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# Advances in writer identification and verification

Lambert Schomaker

icdar-lecty8-ooffice.ppt	algebra	algebra	algebra	algebra
	algebra	algebra	algebra	algebra
	algebra	algebra	algebra	algebra
	algebra	algebra	algebra	algebra
	algebra	algebra	algebra	algebra
	algebra	algebra	algebra	algebra
	algebra	algebra	algebra	algebra
	algebra	algebra	algebra	algebra

L.R.B. Schomaker (2007) Advances in writer identification and verification [Invited lecture],  
*Proc. of 9th Int. Conf. on Document Analysis and Recognition (ICDAR 2007)*, IEEE Computer Society,  
pp. 769-773, vol. II, 23 - 26 September, Curitiba, Brazil.



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# Researchers

- › Marius Bulacu, Axel Brink, Katrin Franke
- › Ralph Niels, Louis Vuurpijl
- › “The Nijmegen Handwriting Group 1984-1993”
- › Netherlands Forensic Institute: Ton Broeders, Wil Fagel, Elisa van den Heuvel
- › Isabelle Guyon, Rejean Plamondon
- › many others



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# Overview

1. handwriting-based biometrics
2. the basis of handwriting individuality
3. slant, curvature
4. allography
5. other features
6. outlook



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# Authentication

- › you are  $x$  because you **possess** a token:  $t = T(x)$
  - › you are  $x$  because you **know** a secret:  $p = P(x)$
  - › you are  $x$  because you **behave** as  $x$ :  $b = B(x)$
- 
- › Uniqueness:  $B(x) \neq B(y)$  for  $x \neq y$
  - › or:  $\forall x B(x) \wedge \neg \exists y \neq x (B(y) = B(x))$
- 
- › Permanence:  $\forall t_1, t_2 \ b_{x,t1} = b_{x,t2}$



# Authentication

- › you are x because you:
    - possess physiological feature, indissolubly connected to individual x:
    - DNA, face, hand, ear, iris, fingerprint
- General Biometrics!



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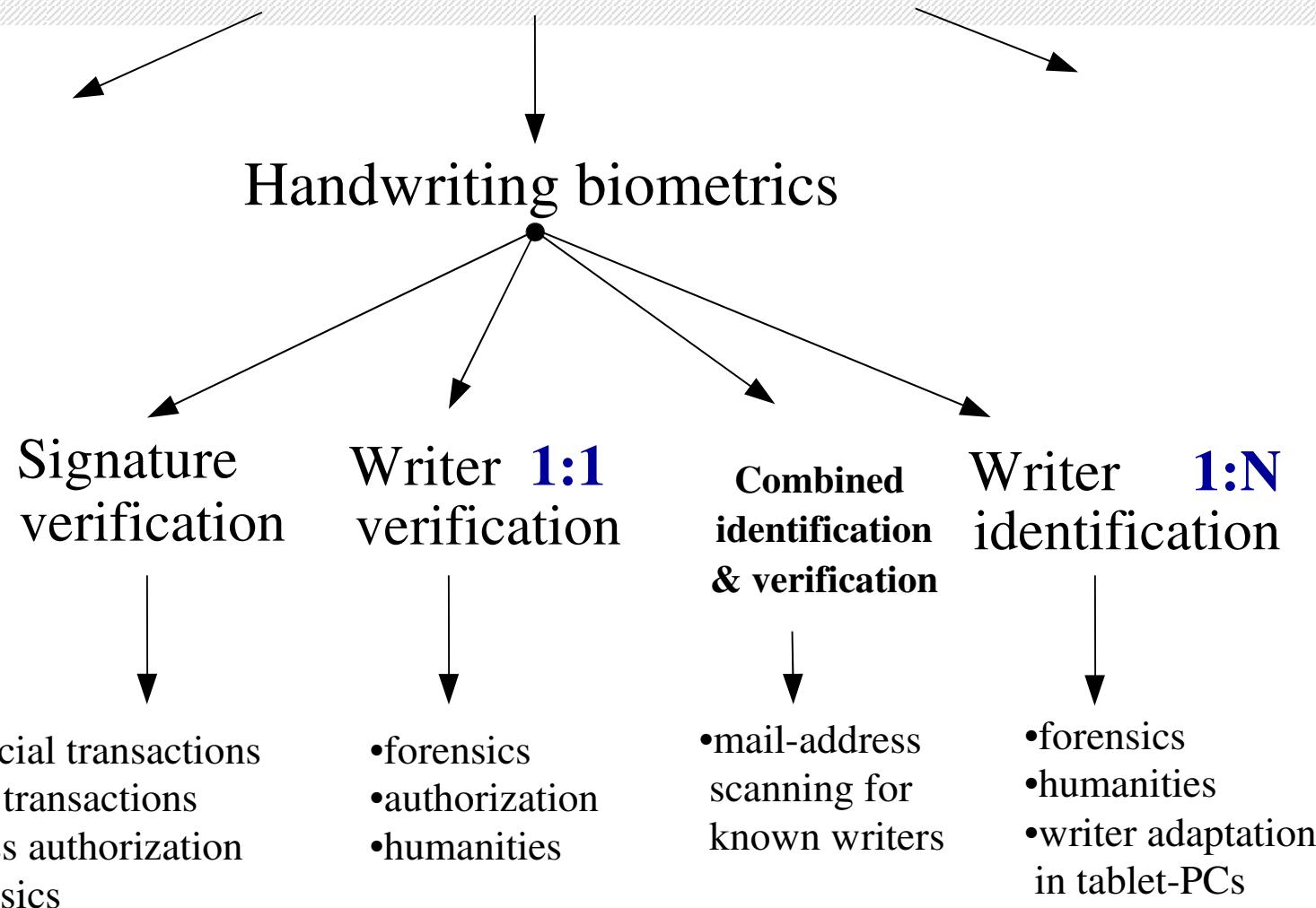
# Behavioral Biometrics

- › you are x because you **behave** as x
  
- › speech
- › gait
- › inter-keystroke delays in typing
- › usage of punctuation in text (,.;;)
- › word-usage histogram
- › ... **handwriting biometrics** ...



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# Behavioral biometrics





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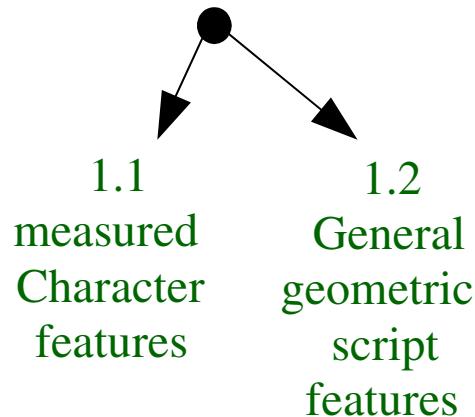
**1. Interactive,  
fully manual  
feature  
measurement**

**2. Automatic**

**3. OCR based**



## 1. Interactive, fully manual



## 2. Automatic

## 3. OCR based

## 1. Interactive, fully manual

### 2. Automatic

### 3. OCR based

“Width”

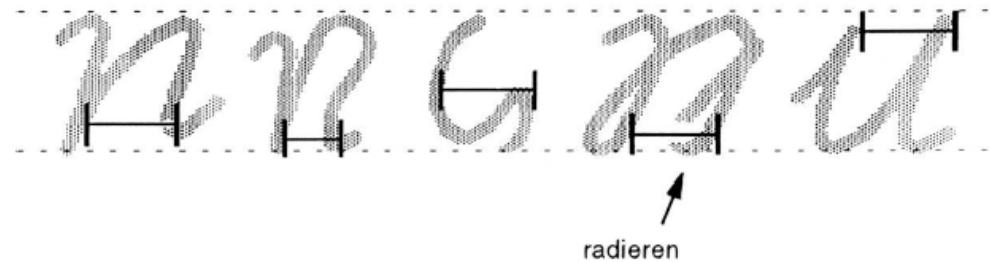


Figure 7.3: Examples of measuring width of handwriting. *Image captured from BKA FISH manual.*

“Corpus”

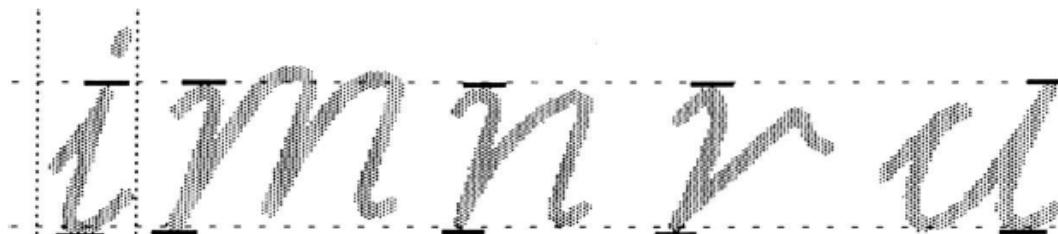


Figure 7.4: Examples of measuring height of handwriting. *Image captured from BKA FISH manual.*

## Manual feature measurements in the BKA/Fish system

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1. Interactive,  
fully manual

2. Automatic

**3. OCR based**

3.1  
computed  
Character  
features



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1. Interactive,  
fully manual

2. Automatic

**3. OCR based**

Query	f	f	f	f	f	f
f	f	f	<b>f</b>	f	f	
f	<b>f</b>	f	f	f	f	

Query	j	j	f	j	j	j
j	j	j	<b>j</b>	j	j	
j	<b>j</b>	j	j	j	j	

Query	m	m	m	m	m	m
m	m	m	m	m	m	
m	<b>m</b>	m	m	m	m	

Query	z	z	z	z	z
z	z	z	<b>z</b>	z	
z	<b>z</b>	z	z	z	

[Niels, Vuurpijl & Schomaker, 2006]

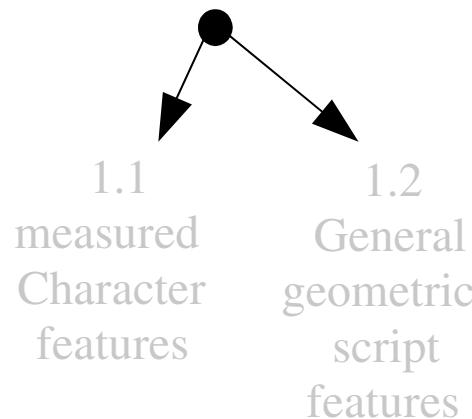
Also cf. Fox system  
(Srihari et al. 2006)

**“OCR”-based, allographic, semi-automatic**

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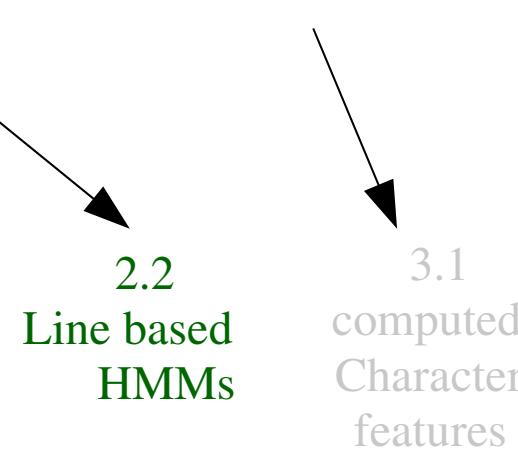
1. Interactive,  
fully manual



## 2. Automatic

2.1  
**Region of  
Interest  
(ROI) based**

3. OCR based





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1. Interactive,  
fully manual

2. Automatic,

3. OCR based

## ROI based

proefnr: geb.dat: 2011 77 man links  
(in te vullen door NICI) huisnr: 60 vrouw rechts x

NICI datacollectie 1999

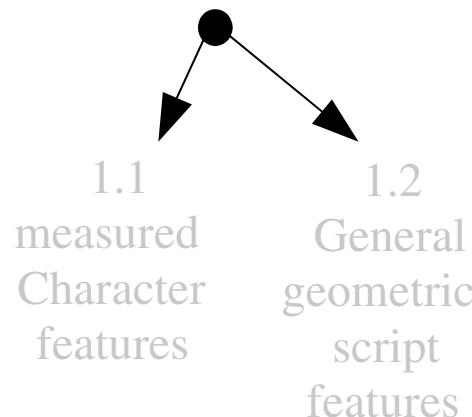
Tekst4: Beschrijving cartoon.

Een mannelijk zit een liegende schotel  
landen. Uit deze schotel stept een  
vreemd uitziend marionnetje, die het  
laaghangende mannelijk hand op zijn neus  
stompt. Verwolgens slapt het marionnetje  
weer in zijn liegende schotel, vliegt weg,  
en laat het mannelijk verbaasd achter.

Who?

