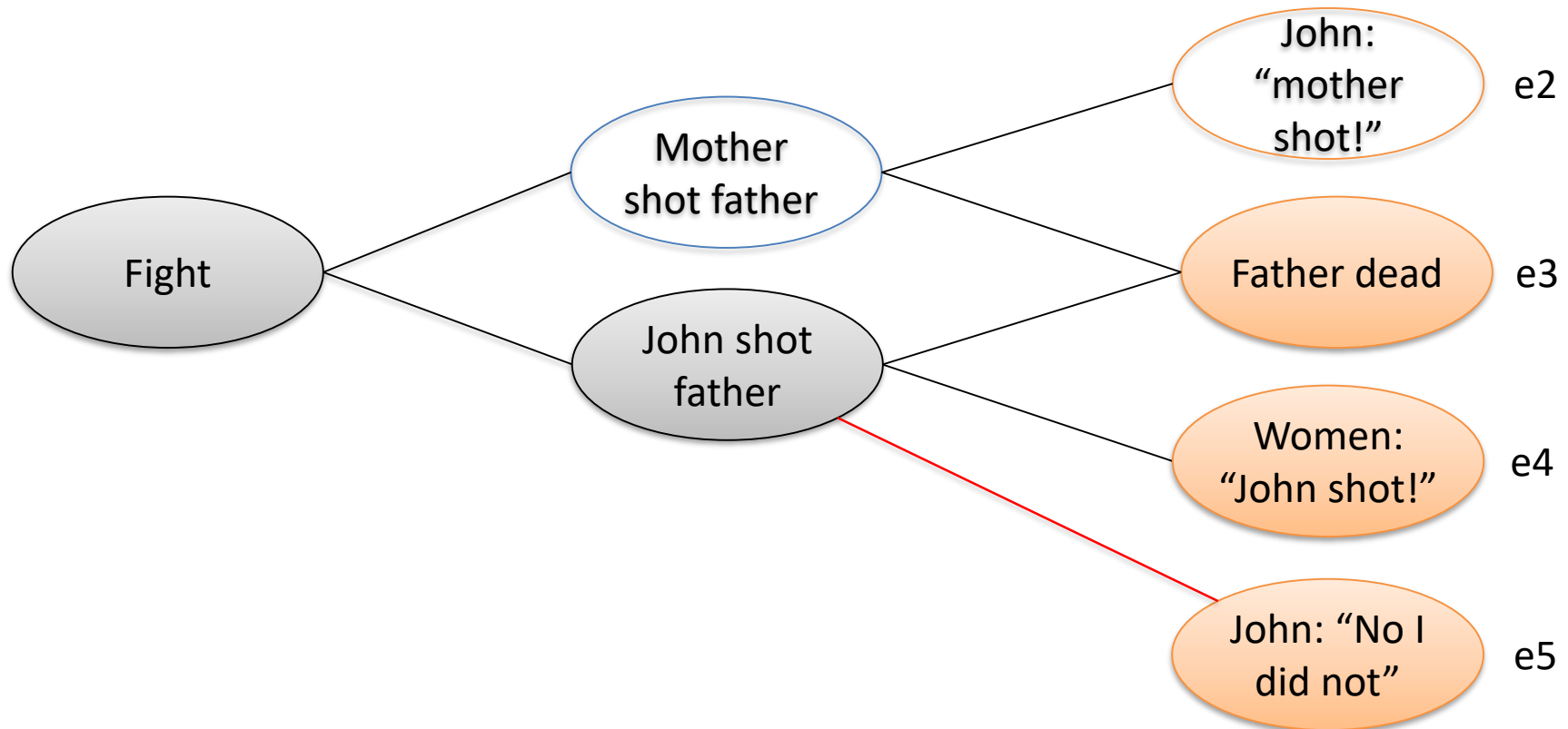
# Support and Attack Reasoning



# Support and Attack

## Qualitative interpretations

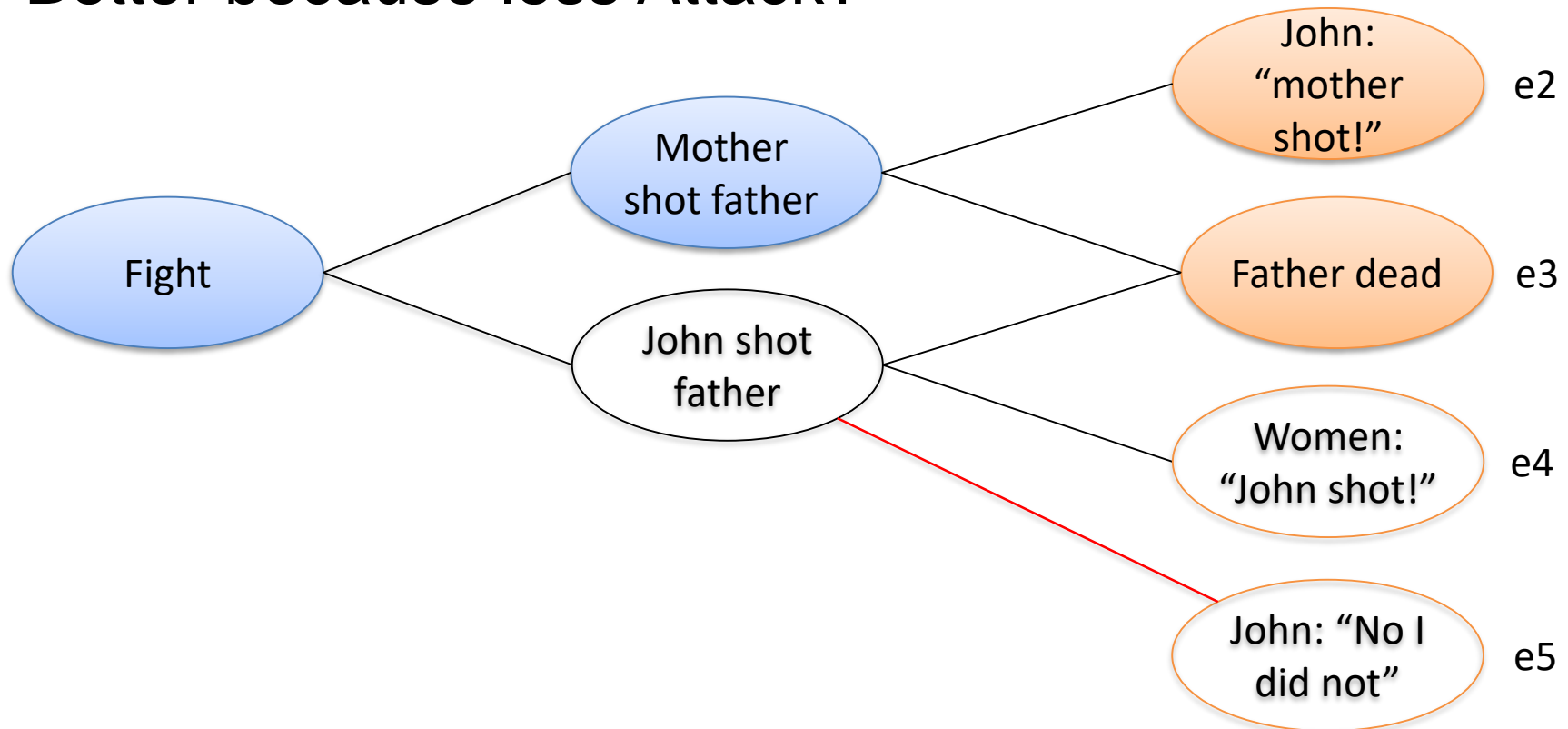
- Support: {e3,e4}
- Attack: {e5}



# Support and Attack

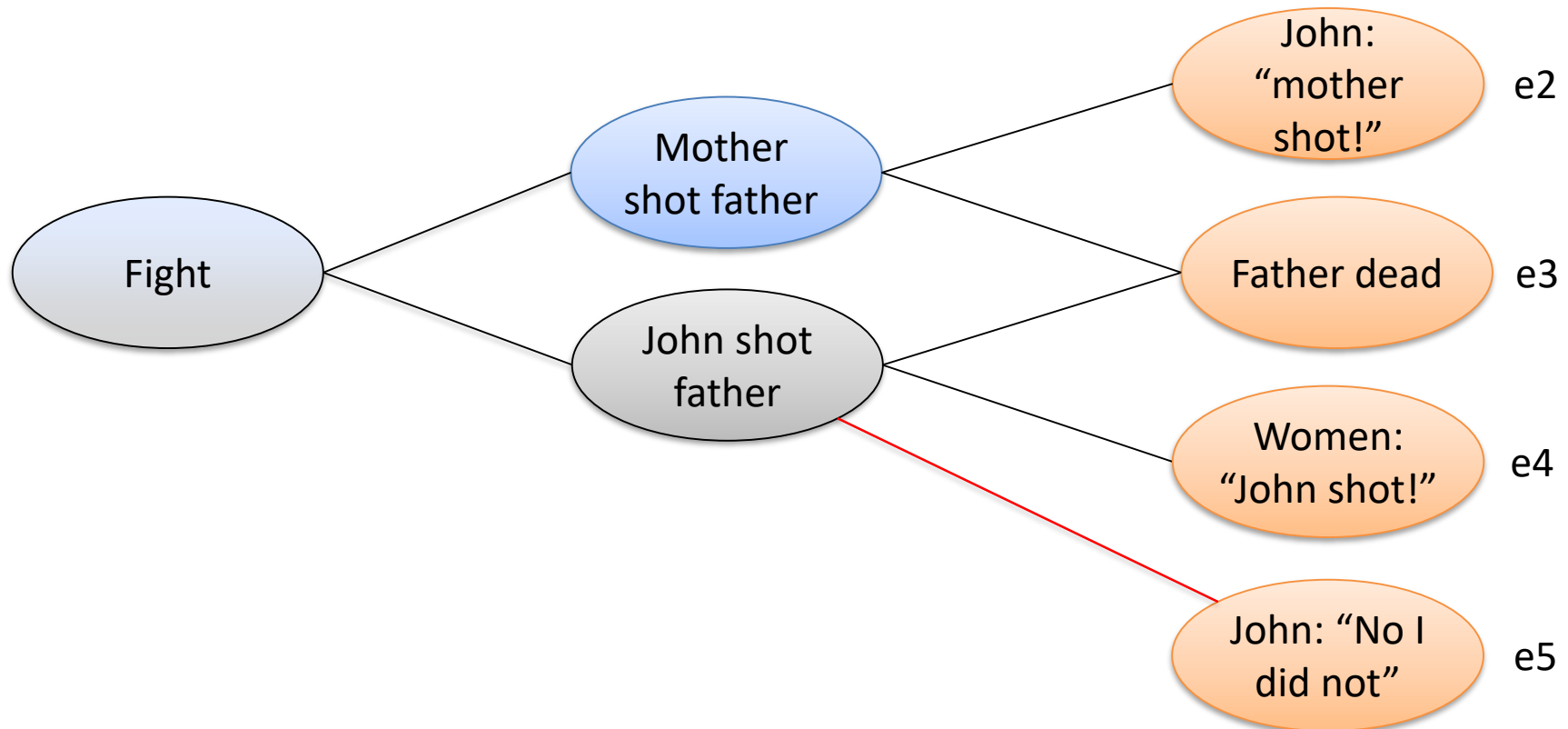
## Qualitative interpretations

- Support = {e2,e3}
- Attack = {}
- Better because less Attack?