Also cf. Bunke et al:  
line HMMs for writers

1. Interactive,  
fully manual



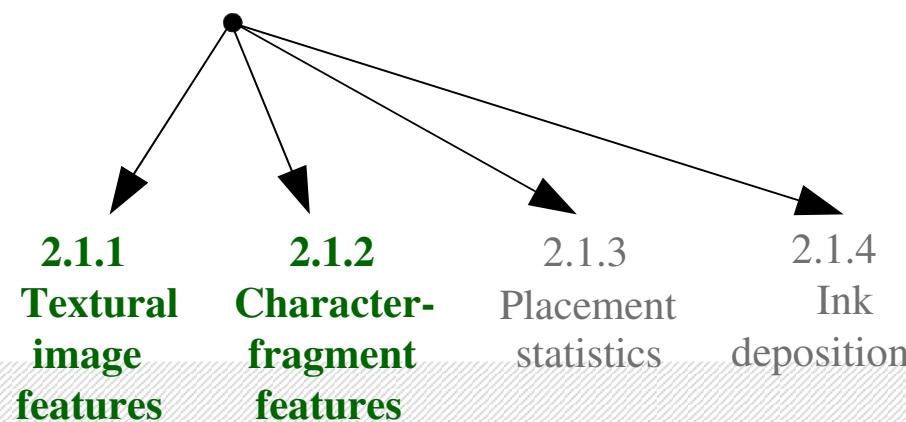
## 2. Automatic

2.1  
**Region of  
Interest  
(ROI) based**

3. OCR based

2.2  
Line based  
HMMs

3.1  
computed  
Character  
features





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# Is there a basis for handwriting individuality in behavioral biometrics?

- › Handwriting of different persons looks different ...
  - › But handwriting is learned - thus can be forged -
  - › Is it stable enough?
- 
- › What are the most reliable features?
  - › How much data are needed in a sample?



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# Factors in individuality

- › between-writer variation
- › within-writer variability
- › nature-nurture (genetics-memetics)
- › Four factors in kinematics & 2D  
(that produce problems in the recognition of HWR)



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alpha  
alpha  
alpha  
alpha

ALPHA  
alpha  
alpha  
alpha

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Neuro-biomechanical variability

worm  
worm  
worm  
worm

~~00000~~  
1 2 3 4      1 2 3      1 2  
E      Δ      C

Allographic variation

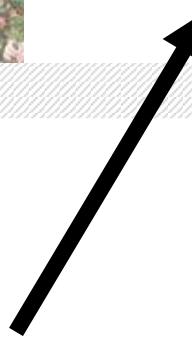
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Sequencing variability

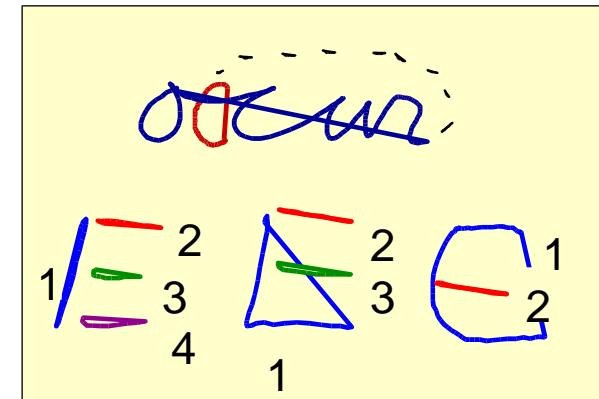
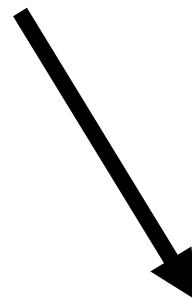
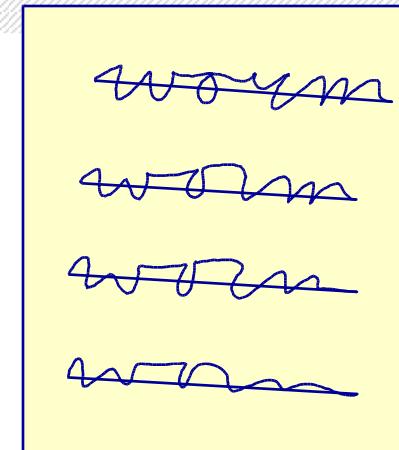


# System State

- fatigue
- psychofarmaca,  
alcohol, coffee
- distractions
  - multitasking
  - acoustic noise
- stress



## / artificial intelligence / HWR group Neuro-biomechanical variability

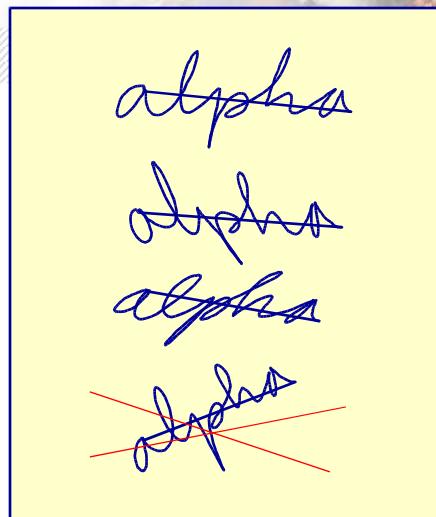


## Sequencing variability

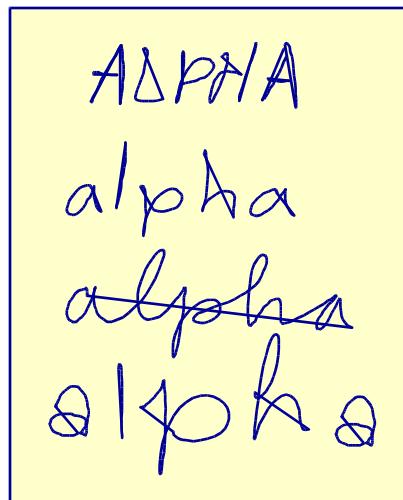


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# System Identity



Part 1) The habitual pen-grip and biomechanical parameters determine:  
size, slant, curvature,  
[pen force]



Part 2) The school system and personal preferences determine allography

## Allographic variation

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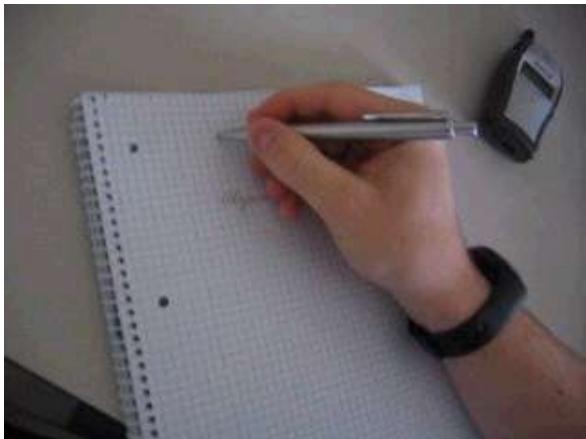
## Slant and curvature

- › are under voluntary control by the brain
- › but: the learned pen grip provides a habitual frame of reference, limiting the variation in shape for a given writer
- › [videos]

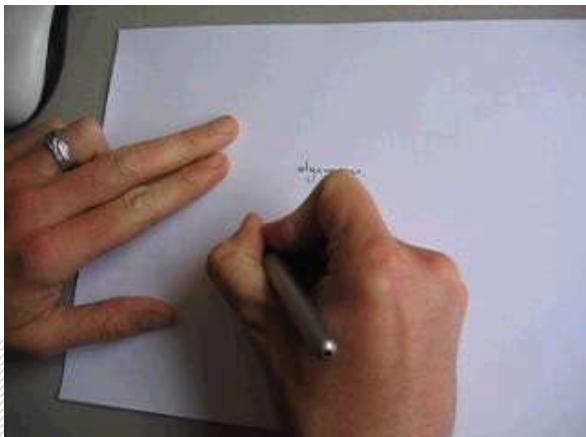


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algemeen

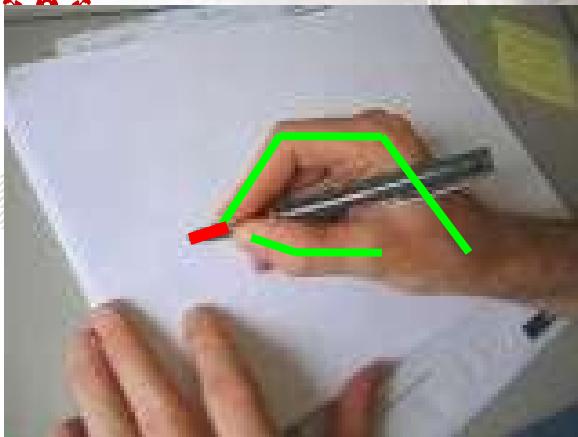


Algemeen



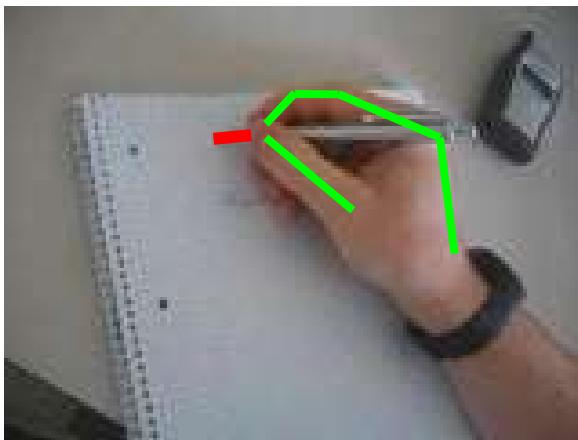
Algemeen

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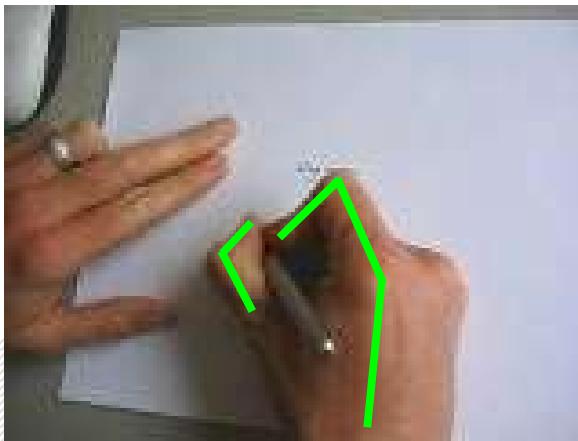


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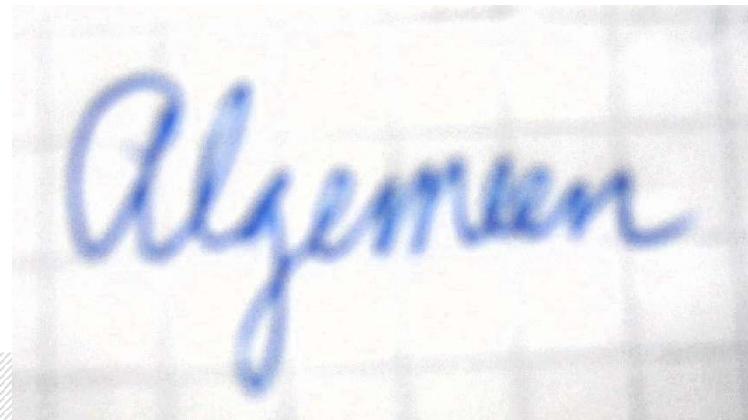
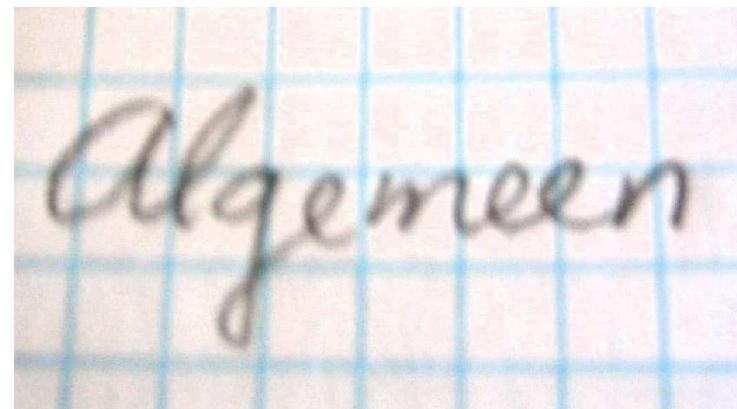
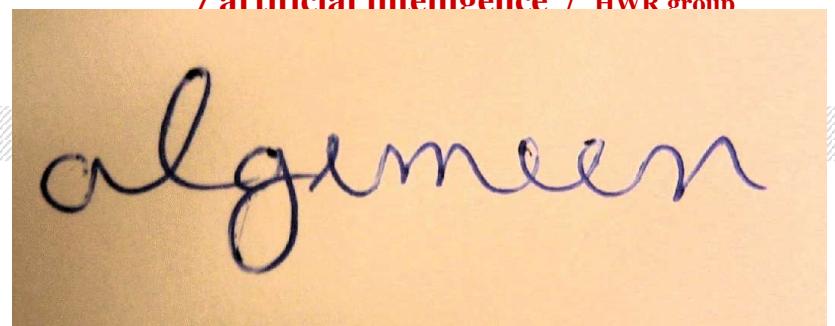
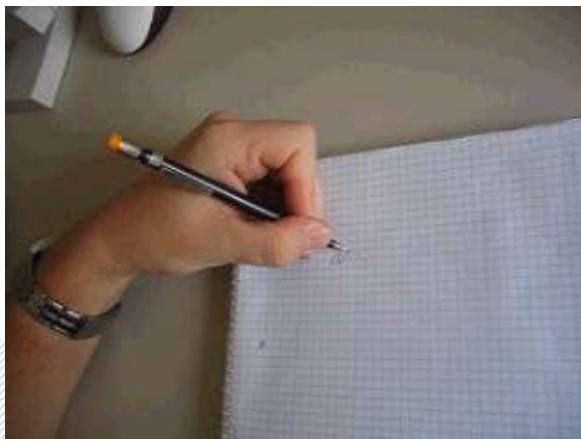
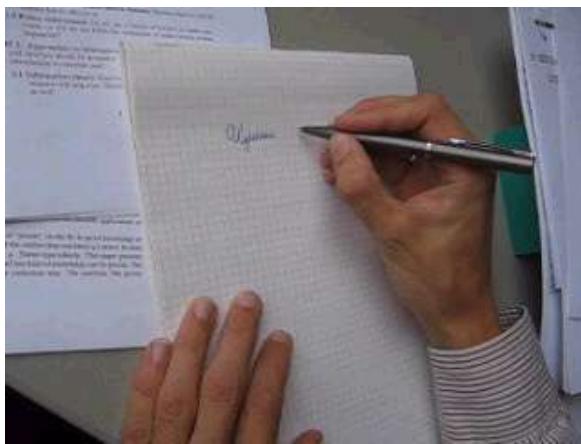
algemeen

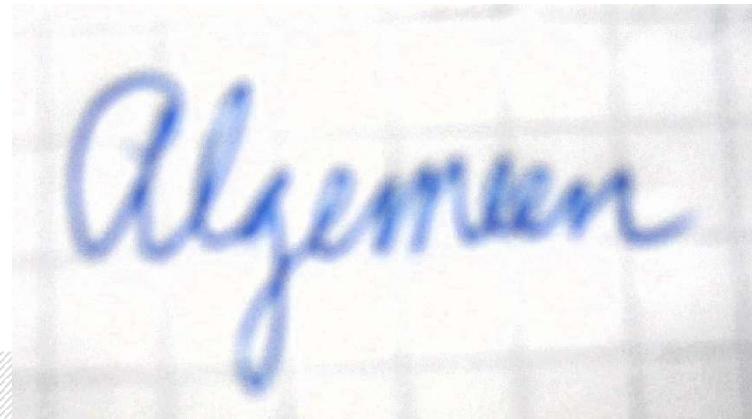
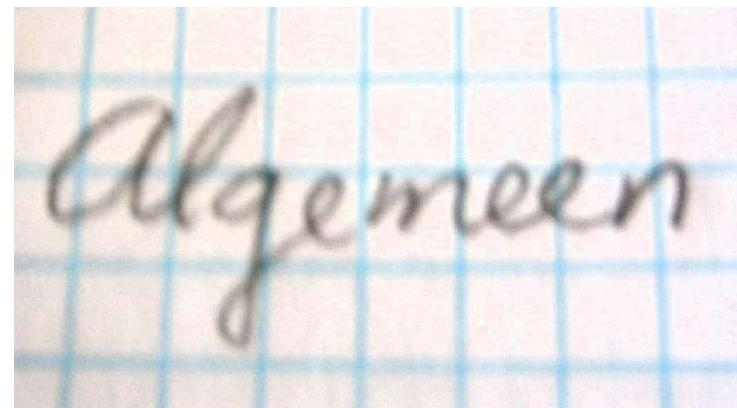
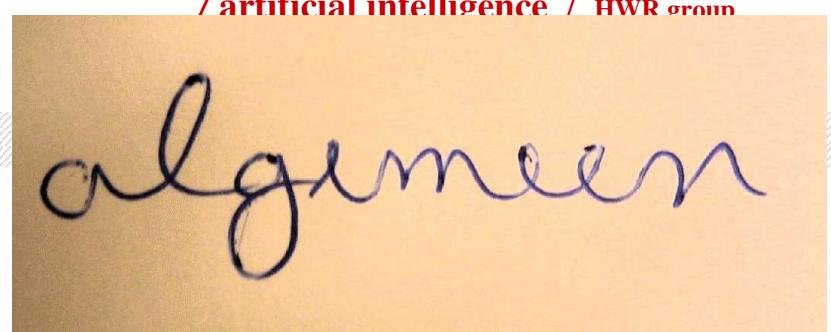
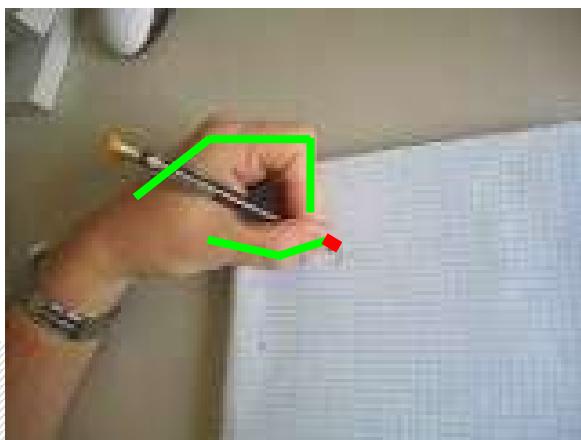
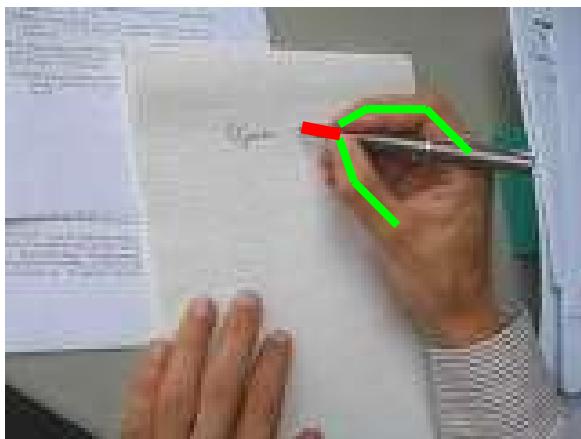


Algemeen



Algemeen







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# Hypothesis

- › if hand biomechanics has a genetic basis,  
i.e., is individual;
- › if handwriting shapes are constrained  
by hand biomechanics;
- › then basic ink-trace characteristics  
such as slant and curvature  
may be good features in handwriting biometrics



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# Hand biomechanics & individuality

- › Park et al (2003) set out to test the urban legend that finger bone lengths obey the Fibonacci sequence

A.E. Park, J.J. Fernandez, K. Schmedders and M.S. Cohen (2003)  
The Fibonacci Sequence: Relationship to the Human Hand  
Journal of Hand Surgery, 28, pp. 157-160.

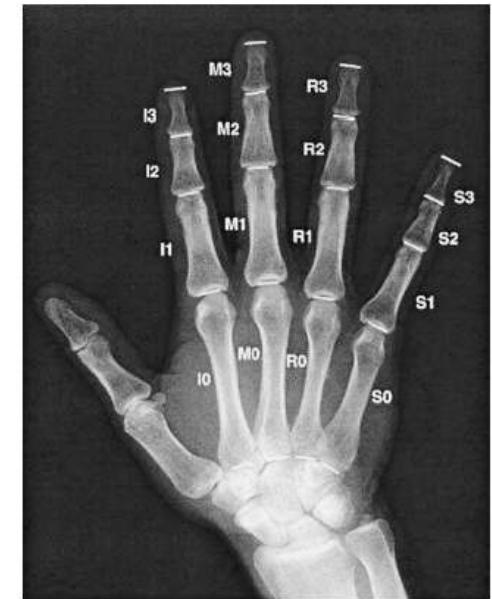


Figure 2. Posteroanterior radiograph of a hand. Bone lengths identified by the name of the field used for statistical analysis. Each data field is composed of a letter to indicate the digit and a number to indicate the bone: I, index finger; M, middle finger; R, ring finger; S, small finger; 0, metacarpal; 1, proximal phalanx; 2, middle phalanx; 3, distal phalanx.

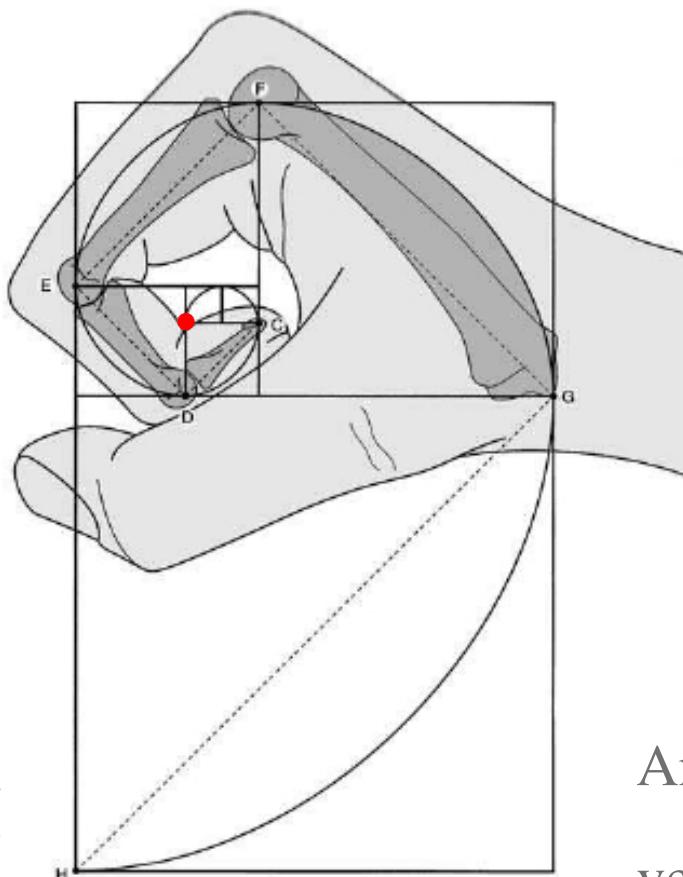


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# Carpal and phalangeal bone-length ratios



Fibonacci: 0,1,1,2,3,5,8,...

$$r = ae^{b\theta}$$

$$\theta = \frac{1}{b} \ln(r/a),$$

$$\arccos \frac{\langle \mathbf{r}(\theta), \mathbf{r}'(\theta) \rangle}{\|\mathbf{r}(\theta)\| \|\mathbf{r}'(\theta)\|} = \arctan \frac{1}{b} = \phi,$$

Angle  $\phi$  between tangent and radial  
vector should be constant (1.618)

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Figure 3. Human hand superimposed on the Fibonacci rect-  
angles and equiangular spiral of Figure 1. This shows the  
proposed relationship of the Fibonacci sequence to the center  
of rotation of the joints of the hand. The connection of points



# Results

- › 100 persons, X-rays of hand
- › **Park et al. (2003)** measured ratios of all consecutive pairs of bones for each finger
- › Fibonacci-compatible value for  $\varphi$  **only** found for **one finger, one pair of bones** (little finger, metacarpal and proximal phalanx lengths)
- › Individuals are characterized by their own typical bone-length ratios!  
→ great for biometrics!