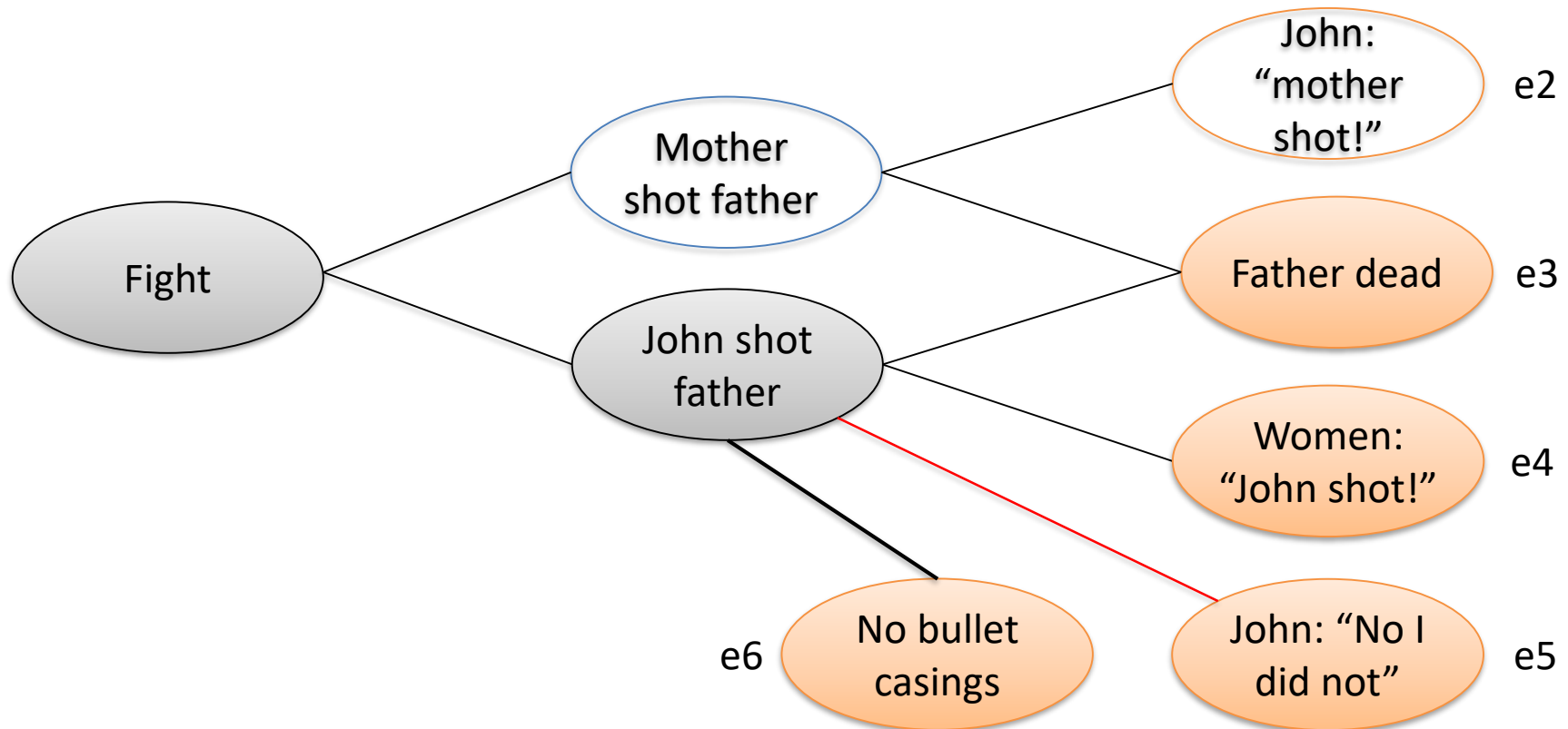
# Support and Attack Reasoning

- (J) has a support of two pieces of evidence, same as (M), and is attacked by 1 piece of evidence while (M) is not attacked.