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# Nature/nurture

- › Twin studies (Srihari et al, 2007) show that error rate  $\epsilon$  in writer verification is ordered:

$$\epsilon(\text{identical twins}) >$$

$$\epsilon(\text{fraternal twins}) >$$

$$\epsilon(\text{arbitrary person pairs})$$



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# Part I textural features, rationale

1. brain
2. biomechanics (muscles/bones)
  - minimum jerk principle [Flash & Hogan, 1985]
  - minimum energy principle [Alexander, 1997]
3. preferred habitual pen grip
4. **slant and curvature distributions**



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## Seminal work on slant

- › Dooijes (1984) was the first to use polar histograms of angles in on-line handwriting

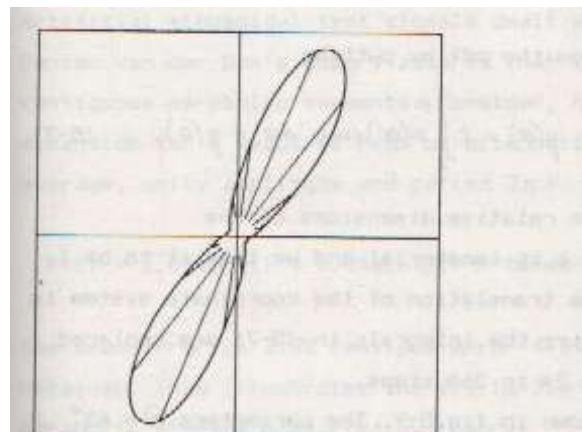


Fig.5-8 (left): distribution of tangent



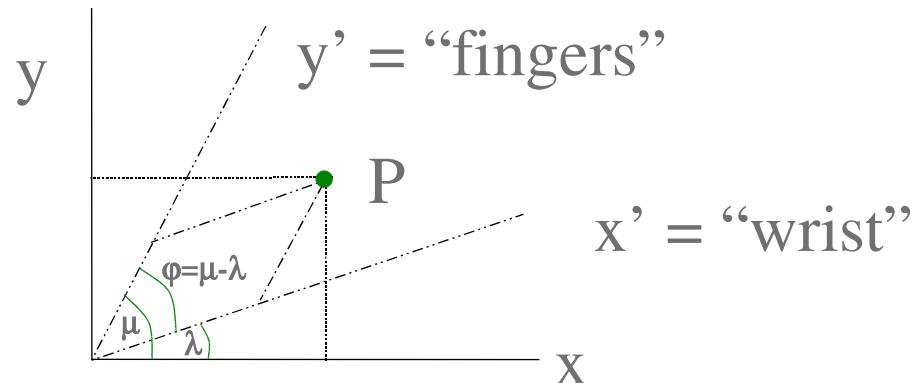
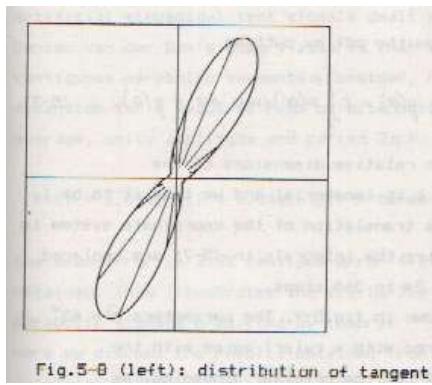
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## Seminal work on slant

- › Dooijes (1984) made an attempt at decomposing the Cartesian recording of a digitizer tablet in to an oblique system of 2 axes, representing the wrist and finger movements:





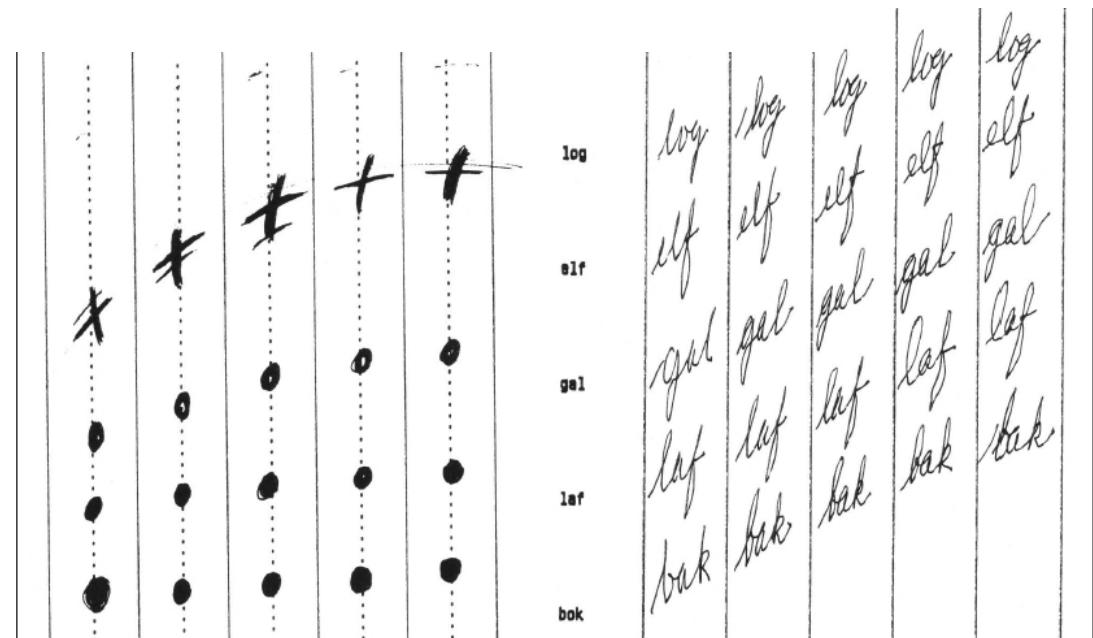
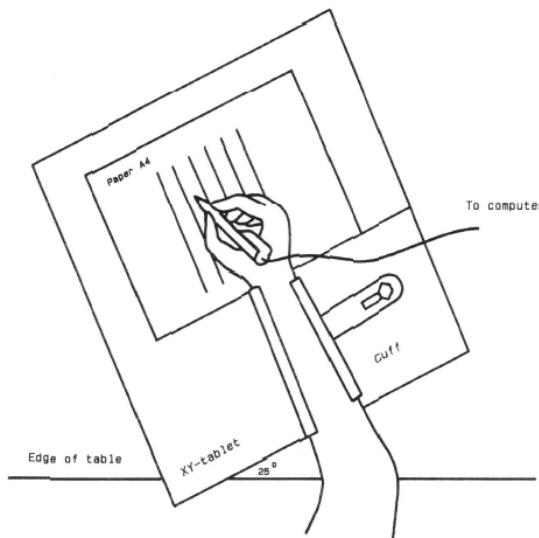
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## Slant, continued

- › Maarse (1987) investigated constancy of slant under varying wrist orientations, revealing remarkable stability of slant angle, with rotating (x',y')





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## Maarse (1987) and sequel

- › The uninstructed writer has a strong tendency to maintain slant, even at the cost of some discomfort in the pen grip
- › **Maarse, Schomaker & Teulings (1988).** With 20 writers, and single-line text samples, an identification performance of 79 in 80 (99%) was reached on LDA with five *on-line* features:
  - 1) axial pen force,
  - 2) **slant angle from polar plot,**
  - 3) average velocity while inking,
  - 4) width of rightward strokes,
  - 5) relative pendown-time vs total writing time.



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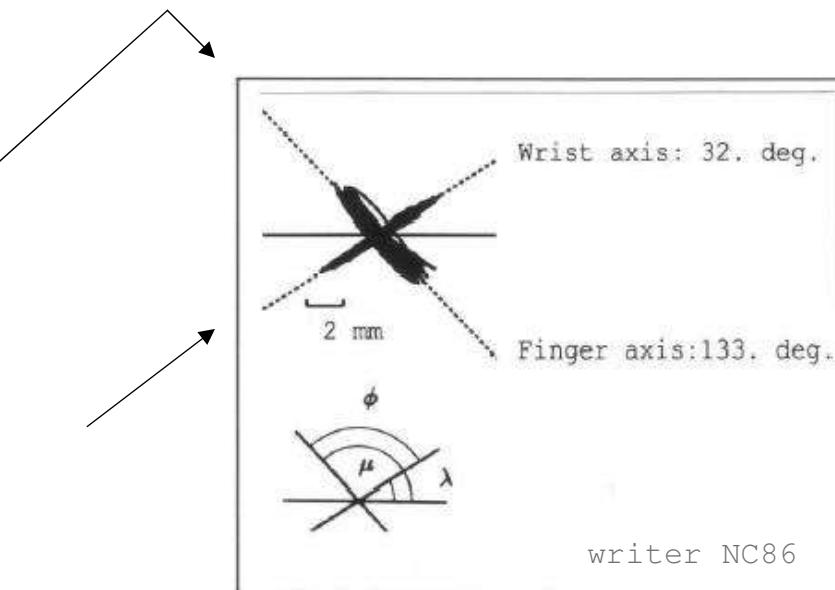


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# Slant summary

- › slant is determined by the biomechanics of the wrist/finger system in interaction with the chosen or trained pen grip

moving fingers, fixed wrist  
are more noisy than  
moving wrist, fixed fingers





# 11 yrs silence, then renewed interest

- › NFI: for the Netherlands Forensics Institute, clean handwriting samples, 250 writers, four pages per writer, were collected: **Firemaker** collection [Schomaker & Vuurpijl, 1999]
  
- › Wanda project for BKA: framework for forensic writer identification [Franke, Schomaker, Vuurpijl, Guyon, 2002]



proefnr: geb.dat: 20 11 77 man links  
(in te vullen door NICI) huisnr: 60 X vrouw rechts X

NICI datacollectie 1999

Tekst1: Bob en David ... (f100,-) uit.

**Bob,** David en sexy Xantippe sparen postzegels van de landen Egypte, Japan, Arganië, de USA, Holland, Italië, Griekenland en Canada.

Zij bezochten veilingen ~~om~~ reisden met de KLM. Voor korte afstanden huurden ze een auto, meestal een VW of een Ford.

De veilingen waren van 7-4-1993 tot 3-5-1993 in New York, Tokyo, Québec, Phoenix, Rome, Parijs, Zürich en Oslo.

Omdat de veilingen steeds begonnen om 12 uur en je gemiddeld 200 tot 300 kilometer moet rijden, slonden zij steeds om 6.30 uur op en vertrekken om 8 uur uit het hotel.

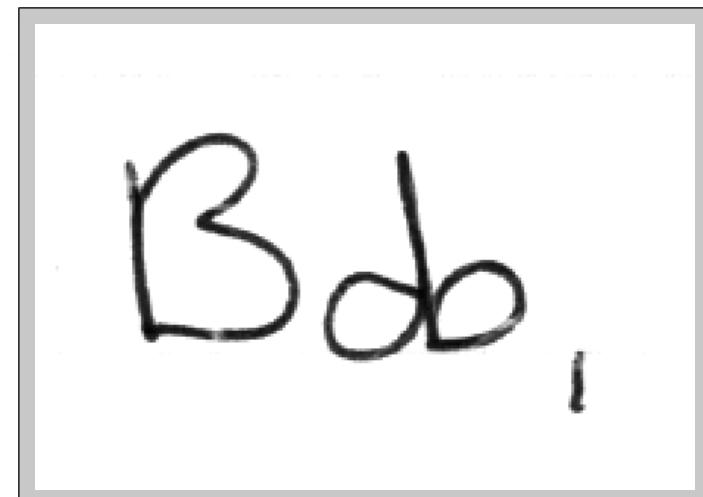
Elke dag hadden zij vijfhonderd (f500,-) gulden nodig. Daarvoor gebruikten zij elke keer een cheque van tweehonderd (f200,-) en een cheque van driehonderd (f300,-) gulden. Aan geschenken gaven ze altijd honderd gulden (f100,-) uit.

proefnr: geb.dat: 20 11 77 man links  
(in te vullen door NICI) huisnr: 60 X vrouw rechts X

NICI datacollectie 1999

Tekst4: Beschrijving cartoon.

Een mannelijke zit een vliegende schadel landen. Uit deze schadel slapt een vreemd uitziend mannetje, die het lachende mannetje hand op zijn neus stompt. Verjudens slapt het mannetje weer in zijn vliegende schadel, vliegt weg, en laat het mannetje verbaasd achter.

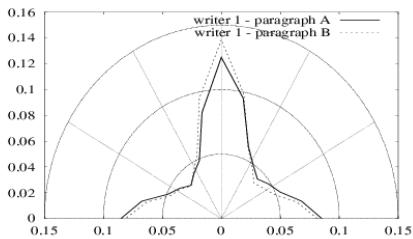


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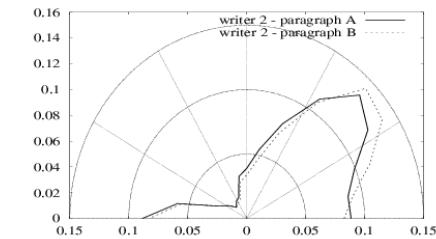


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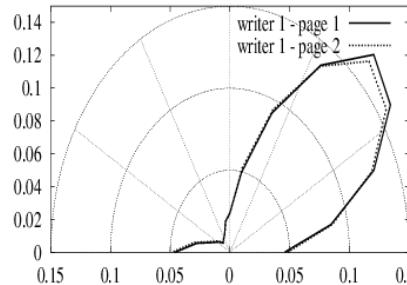
NADAT ZE IN NEW YORK  
PARIS, ZÜRICH EN OS  
VLOGEN ZO UIT DE U



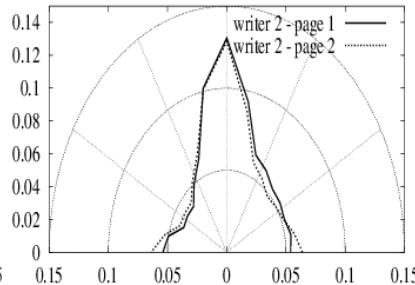
NADAT ZE IN NEW  
PARIS, ZÜRICH EN  
VLOGEN ZE UIT DE U



Onder de oelingen  
tot 300 kilometer  
en vertrekken om



Zij bezochten ve  
korte afstander  
VW of een FC



Revived\* the polar histogram  
 $r=p(\varphi)$  for  
off-line

compute angles  $\varphi$  on the ink  
edges in the image

\* [Maarse, 1988; Crettez, 1995]



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## Distance Measures

- Hamming:

$$d = \sum_i |p_i - q_i|$$

- Euclid

$$d = \sqrt{\sum_i (p_i - q_i)^2}$$

- Minkowski

$$d = \left( \sum_i |p_i - q_i|^n \right)^{1/n}$$

- Hausdorff

$$d = \max_i (|p_i - q_i|)$$

- Chi Squared ( $\chi^2$ )

$$d = \sum_i \frac{(p_i - q_i)^2}{p_i + q_i}$$

- Bhattacharyya

$$d = 1 - \sum_i p_i \cdot q_i$$



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# p( $\varphi$ ) edge-angles histogram

- › Writer identification [Bulacu & Schomaker, CAIP, 2003]
- › 250 writers, 1 vs 499 samples
- › Top-1 = 29 - 34%
- › Top10 = 66 - 79%

Are there other factors besides slant?



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# (Performance confidence margins)

$\alpha = 0.05$	Perf=90%
N:	Conf.band:
100	$\pm 6\%$
150	$\pm 5\%$
250	$\pm 4\%$
900	$\pm 2\%$



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## Pen-tip movement in 2D

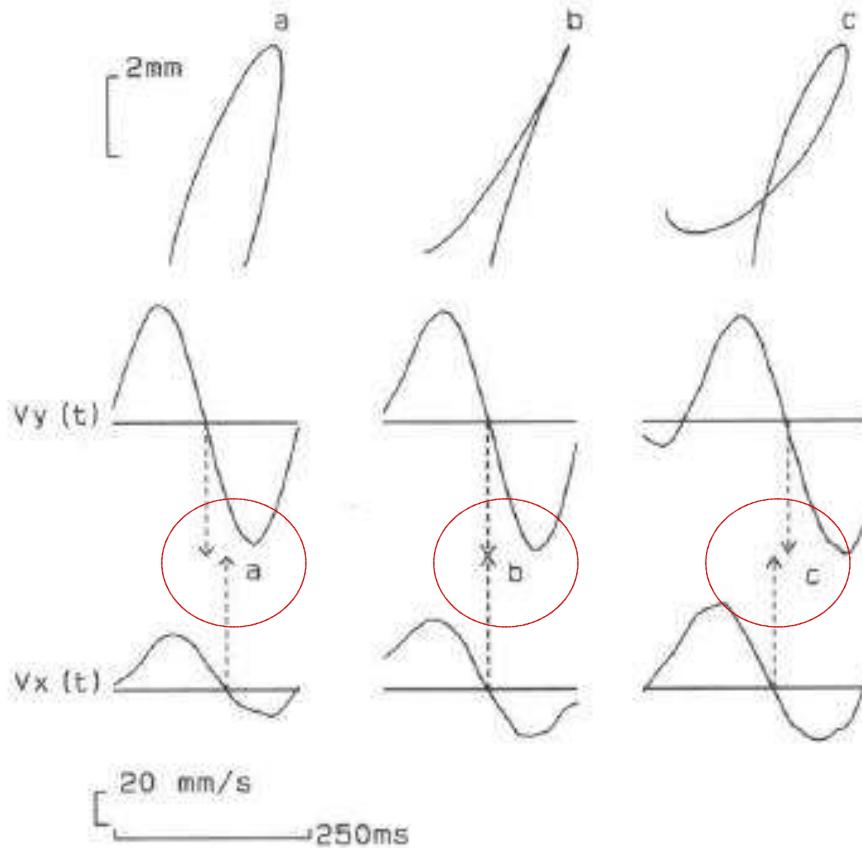
- › wrist and finger movements produce horizontally translated Lissajous patterns: pen-tip movement is a phasor signal
  - [Hollerbach, 1981; Schomaker et al. 1989]
- › roundness, curvature are clear visual characteristics



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phase  $v_y, v_x$  &  
curvature of  
handwriting:

$$\Phi = 2\pi\Delta t / T$$

$\Phi \rightarrow 90^\circ$   
“roundish”

$\Phi \rightarrow 0^\circ$   
“sharp”

Figure 2. Basic stroke shapes and their relative timing in the velocity domain, a) blunt, clockwise stroke ending,  $v_x$  lags  $v_y$ , b) sharp stroke ending, no delay, c) blunt, counter-clockwise stroke, looping with next stroke,  $v_x$  leads  $v_y$  in time. [Schomaker, 1991]



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# Roundness of handwriting

- › is caused by the differential phase modulation for the **wrist** and the **finger** system
- › Roundness: “transfer function for time signals”
- › (Slant: “affine transform”)

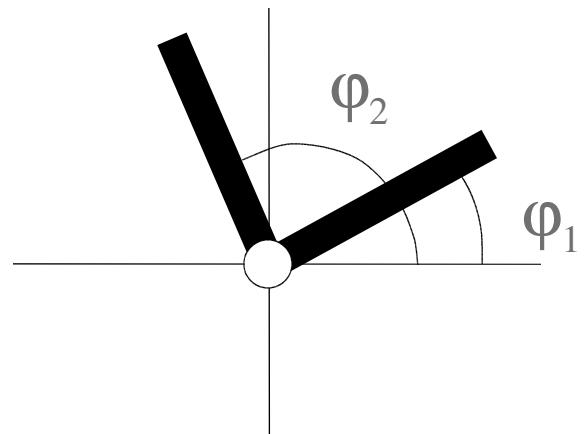
## Hinge feature

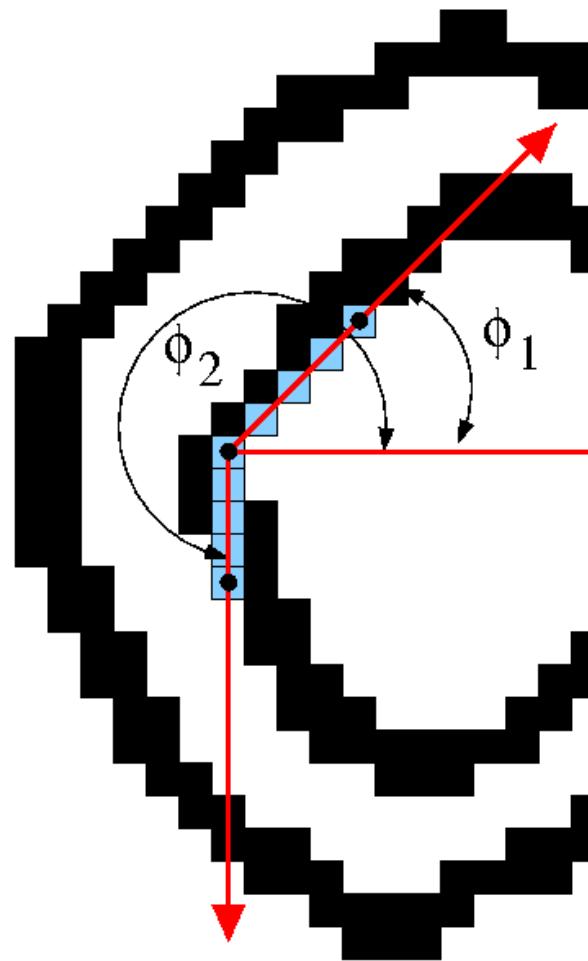
[Bulacu & Schomaker, 2003]

- › combines slant information
- › and curvature information
- › is a transform on images

$$p(\varphi_1, \varphi_2) = H(\varphi_1, \varphi_2, I(x, y))$$

- › where the angles  $\varphi_1, \varphi_2$  refer to the legs of a hinge
- › probability of angular co-occurrence in hinge patterns along ink contour







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# Computing the hinge transform

- › Find contours along ink
- › Define a set of hinges:  $\varphi_1, \varphi_2$  combinations
- › And count their occurrence:  $p(\varphi_1, \varphi_2)$

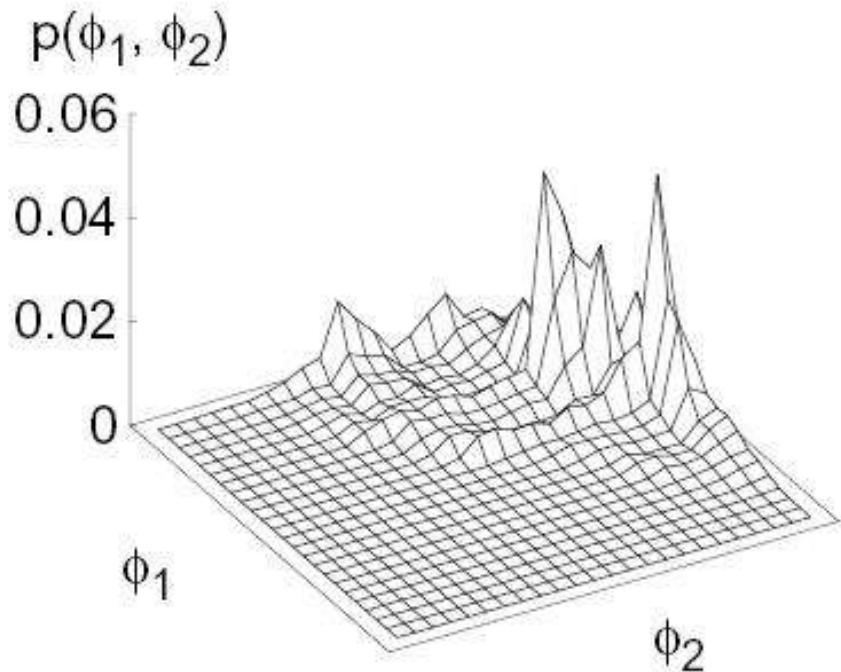


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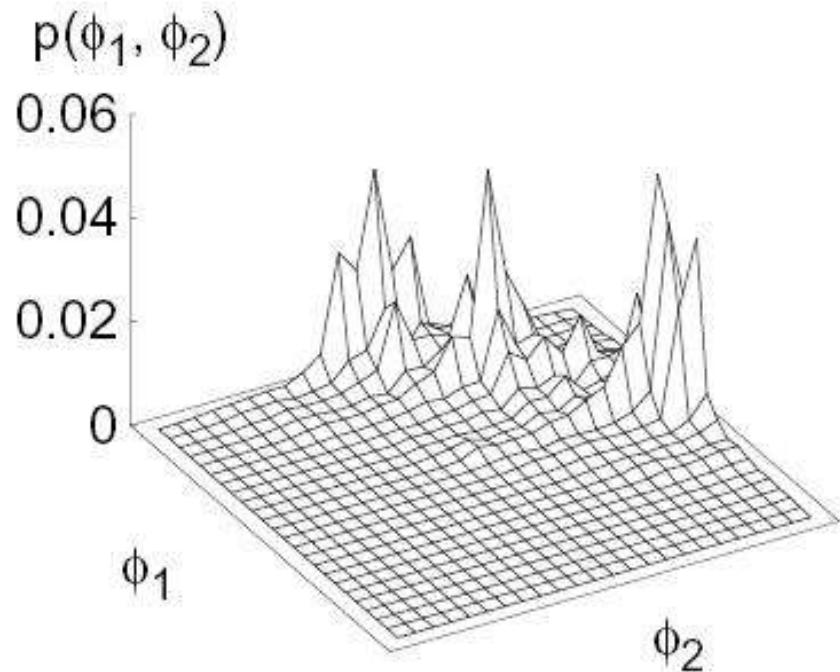
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writer 1 - sample 1



writer 2 - sample 1



[Bulacu &amp; Schomaker, PAMI, 2007]



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## $p(\phi_1, \phi_2)$ hinge histogram [Schomaker & Bulacu, PAMI, 2004]

- › Writer identification, Upper case
- › nearest neighbour,  $\chi^2$  (Chi square) distance measure
- › 250 writers, 1 vs 499 samples
- › Top-1=83%
- › Top10=97%



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## Part II individual's use of character shapes

- › textural features are informative
- › what about detailed character shape: **allography?**



# Allographs & shape families

g g y y h h k k

id-1

g g y y h h k k

id-2

g g y y h h k k

Writer

id-3

g g y y h h k k

id-4

g g y y y h h k k

g g y y y h h k k



# How to use allographic information?

- › There is no commonly accepted global list of character shapes (allographs) for Western handwriting, nor for other scripts
  
- › Avoid cumbersome human work  
(prefer ‘automatic’, ROI based analysis)



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# Allographic writer identification

## › Assumption:

- given an exhaustive table of allographs:  $L(\lambda, v_\lambda)$  for all letters  $\lambda$  and their variants  $v_\lambda$
- each writer  $w$  is characterized by
$$w \xrightarrow{\quad} p(L)$$
- i.e., a distribution of probabilities of emission of each allograph, by writer  $w$



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# Allographic writer identification