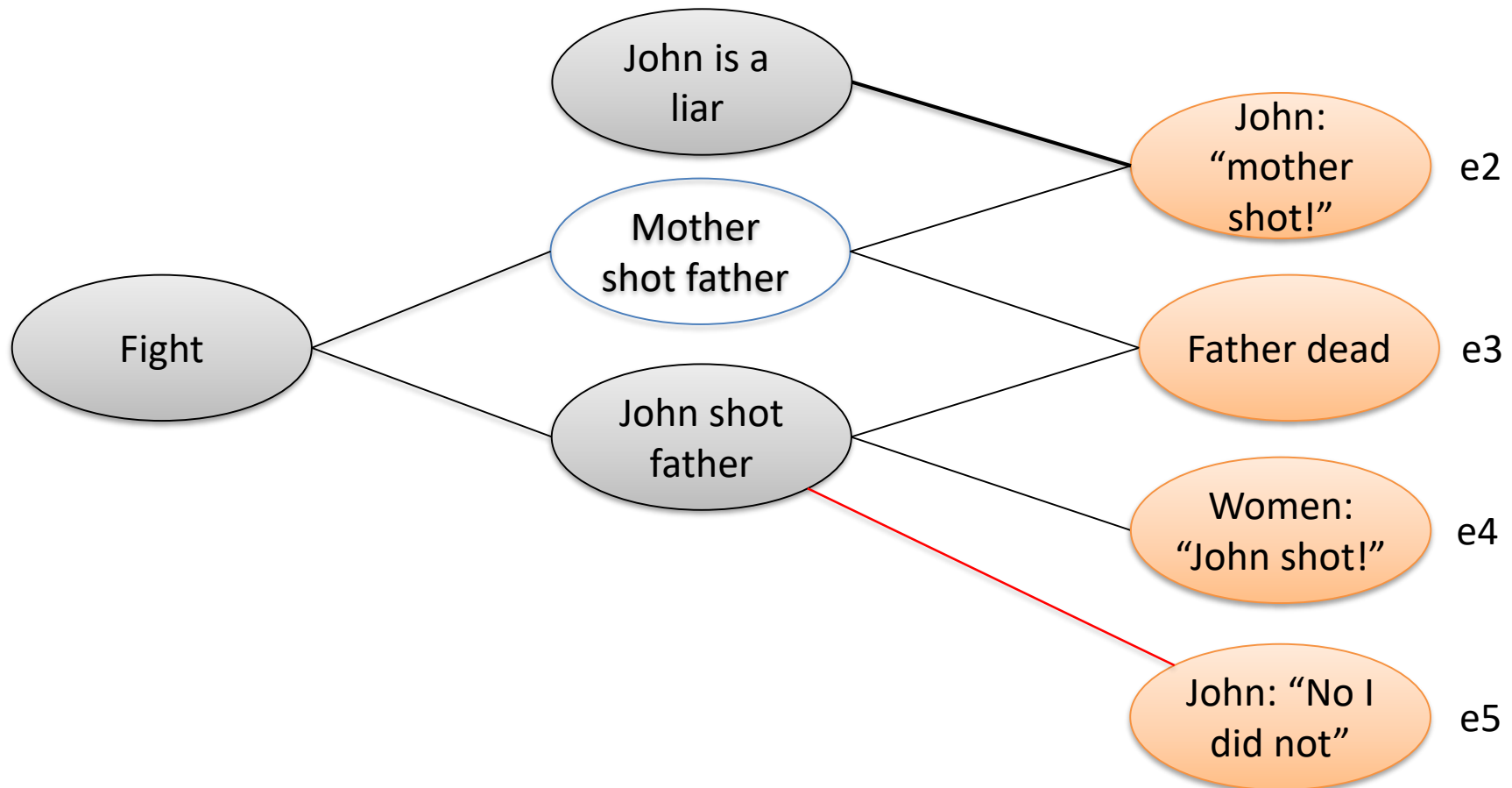
# Support and Attack Reasoning

- Find extra supporting evidence for J, increasing Support



# Support and Attack Reasoning

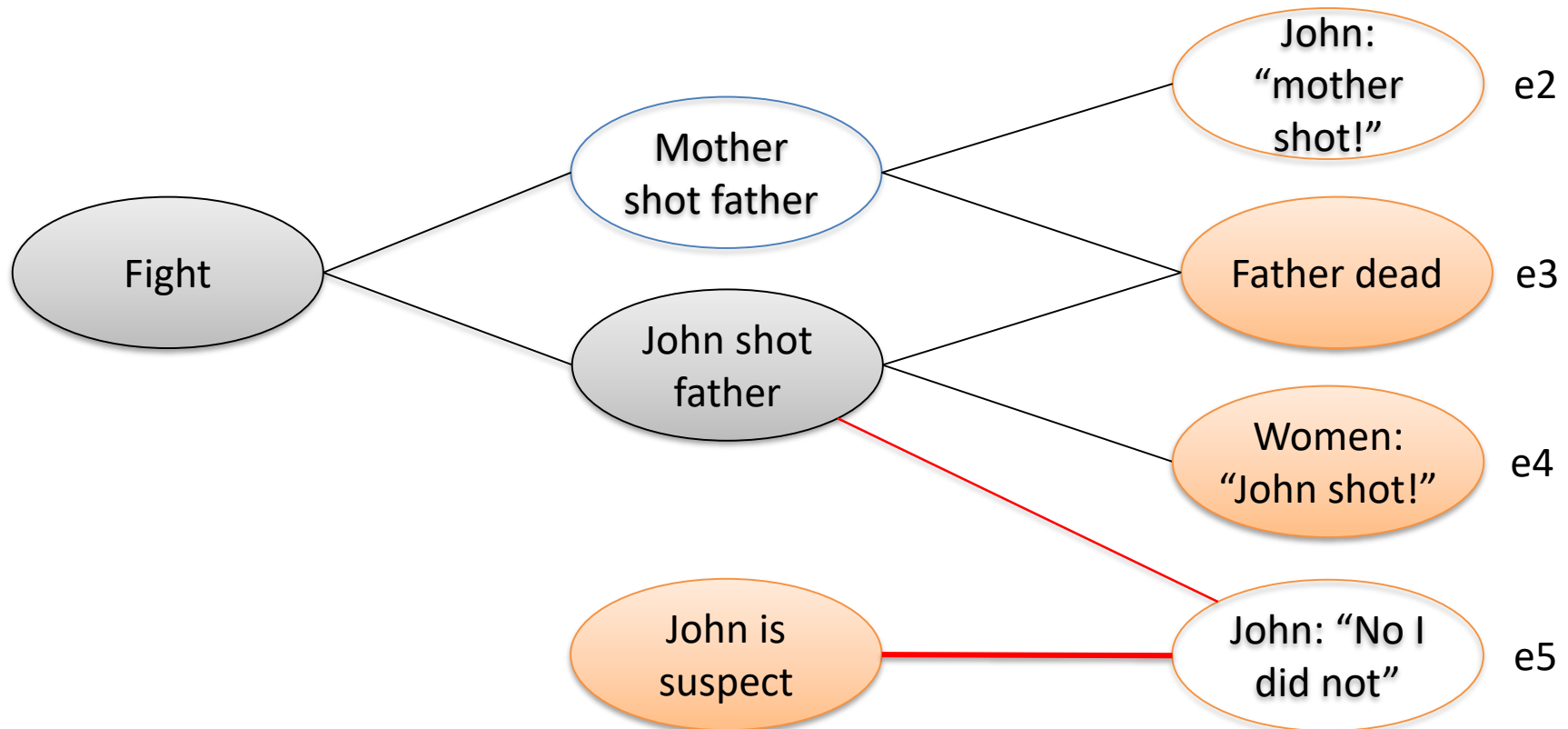
- Explain the evidence that the other story explains by expanding your story (increasing support)





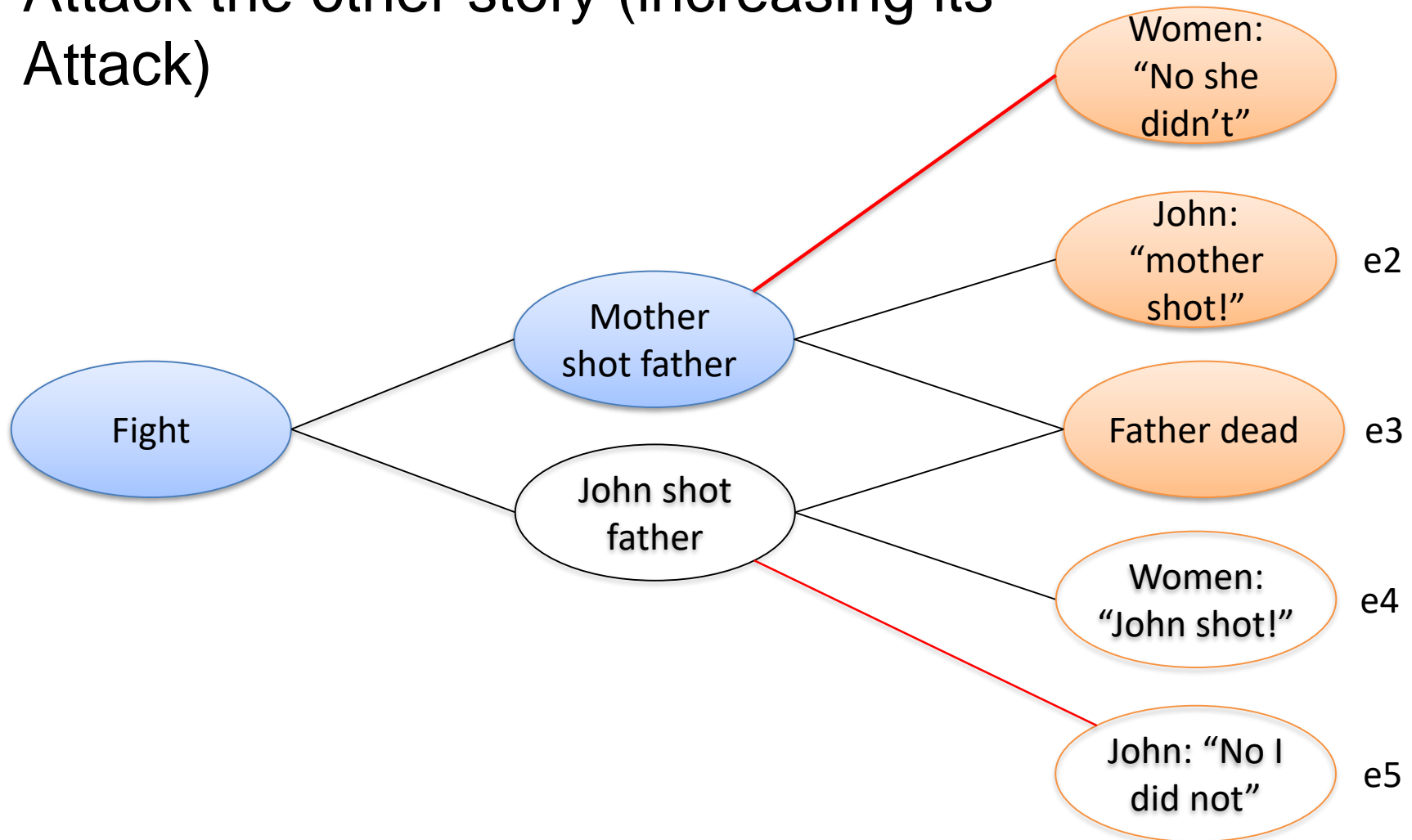
# Support and Attack Reasoning

- Attack the attacking evidence (decreasing Attack)



# Support and Attack Reasoning

- Attack the other story (increasing its Attack)



# Evidence Reasoning

- Qualitative reasoning about the strength of stories given the evidence
- Improve your story by
  - Finding new supporting evidence
  - Expanding your story to explain more existing evidence
  - Attacking the other story
  - Attacking your attackers
- No final “decision”, but also no numbers needed