- › Hypothesis:
  - given an estimated table of character fraglets:  $F(v)$  with shapes numbered  $v$ ,
  - assuming that each fraglet is a *distinct* building block for one or more allographs,
  - then each writer  $w$  can be characterized by
$$\overset{\rightarrow}{w} = p(F)$$
  - i.e., a distribution of probabilities of emission of character fraglets, by writer  $w$



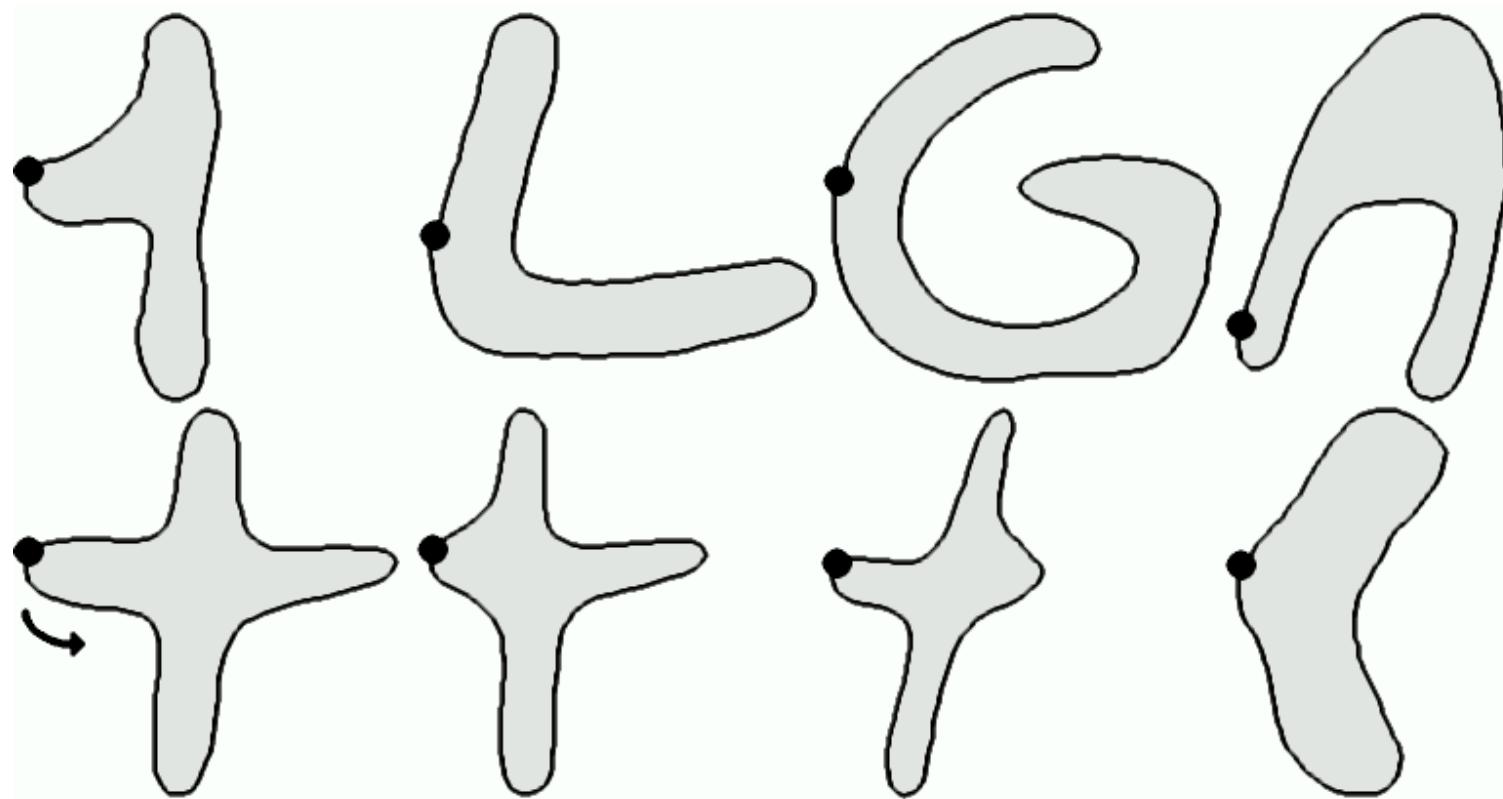
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# Connected-Component Contours ( $\text{CO}^3$ )





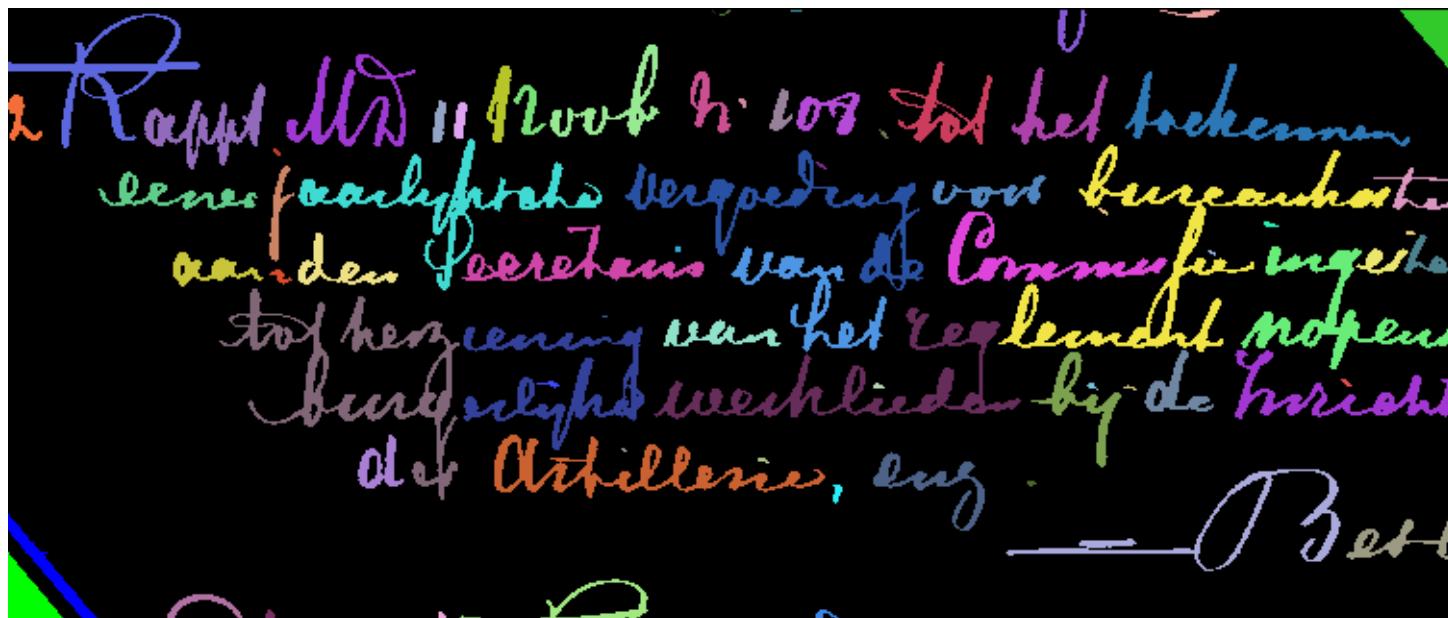
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CO<sup>3</sup> works in UPPER case.  
How about connected cursive?



→ Connected components in cursive script  
are too complex in shape



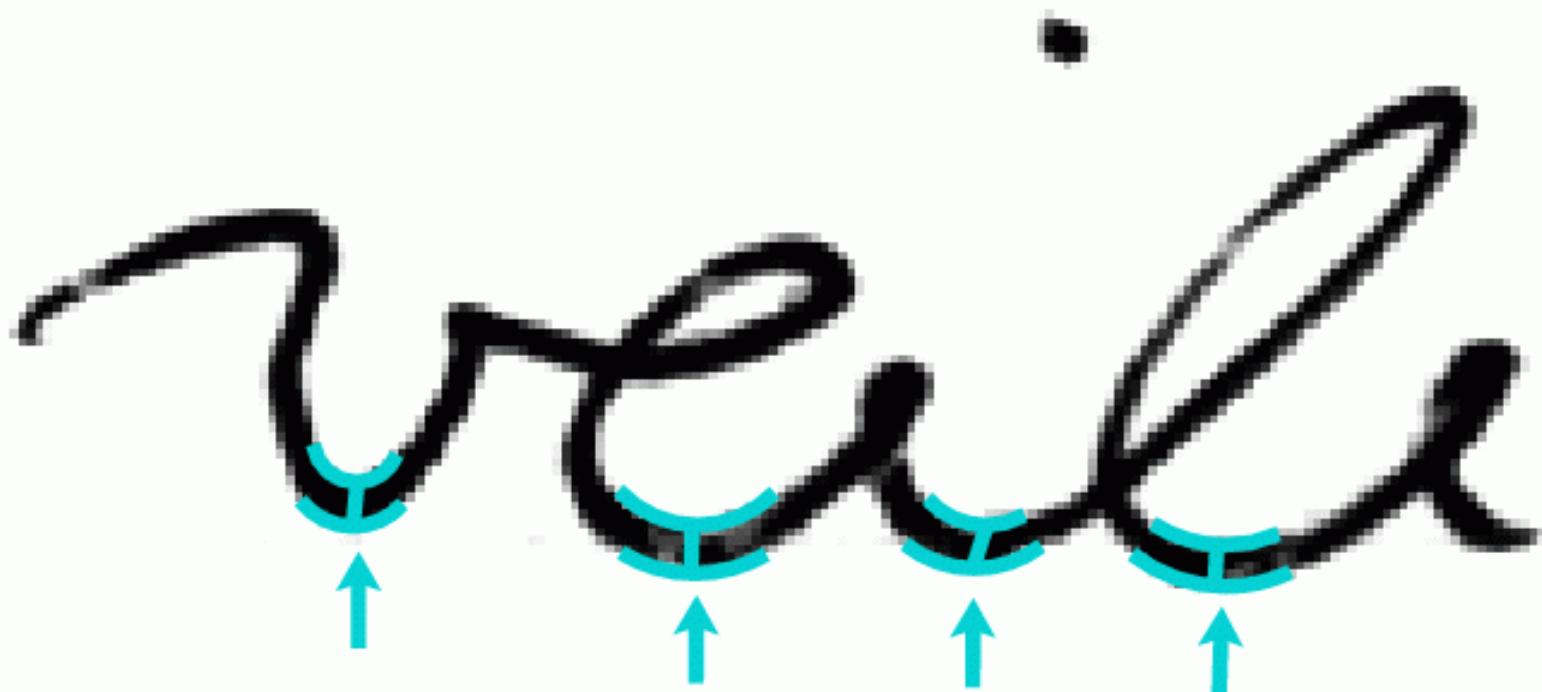
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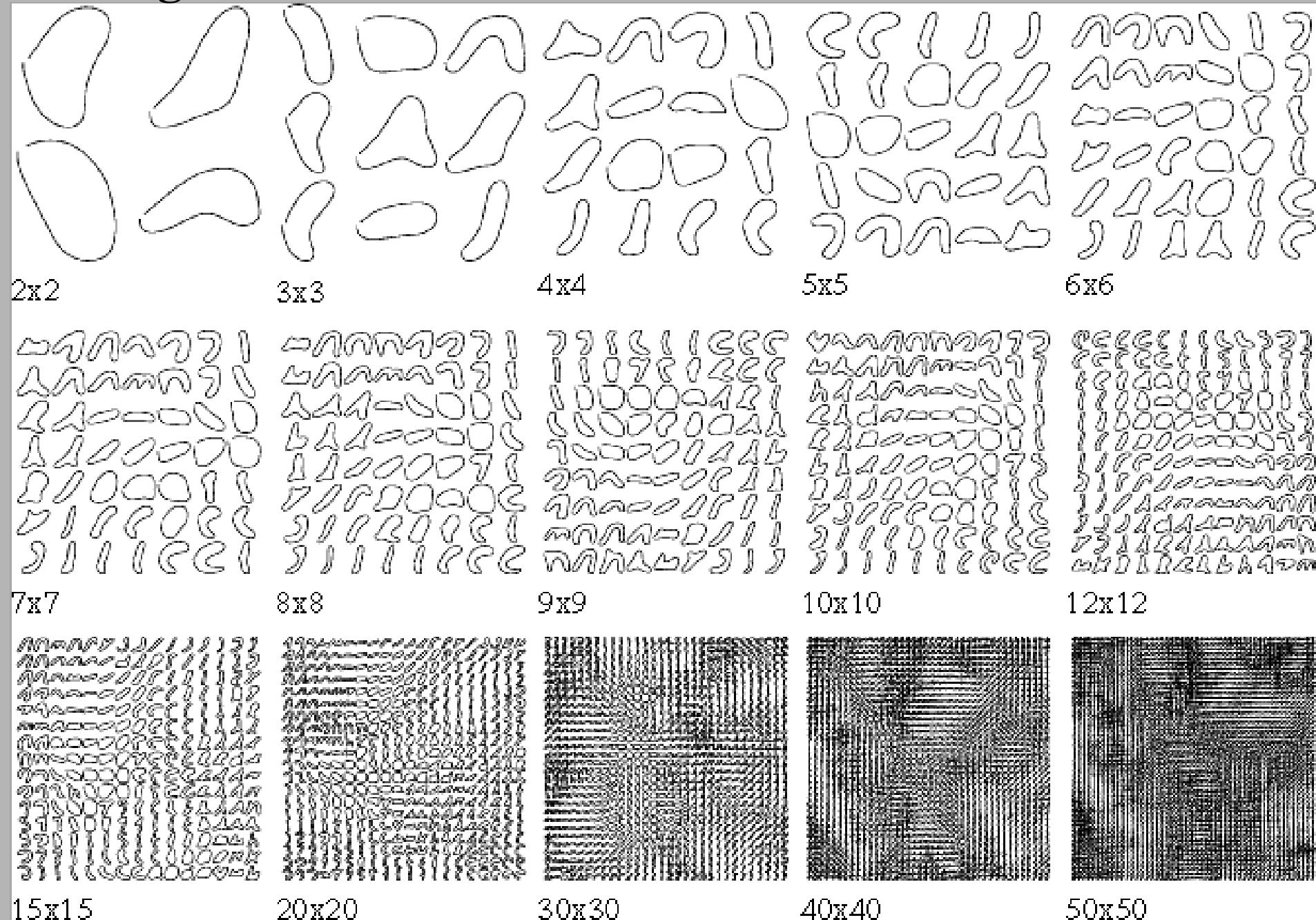
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## Segment cursive patterns into fragmented CoCos



cf. [Bensefia & Paquet, 2005]