# Strength of explanations

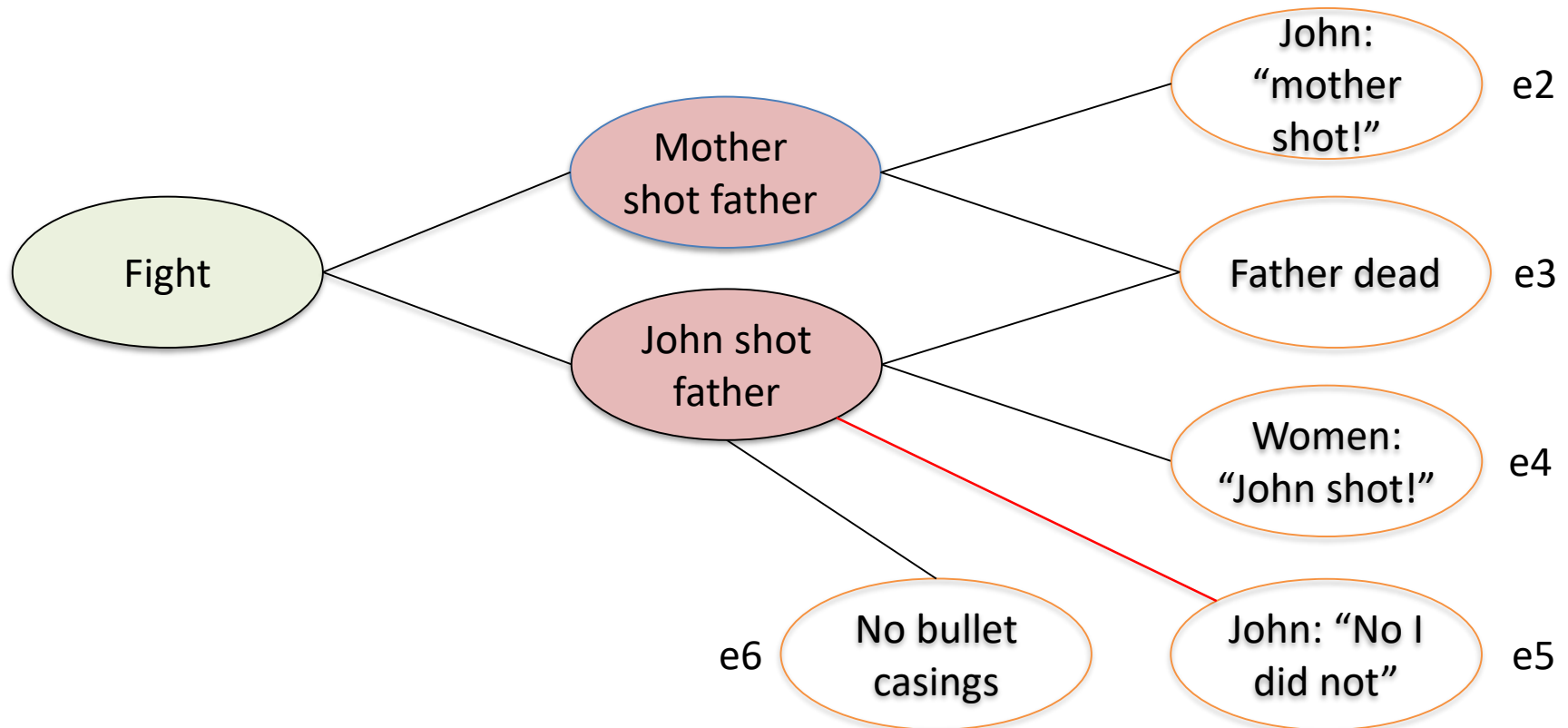
## Evidence

- Measuring support and attack
- Supporting evidence
  - $\Pr(\text{Story} \mid \text{Evidence}) > \Pr(\text{Story})$
- Attacking evidence
  - $\Pr(\text{Story} \mid \text{Evidence}) < \Pr(\text{Story})$
- “Evidence” can be 1 piece, but also a set

# Support and Attack

## Measuring

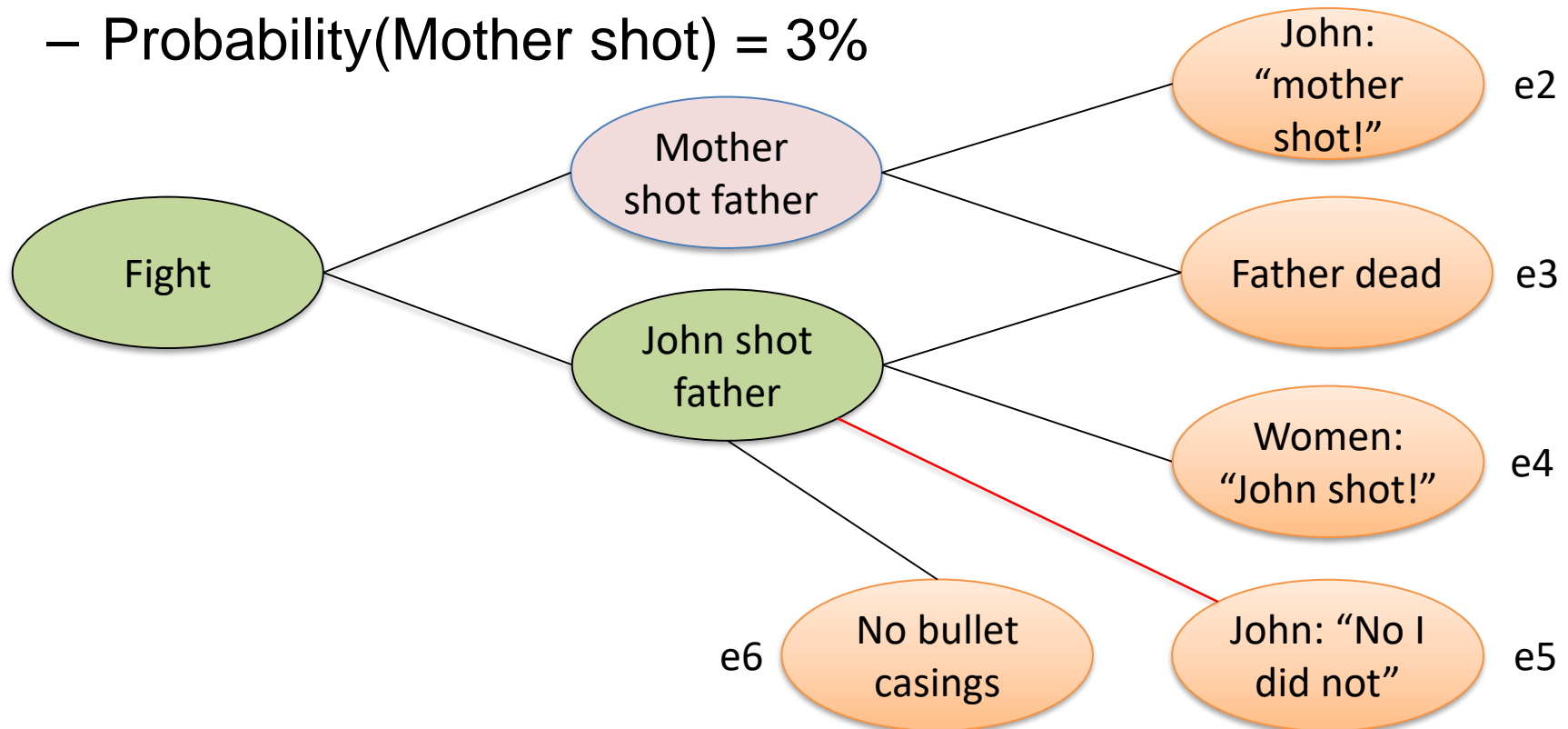
- Prior probabilities



# Support and Attack

## Measuring

- Compare the posterior probabilities with the priors for all stories
  - Probability(John Shot) = 95%
  - Probability(Mother shot) = 3%