# Fragmented CO<sup>3</sup> Kohonen SOFMs



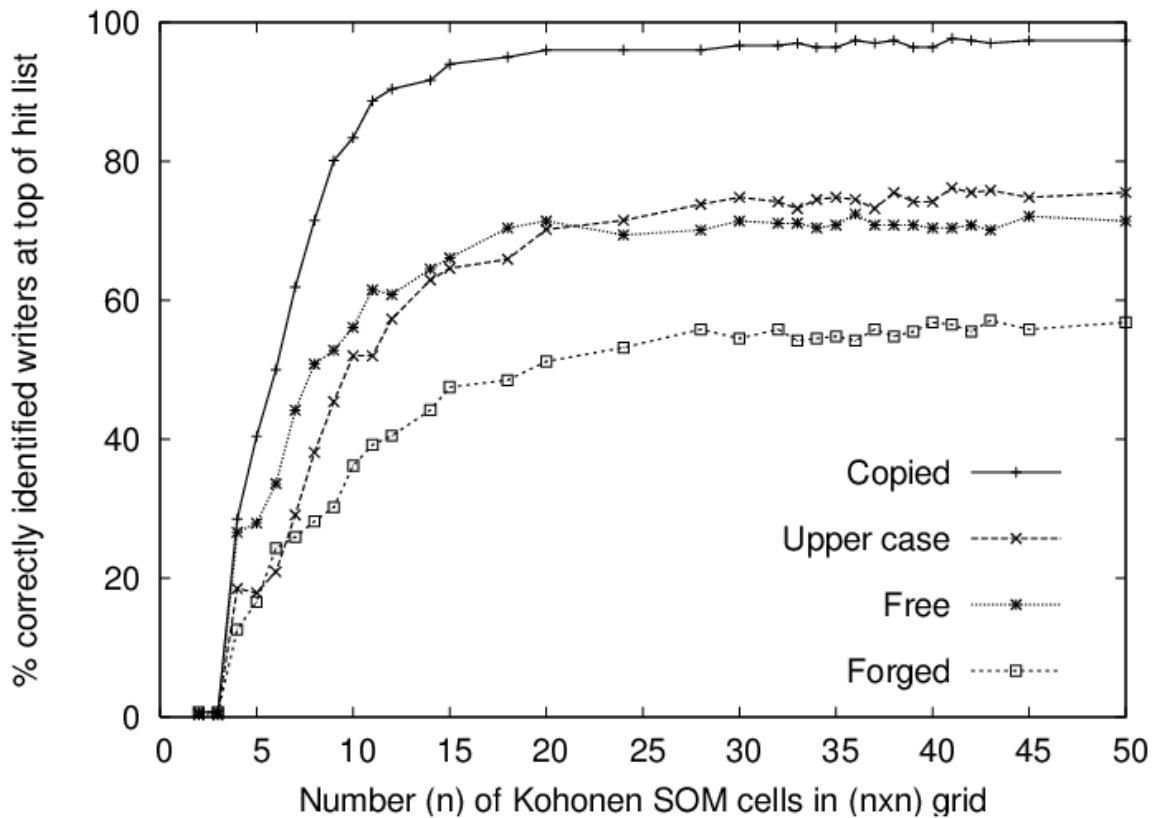


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# Codebook size and performance



Schomaker, L.R.B. & Bulacu, M. & Franke, K. (2007). Automatic Writer Identification Using Fragmented Connected-Component Contours, In: F. Kimura & H. Fujisawa, Proc. of the 9<sup>th</sup> IWFHR, IEEE Computer Society, pp. 185-190.

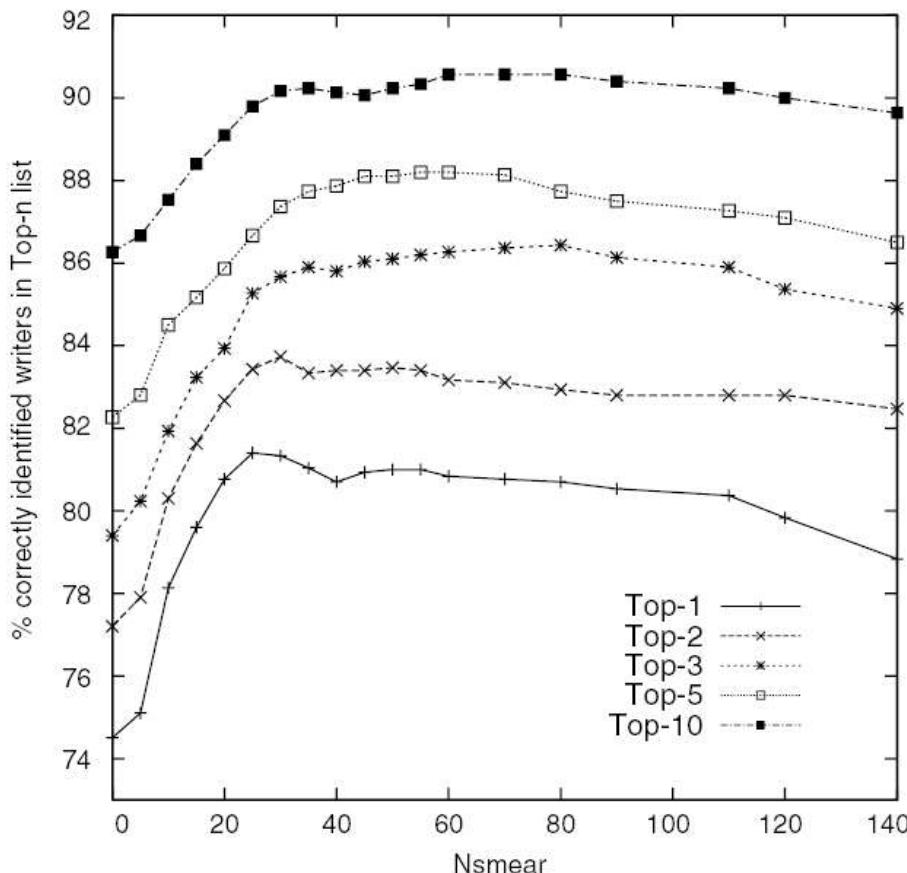


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# Improved robustness by smearing tallies



Schomaker, L.R.B., Franke, K. & Bulacu, M. (2007). Using codebooks of fragmented connected-component contours in forensic and historic writer identification, *Pattern Recognition Letters*, 28(6), p. 719-727.

Nsmear: the number of 1NN feature-space neighbours in the codebook to receive a tally, given a connected-component instance



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**Count fraglet  
occurrence in  
input sample**

**compare to  
reference  
vectors**

**use Hamming or  
Chi-square  
distance**

## P(CO<sup>3</sup>) images

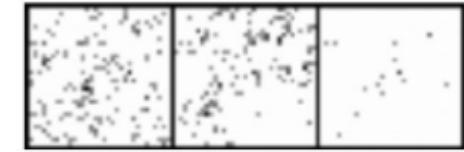
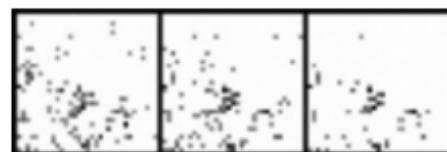
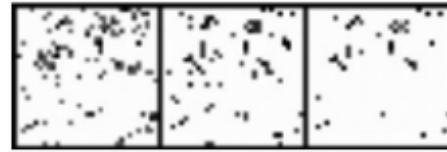
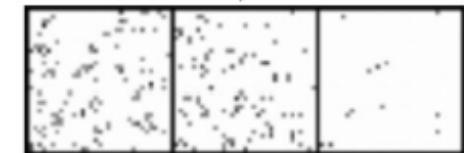
Same writer

$A_w$     $B_w$    Common



Different writer

$A_w$     $B_{v \neq w}$    Common



**Query: Writer 570**

NADAT ZE IN NEW YORK  
QUEBEC, PARIJS, ZÜRICH EN  
GEWEEST, VLOGEN ZE UIT T  
MET VLUCHT KL 658 OM 12 UUR

**1. Writer 570 (D=1.293) CORRECT**

ZE KWAKKEN AAN IN DUS  
UUR EN IN AMSTERDAM OF  
'S AVONDS. DE FIAT VAN BE  
VN VAN DAVID STONDEN

**3. Writer 424 (D=1.391)**

NADAT ZE IN NEW YORK, T  
, PARYS, ZÜRICH EN OSLO W  
, VLOGEN ZE UIT DE USAAT  
VLUCHT KL 658 OM 12 I

**5. Writer 514 (D=1.417)**

NADAT ZE IN NEWYORK, TOKI  
PARYS, ZÜRICH EN OSLO WA  
VLOGEN ZE UIT DE USA TEI

**7. Writer 408 (D=1.430)**

NADAT ZE IN NEW YORK  
QUEBEC, PARYS, ZÜRIC  
OSLO WAREN GEWEEST,  
ZE UIT DE USA TERU

**9. Writer 530 (D=1.468)**

NADAT ZE IN NEW YORK, TOKYI  
PARIJS, ZÜRICH EN OSLO WAREI  
VLOGEN ZE UIT DE USA TERU

**2. Writer 567 (D=1.378)**

NADAT ZE IN NEW YORK, TOKYO  
ZÜRICH EN OSLO WAREN GEWEEST  
DE USA TERUG MET VLUCHT KL I

**4. Writer 552 (D=1.395)**

NADAT ZE IN NEW YORK, T  
QUEBEC, PARYS, ZURICH  
WAREN GEWEEST, VLO  
UIT DE USA TERUG

**6. Writer 498 (D=1.425)**

NADAT ZE IN NEW YORK, QUÉBEC  
EN OSLO WAREN GEWEEST, VLOGEI  
USA TERUG MET VLUCHT KL 658

**8. Writer 493 (D=1.466)**

NADAT ZE IN NEW YORK, T  
PARIJS, ZÜRICH EN OSLO WA  
VLOGEN ZE UIT DE USA TER  
VLUCHT KL 658 OM 12 UUR

**10. Writer 447 (D=1.475)**

NADAT ZE IN NEW YORK, TOKYC  
PARYS, ZÜRICH EN OSLO WAF  
VLYGEN ZE UIT DE USA TERU

# Sample hit list



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## Identification Performance [Schomaker & Bulacu, 2005]

Feature / Method	N Writers	lowercase		UPPERCASE	
		Top 1	Top 10	Top 1	Top 10
hinge	$p(\phi)$	150	53%	88%	34% 79%
	$p(\phi_1, \phi_2)$	150	84%	97%	84% 97%
	$p(\phi_p, \phi_3)$	150	70%	94%	68% 91%
fraglets	$p(CO^3)$	150	--	--	72% 93%
	$p(FCO^3)$	150	71 - 97%	90 - 100%	73% 91%
	system A	100	34%	90%	-- --
	system B	100	65%	90%	-- --



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## Single features, 900 writers [Bulacu &amp; Schomaker, 2006]

	Feature	Identification		Verification EER
		Top 1	Top 10	
hinge	$f1$	$p(\phi)$	43	72
	$f2$	$p(\phi_1, \phi_2)$	80	91
	$f3h$	$p(\phi_1, \phi_3)$ h.	65	84
	$f3v$	$p(\phi_1, \phi_3)$ v.	59	82
fraglets	$f4$	$p(g)$	76	92
	$f5h$	$p(rl)$ h.	8	29
rl white	$f5v$	$p(rl)$ v.	10	34