# Comparing Support and Attack

## Measuring

- Total evidential support/attack
  - $\text{SuppAtt}(M) = \Pr(M \mid e_2, \dots, e_6) / \Pr(M)$
  - $\text{SuppAtt}(J) = \Pr(J \mid e_2, \dots, e_6) / \Pr(J)$
- $\text{SuppAtt}(M) < \text{SuppAtt}(J)$ 
  - J is more strongly supported (or less strongly attacked) by the evidence than M
- Measuring a story's conformance to the evidence
  - Aggregation, strong vs weak evidence, total influence of evidence on story
- However: all numbers have to be filled in

# Strength of explanations

## Completeness & plausibility

- A story is *coherent* if it conforms to our world knowledge
- World knowledge can be encoded as rules/generalizations
  - If you shoot someone they might die
- World knowledge can be encoded as story schemes
  - person  $x$  has a motive  $m$  to kill person  $y$
  - person  $x$  kills person  $y$  (at time  $t$ ) (at place  $p$ ) (with weapon  $w$ )
  - person  $y$  is dead



# Strength of explanations

## Completeness

- **Completeness**
  - Does the story mention all the relevant events we expect to see?
- A complete story mentions all parts of a script, and nothing more

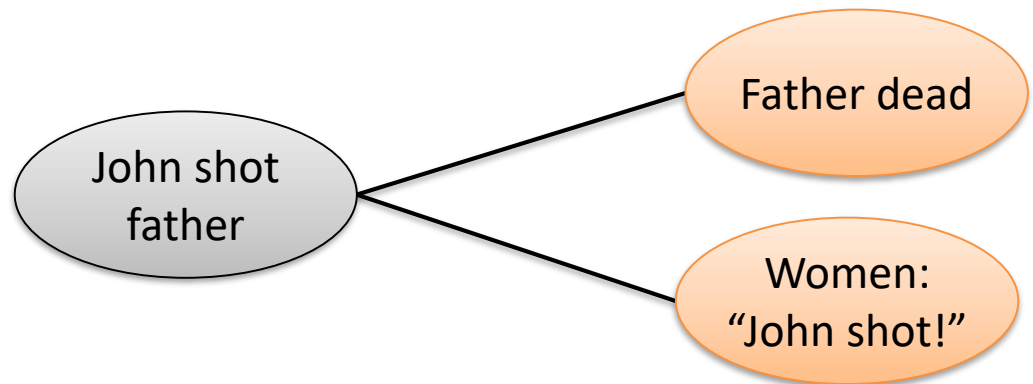
# Completeness

- Missing elements

Motives  
Enabling states

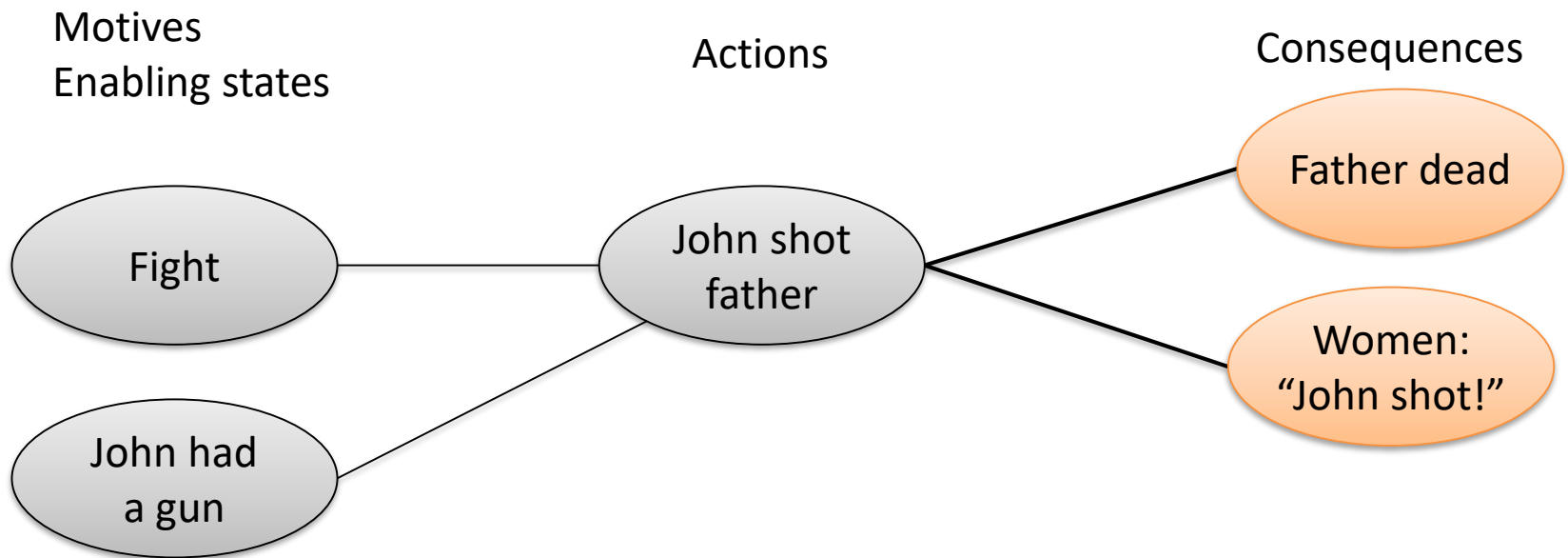
Actions

Consequences



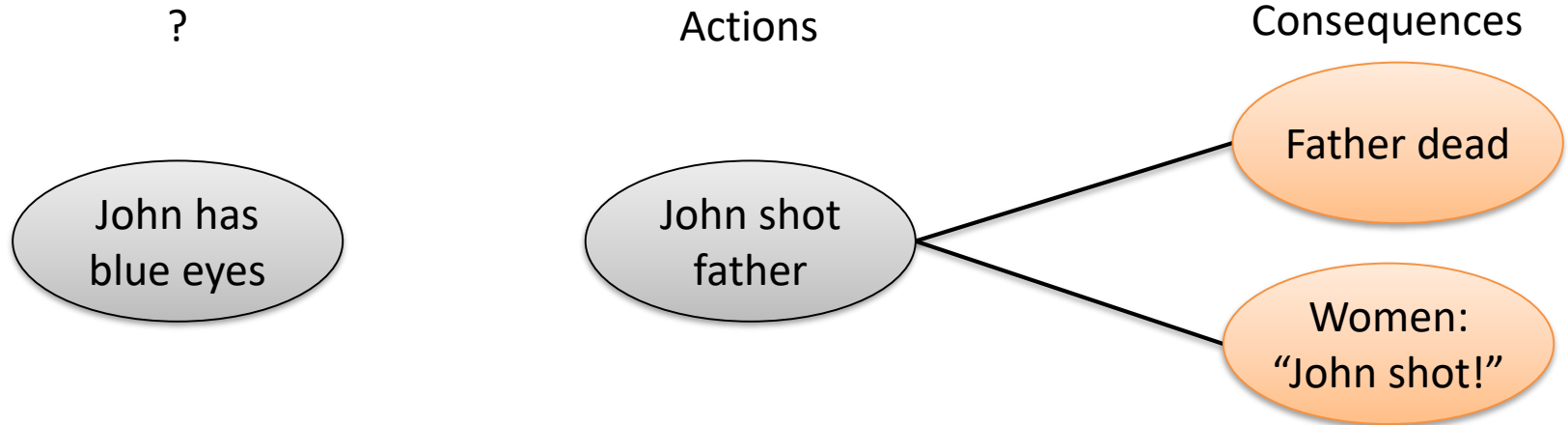
# Completeness

- Add missing elements



# Completeness

- Superfluous elements can be deleted

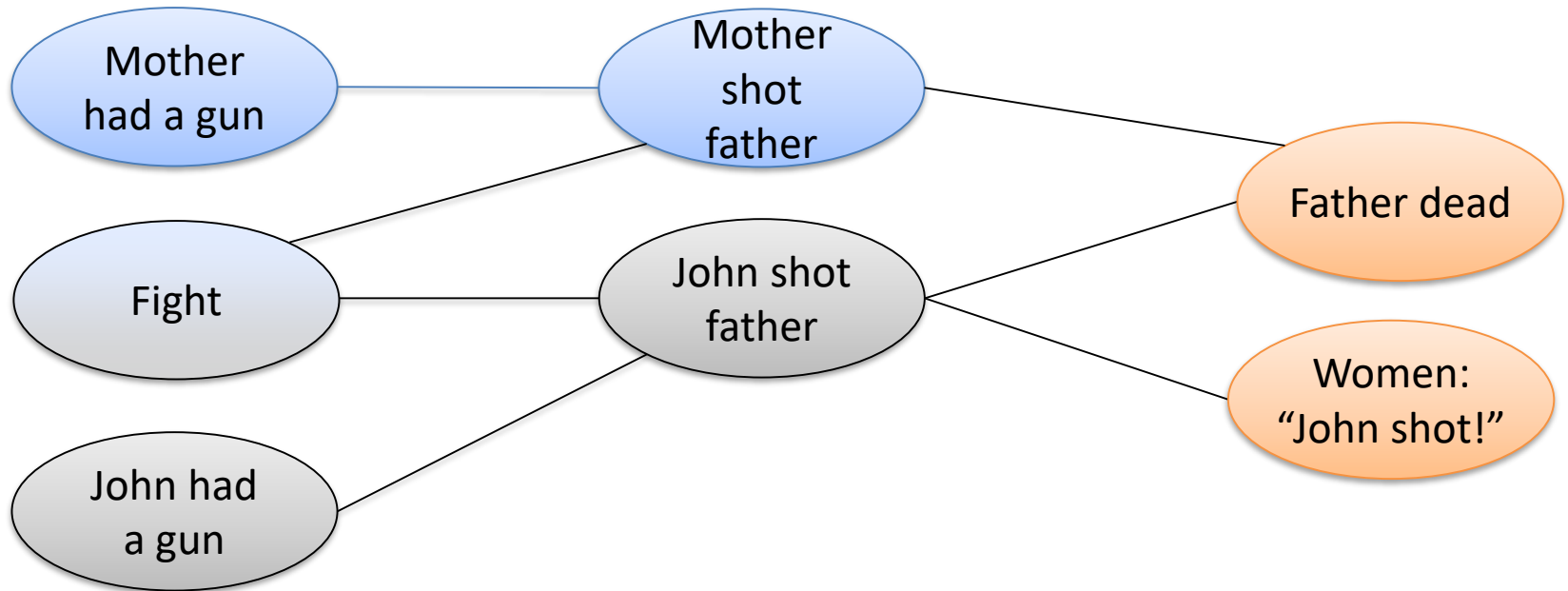


# Plausibility

- The inherent plausibility of events and links between events
  - Mothers never carry guns
  - Criminals like John always carry guns
  - Shooting someone causes them to die
  - It is implausible that a gun going off in a scuffle would have killed father
  - Suspects always deny the charges against them

# Plausibility Reasoning

- Argue for the plausibility of your own story, and against that of the others



# Plausibility Reasoning

It is general knowledge that mothers never have guns

It seems highly unlikely that a gun going off in a scuffle killed father

Mother had a gun

Mother shot father

Fight

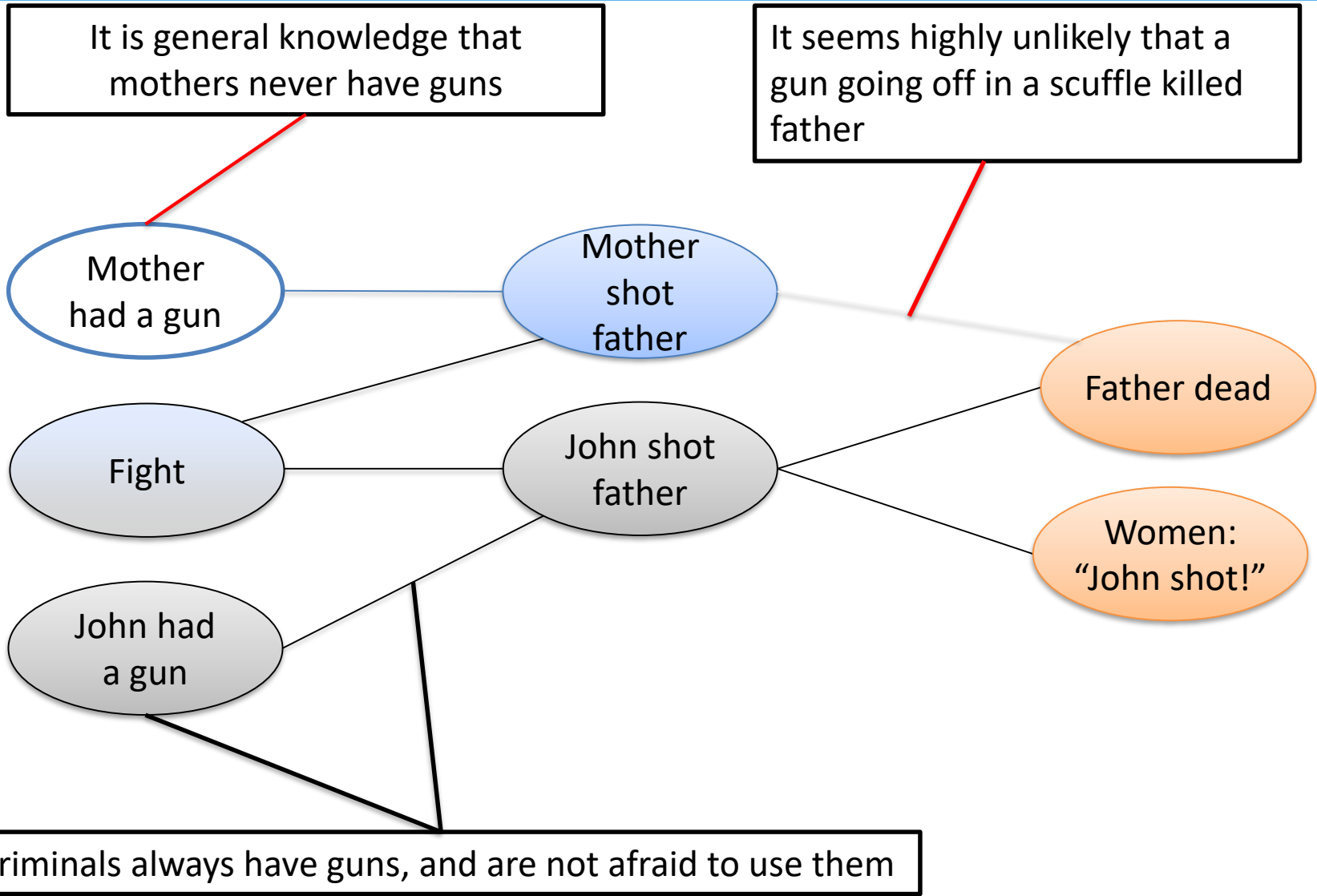
John shot father

John had a gun

Father dead

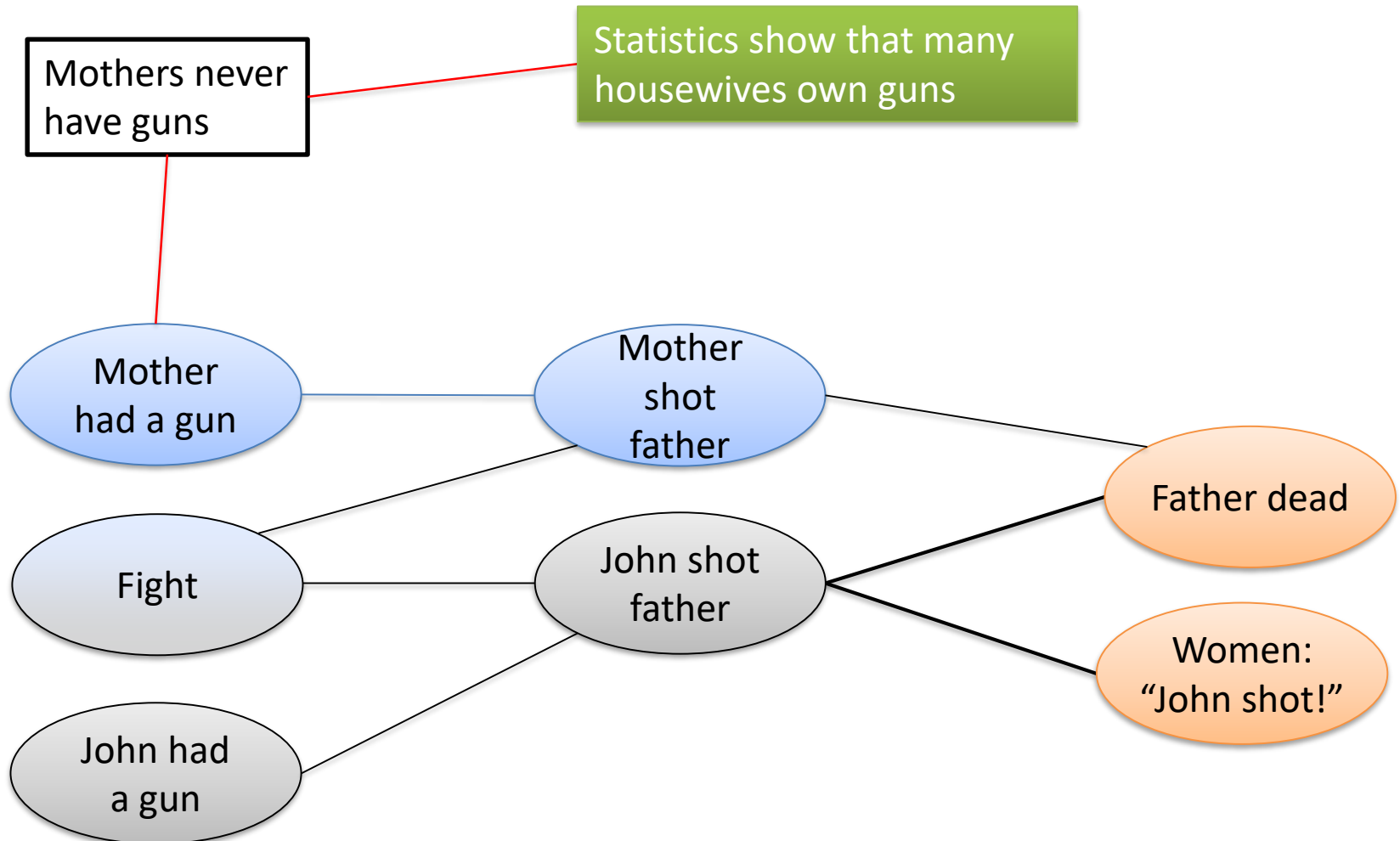
Women: "John shot!"

Criminals always have guns, and are not afraid to use them



# Plausibility Reasoning

- Attacking attackers





# Evidence Reasoning

- Qualitative reasoning about the completeness & plausibility of stories
- Improve your story by
  - Completing it and deleting superfluous elements
  - Arguing that the other story is incomplete
  - Arguing for the plausibility of your story
  - Arguing against the plausibility of the other story
  - Attacking your attackers
- No final “decision”, but also no numbers needed

# Plausibility

## Measuring

- Plausibility can be expressed as probabilities
- Criminals always carry guns
  - $\Pr(\text{Criminal\_John\_has\_gun}) = 1$
- Criminals are not afraid to use guns
  - $\Pr(\text{J\_shot} \mid \text{fight}, \text{J\_has\_gun}) > 0.5$
- Mothers (almost) never carry guns
  - $\Pr(\text{Mother\_has\_gun}) = 0.001$
- It is implausible that a gun going off in a scuffle would have killed father
  - $\Pr(\text{f\_dead} \mid \text{m\_shot}) < 0.1$
- Measuring plausibility is necessary to come to a decision
- Measuring plausibility is dangerous if probabilities left implicit
  - Argue about them!

# Conclusions

- Reasoning based on competing *stories*
- Stories can be *argued* about
  - How well they conform to the evidence
  - How complete & plausible they are
  - How much better than other stories they are
- *Probabilities* can be used to measure how good stories are
  - How inherently plausible the events and links are
  - How (much more or less) likely they are given the evidence

# Conclusions

- Always need world knowledge
  - Possible counterarguments
  - Probabilities
- Qualitative reasoning
  - No complete probability distribution needed
- Quantitative reasoning
  - Close to statistical (machine learning) in AI