## Combination performance [Bulacu & Schomaker, 2006]

- › f1: hinge histogram
- › f2: fraglet histogram
- › f3: white run-length histogram
- › average the distances (Chi square)
- › 900 writers
- › Top1: 87 %
- › Top10: 96%
- › EER: 2.6%              **Using a single writer-independent threshold**



## Other features tested

- › Variants on hinge (angle-line-angle, ‘ala’)
- › Ink deposition
  - Brush (ink-density related)
- › Placement statistics
  - Autocorrelation
  - Horizontal runlength of white
  - Vertical runlength of black
- › Misc.
  - #bytes after Lempel-Ziff / #black\_pixels
  - wavelets



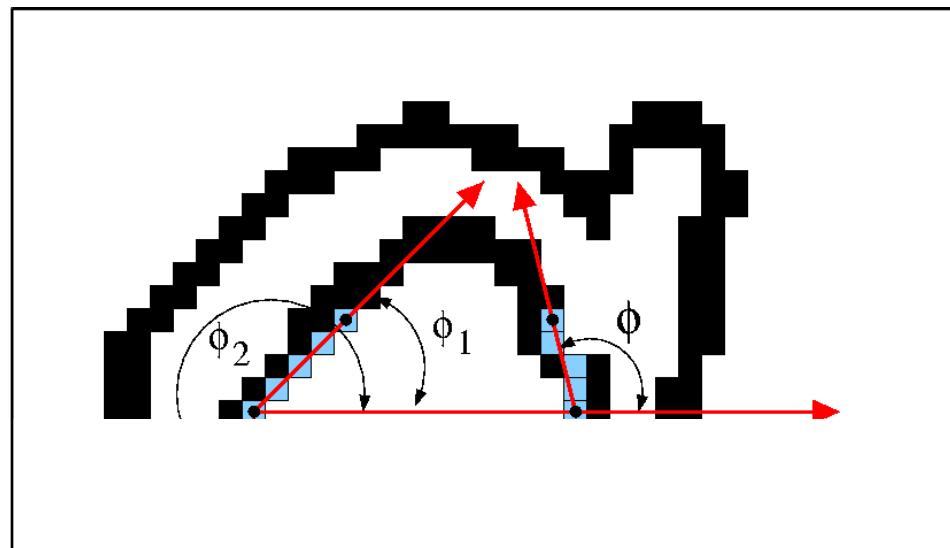
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## Habitual slant & angle co-occurrence ‘ala’

- ›  $P(\Phi_1, \Phi)$  where  $\Phi$  is the angle of the edge to the right of  $\Phi_1$  after crossing a non-edge zone [Bulacu & Schomaker, 2003]





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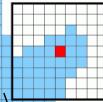
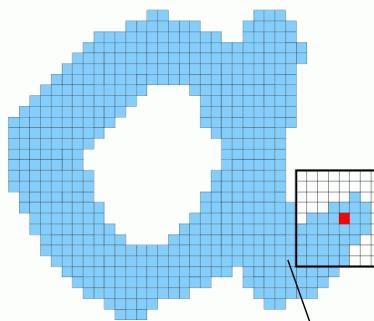


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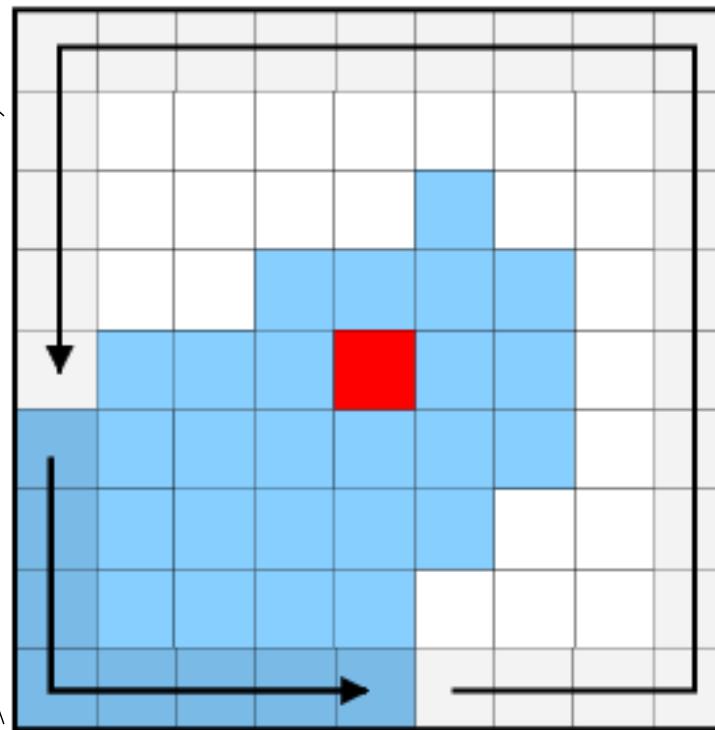
## Ink deposition

- › Doermann, ICPR 1992
- › Franke & Rose (2004);  
Franke, Schomaker  
& Köppen (2005):  
analysis of ink traces  
by industrial robot





Run length, background (Lw)



Center pixel

Background

Ink

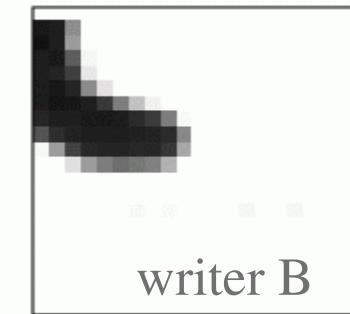
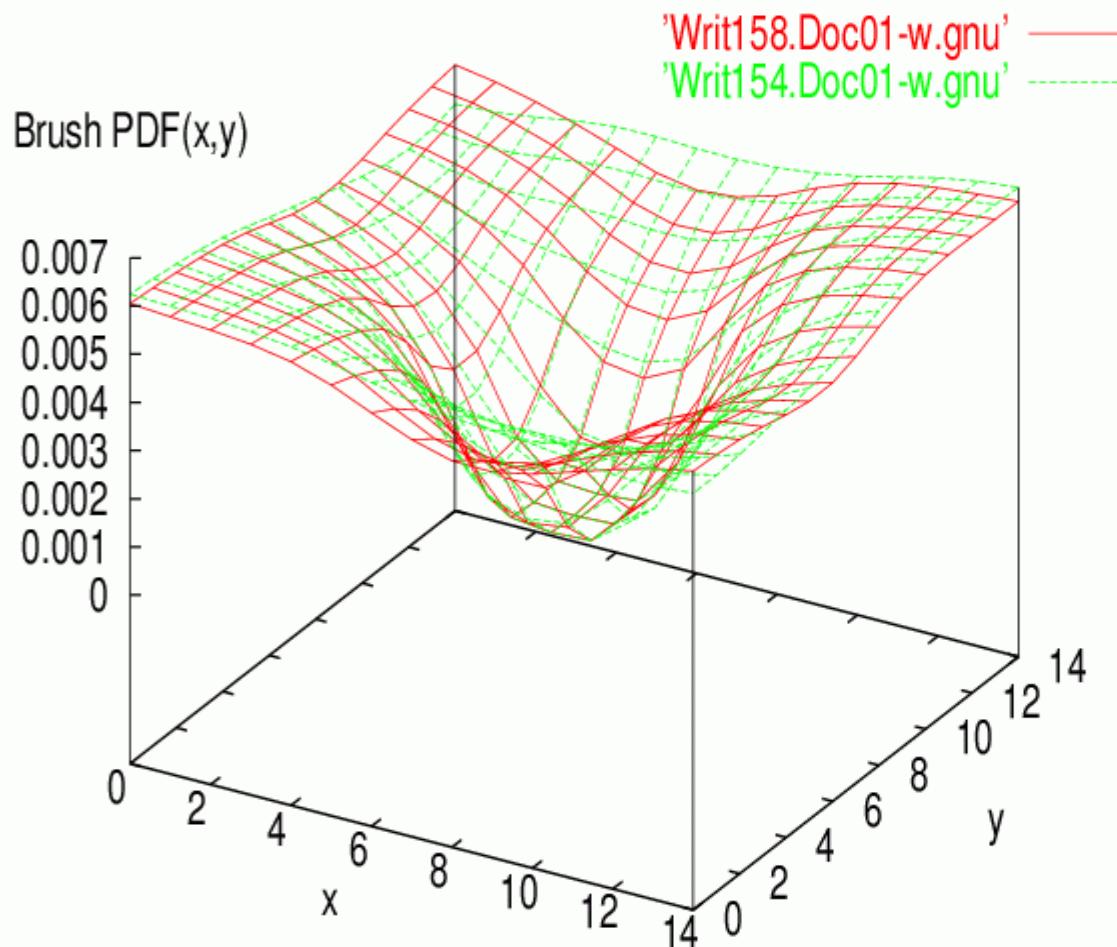
Perimeter pixels:

Ink

Background

Run length, ink (Lb)

# Brush feature [Schomaker et al., ICIP '03]



Writer identification, 250 writers:

Top1: 53-69%, Top10: 81-93%



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# Other features UPPER case

Not so good

Nearest-Neighbor Performance of Other Features on  
Set "ab:" Leave One Out (1 versus 299 Samples),  
N = 150 Writers, as Before

Feature	Description	Ndim	Top1 (%)	Top10 (%)
e	normalized entropy	1	2	19
w1	wavelets,Haar	99	5	14
w2	wavelets,Odegard	99	14	28
w3	wavelets,Adelson	99	14	29
w4	wavelets,Antonini	99	14	29
w5	wavelets,Brislawn	99	14	29
w6	wavelets,Daubechies 14	99	15	29
w7	wavelets,Villasenor 2	99	15	30
v	vertical run-length PDF	100	21	61
r	horizontal autocorrelation	100	25	61
h	horizontal run-length PDF	100	26	66
f0	edge-angular PDF	16	34	79
b	brush feature, 15x15	225	69	93
f1	$CO^3$ PDF	1089	72	93
f2	hinge-angular PDF	464	80	97

Given are the dimensionality Ndim of the feature vectors and the Top1 and Top10 percentages of the correct writer found in a sorted hit list of size 1 and 10, respectively.



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# “comparison” with other systems

<i>Method/Feature</i>	<i>N</i> <i>writers</i>	<i>Top-1</i> (%)	<i>Top-10</i> (%)	<i>EER</i> (%)	<i>Match</i>	<i>Notes</i>	
misc. features	20	91	-	-	MLP	w [17]	Marti et al
‘SysA’	100	34	90	-	-	w [28]	
‘SysB’	100	65	90	-	LDA	w [28]	
char. models	100	-	-	0.9	HMM	w [25]	Bunke et al
co3	150	72	93	-	1NN	p,U [28]	
brush	250	53	81	-	1NN	n [30]	
splitEdge	250	29	69	-	1NN	n [3]	
splitAla	250	64	86	-	1NN	n [3]	
splitHinge	250	79	96	-	1NN	n [3]	
fco3	900	76	92	5.8	1NN	p [4]	
hinge+fco3+runl	900	79	96	3.3	1NN	p [4]	
misc. features	1500	96	-	3.5	1NN	w [33]	Srihari et al



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# Wrapping up

- › Hinge and allographic fraglet methods are powerful
- › Automatic ‘ROI’ based methods work!
  - Also on Arabic and historical manuscripts!
  - No writer-specific training
- › Combining textural and allographic features improves performance
- › Human experts are still better at verification!



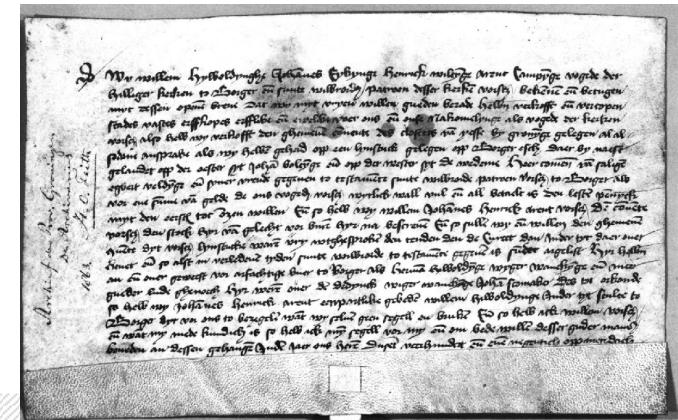
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# Future work

- > Sensitivity to amount of text in the sample
- > Asymptotic performance?
- > Explainable decisions?
- > Scribe classification of historical charters
  - [Bulacu & Schomaker, ICIAP, 2007]
- > ... new features [Brink, ...]
- > Writer-specific verification





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<http://www.ai.rug.nl/~lambert/publications.html>



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